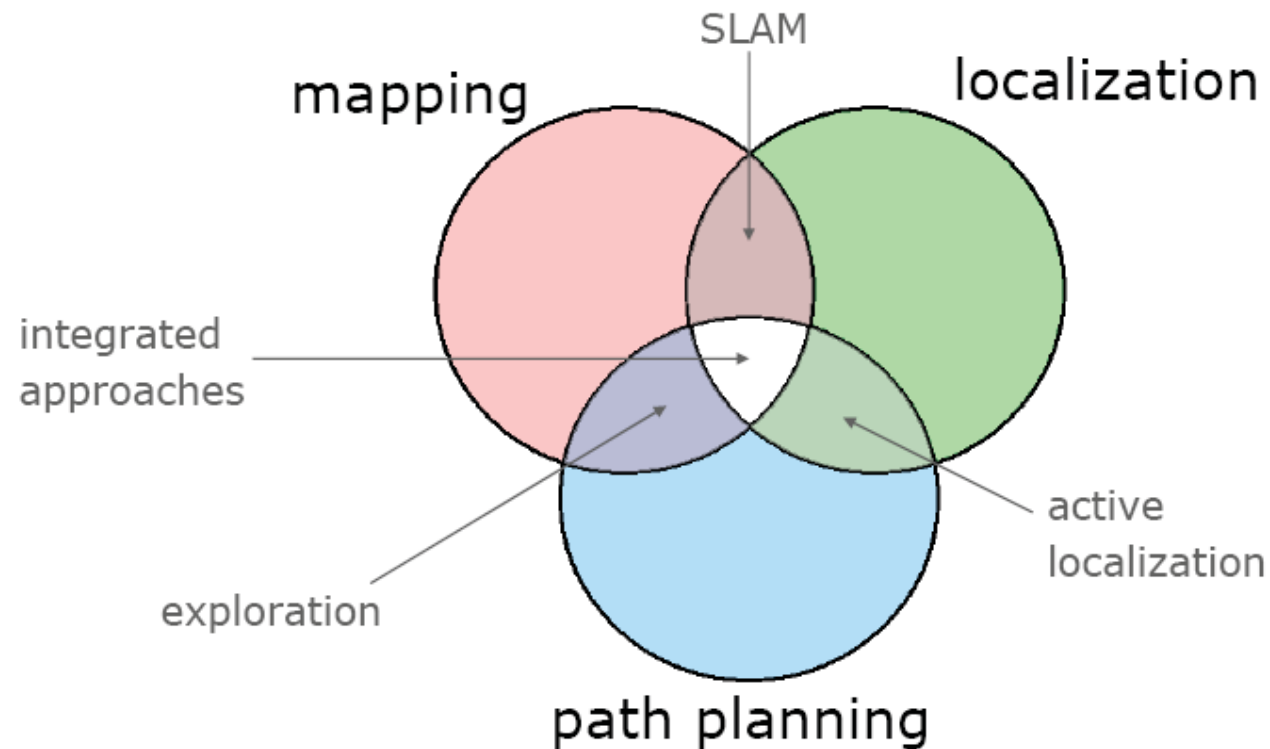


# Robotica Probabilistica

## **Information Gain-Based Exploration**

# Task dei Robot Mobili



# Esplorazione e SLAM

- SLAM is typically **passive**, because it consumes incoming sensor data
- Exploration **actively guides the robot** to cover the environment with its sensors
- Exploration in combination with SLAM: **Acting under pose and map uncertainty**
- Uncertainty should/needs to be taken into account when selecting an action

# Filtri Particellari

- Each particle represents a possible trajectory of the robot
- Each particle
  - maintains its own map and
  - updates it upon “mapping with known poses”
- Each particle survives with a probability proportional to the likelihood of the observations relative to its own map

# Fattorizzazione

poses map observations & odometry

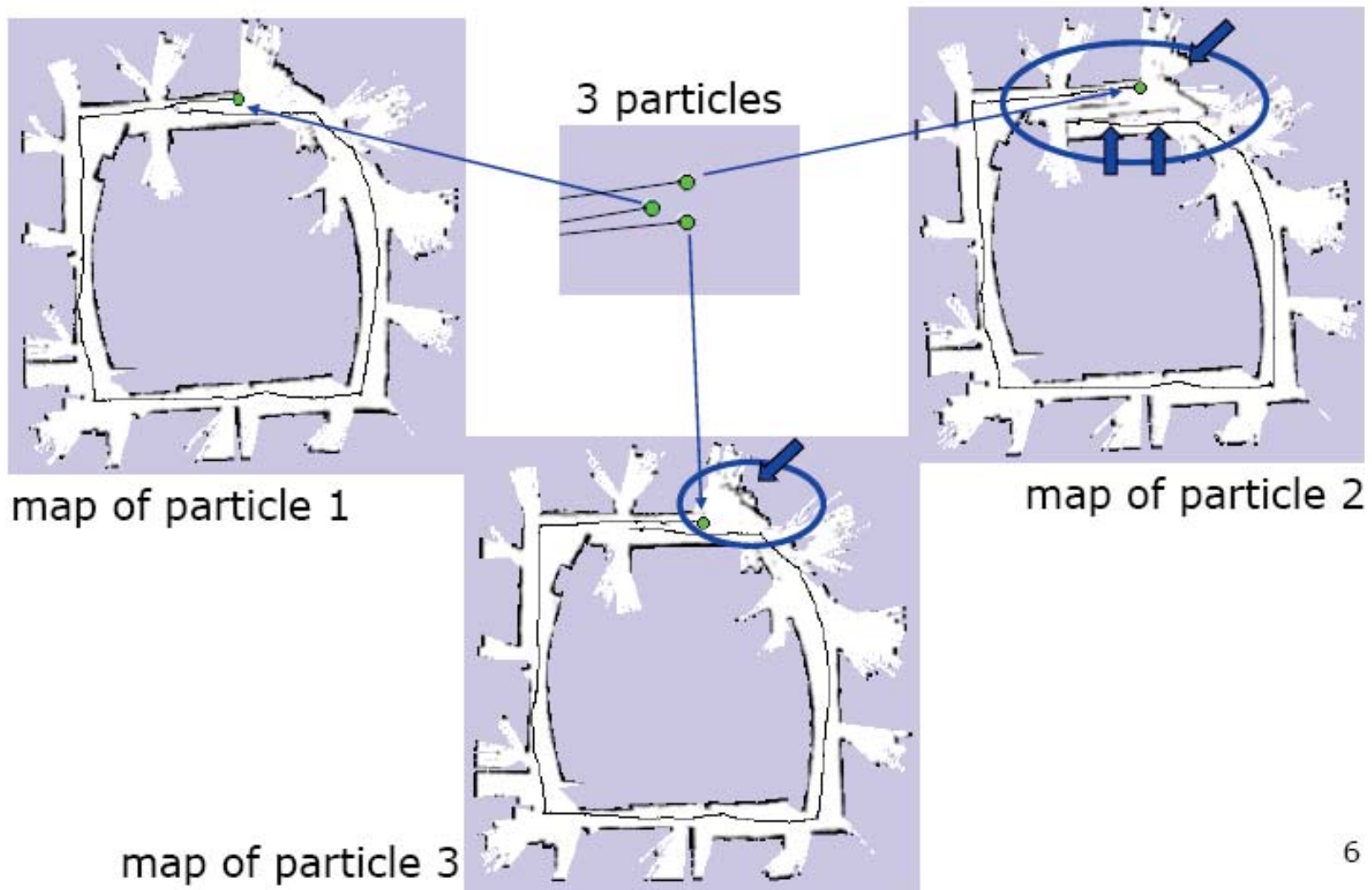
$$p(x, m | z, u)$$

$$= p(m | x, z, u) p(x | z, u)$$

Mapping with known poses

Particle filter representing trajectory hypotheses

# Filtri Particellari



# FastSLAM



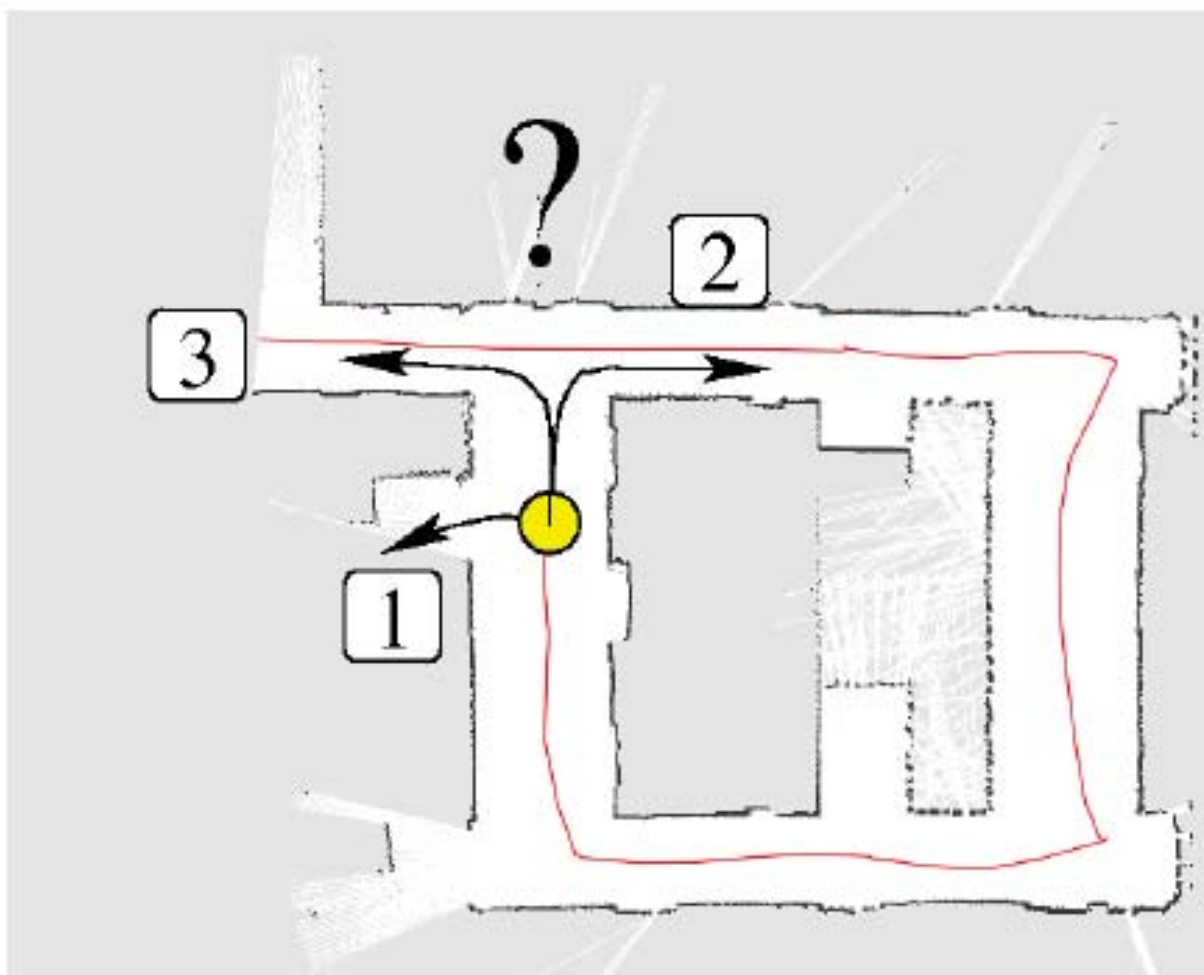
- **30 particles**
- 250x250m<sup>2</sup>
- 1.75 km (odometry)
- 20cm resolution during scan matching
- 30cm resolution in final map

# Esplorazione

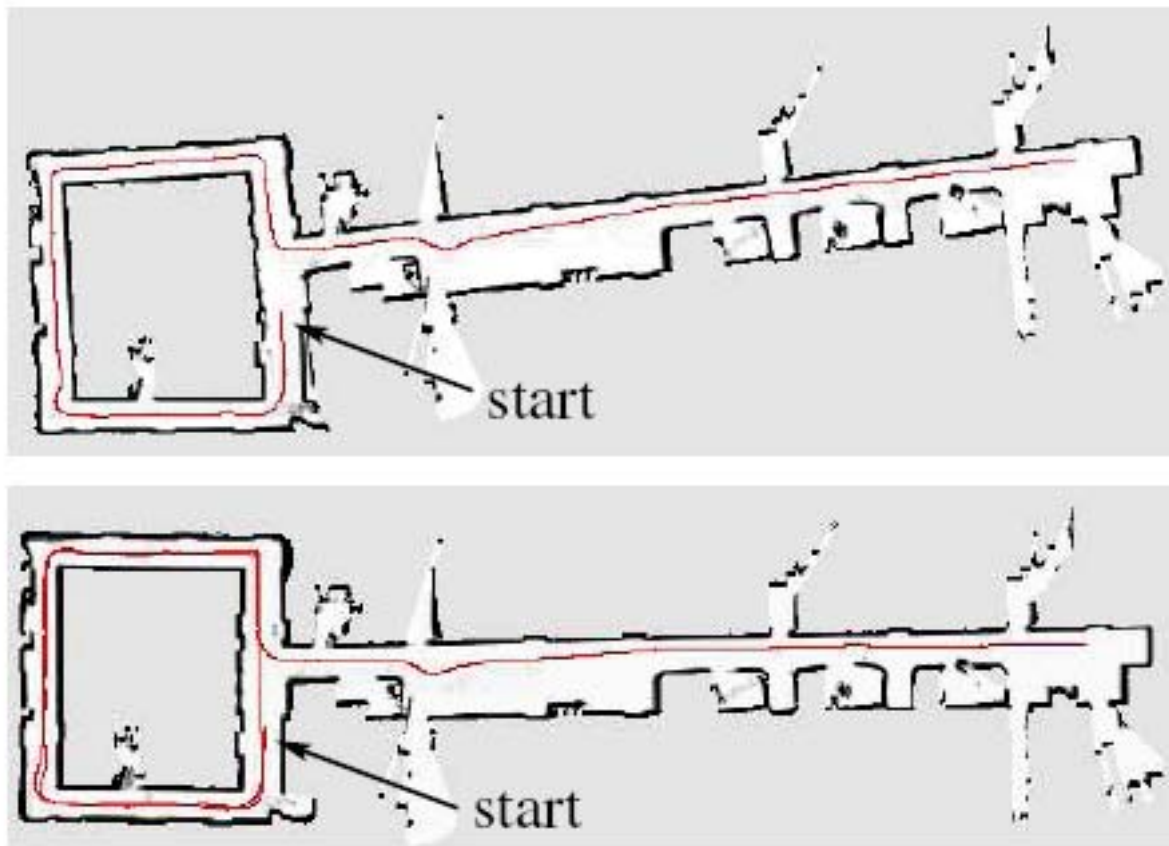
- The approaches seen so far are purely passive
- By reasoning about control, the mapping process can be made much more effective
- Question: **Where to move next?**



# Esplorazione



# Esplorazione vs SLAM



La strategia di esplorazione determina la qualità della mappa

# Approccio Decision-Teoretico

- Learn the map using a Rao-Blackwellized particle filter
- Consider a set of potential actions
- Apply an exploration approach that minimizes the overall uncertainty

**Utility = uncertainty reduction - cost**

# Incertezza Posterior

- Entropy is a general measure for the uncertainty of a posterior

$$\begin{aligned} H(p(x)) &= - \int_x p(x) \log p(x) dx \\ &= E_x[-\log(p(x))] \end{aligned}$$

- Information Gain = Uncertainty Reduction

$$I(t + 1 | t) = H(p(x_t)) - H(p(x_{t+1}))$$

# Calcolo Entropia

$$\begin{aligned} H(p(x, y)) &= E_{x,y}[-\log p(x, y)] \\ &= E_{x,y}[-\log(p(x) p(y | x))] \\ &= E_{x,y}[-\log p(x)] + E_{x,y}[-\log p(y | x)] \\ &= H(p(x)) + \int_{x,y} -p(x, y) \log p(y | x) dx dy \\ &= H(p(x)) + \int_{x,y} -p(y | x)p(x) \log p(y | x) dx dy \\ &= H(p(x)) + \int_x p(x) \int_y -p(y | x) \log p(y | x) dy dx \\ &= H(p(x)) + \int_x p(x) H(p(y | x)) dx \end{aligned}$$

# Calcolo incertezza della Mappa e della Posa

$$H(p(x_{1:t}, m | d_t)) = H(p(x_{1:t} | d_t)) + \int_{x_{1:t}} p(x_{1:t} | d_t) H(p(m | x_{1:t}, d_t)) dx_{1:t}$$

Data la rappresentazione approssimata

$$H(p(m, x_{1:t} | d_t)) \approx H(p(x_{1:t} | d_t)) + \sum_{i=1}^{\#particles} \omega_t^{[i]} H(p(m^{[i]} | x_{1:t}^{[i]}, d_t))$$

Incertezza percorso + incertezza mappa

# Incertezza del posterior nelle Grid Map

Ogni cella è una variabile aleatoria binaria

Occupancy Grid map  $m$ :

$$H(p(m)) = - \sum_{c \in m} p(c) \log p(c) + (1 - p(c)) \log(1 - p(c))$$

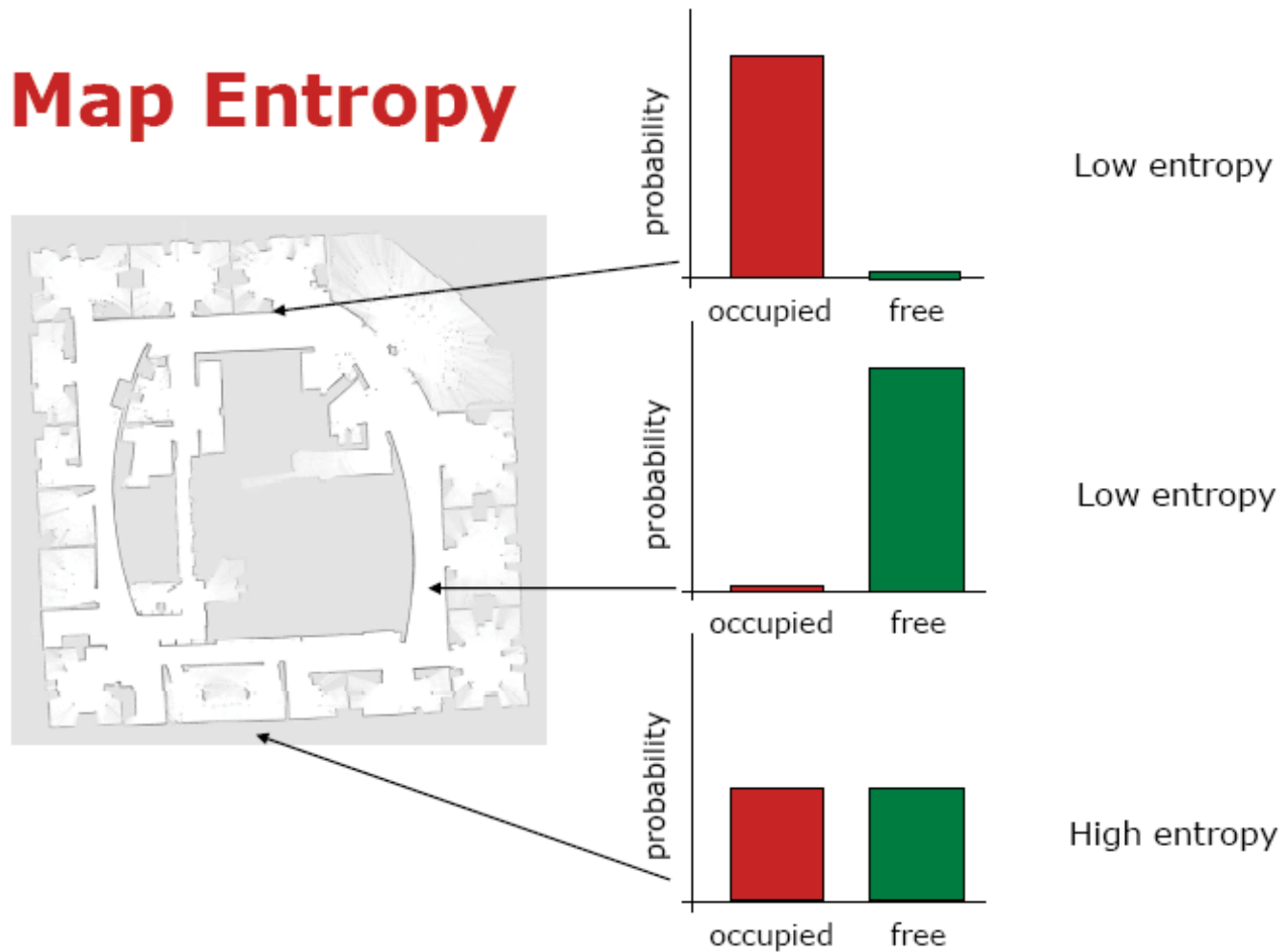
map  
uncertainty

grid cells

probability that the  
cell is occupied

# Entropia della Mappa

## Map Entropy



The overall entropy is the sum of the individual entropy values



# Incerteza sulla traiettoria

- Ogni posa dipende dalle pose precedenti  $0:t-1$
- Approssimazione con incerteza media sul percorso:  $H(p(x_{1:t}|d_t))$
- Posterior su traiettoria rappresentato come gaussiana

# Incerteza sulla traiettoria

## 1. High-dimensional Gaussian

$$H(\mathcal{G}(\mu, \Sigma)) = \log((2\pi e)^{(n/2)} |\Sigma|)$$

reduced rank for sparse particle sets

## 2. Grid-based approximation

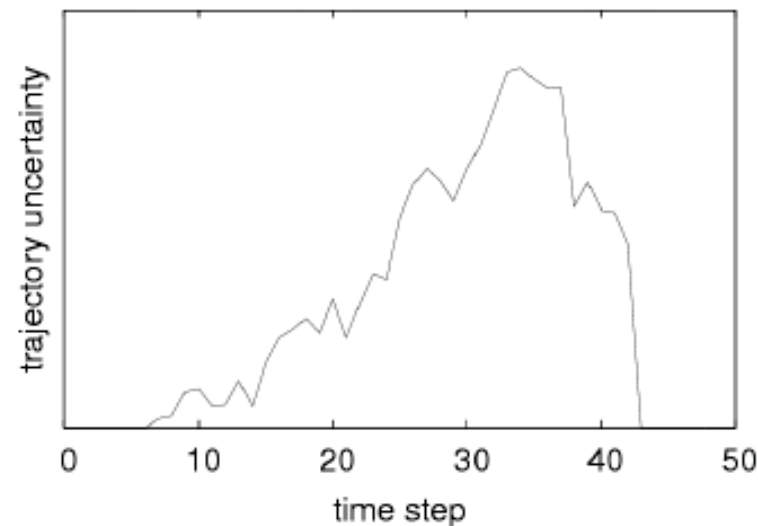
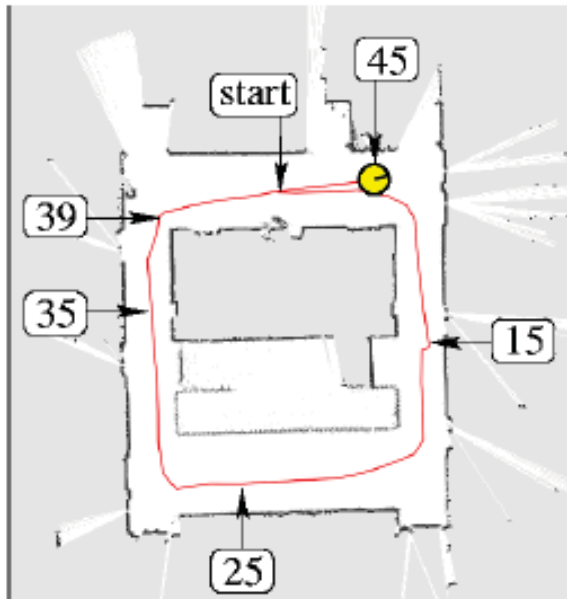
$$H(p(x | d)) \rightsquigarrow \text{const.}$$

for sparse particle clouds

# Approssimazione incertezza sulla traiettoria

Average pose entropy over time:

$$H(p(x_{1:t} | d)) \approx \frac{1}{t} \sum_{t'=1}^t H(p(x_{t'} | d))$$



# Guadagno di informazione con l'esecuzione delle azioni

- The reduction of entropy in the model

observations to be obtained

action

$$I(\hat{z}, a) = H(p(m, x | d)) - H(p(m, x, \hat{x} | d, a, \hat{z}))$$

H before action is carried out

H after action is carried out

new poses introduced by action

# Guadagno di informazione atteso

- To compute the information gain one needs to know the observations obtained when carrying out an action
- This quantity is not known! Reason about potential measurements

$$E[I(a)] = \int_{\hat{z}} p(\hat{z} | a, d) \cdot I(\hat{z}, a) d\hat{z}$$

# Sequenze di Misure

- The filter represents a posterior about possible maps
- Use these maps to reason about possible observation
- Simulate laser measurements in the maps of the particles

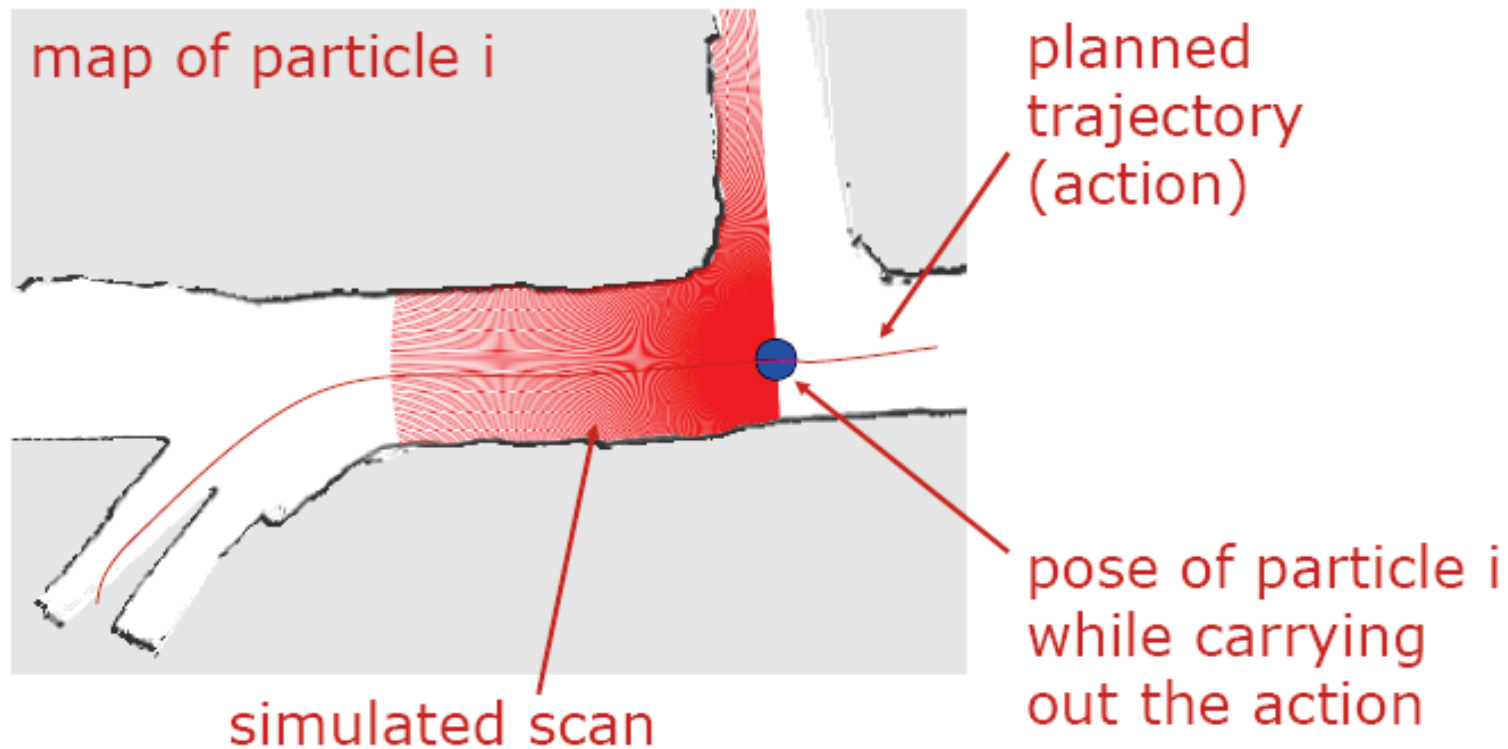
$$E[I(a)] = \int_{\hat{z}} p(\hat{z} | a, d) \cdot I(\hat{z}, a) d\hat{z}$$

measurement sequences  
simulated in the maps

likelihood  
(particle weight)

# Sequenze di Misura

- Ray-casting in the map of each particle to generate observation sequences



$$p(\hat{z} | a_t, d_t) \approx \sum_{i=1}^{\#particles} p(\hat{z} | a_t, m^{[i]}, x_{1:t}^{[i]}, d_t) \cdot \omega_t^{[i]} p(m^{[i]} | x_{1:t}^{[i]}, d_t)$$

# Utilità

- To take into account the cost of an action, we compute a utility

$$U(a) = I(a) - \alpha \cdot cost(a)$$

- Select the action with the highest expected utility

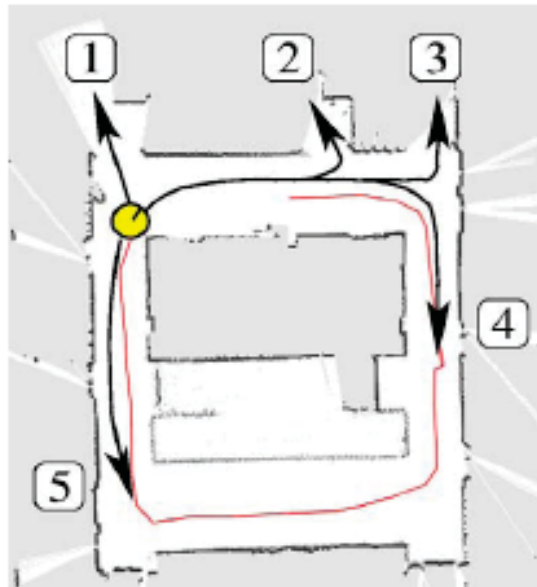
$$a^* = \operatorname{argmax}_a \{E[U(a)]\}$$



# Azioni specifiche

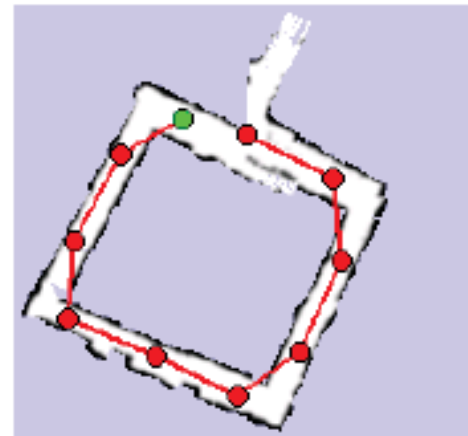
To efficiently sample actions we consider

- **exploratory actions (1-3)**
- **loop closing actions (4)** and
- **place revisiting actions (5)**

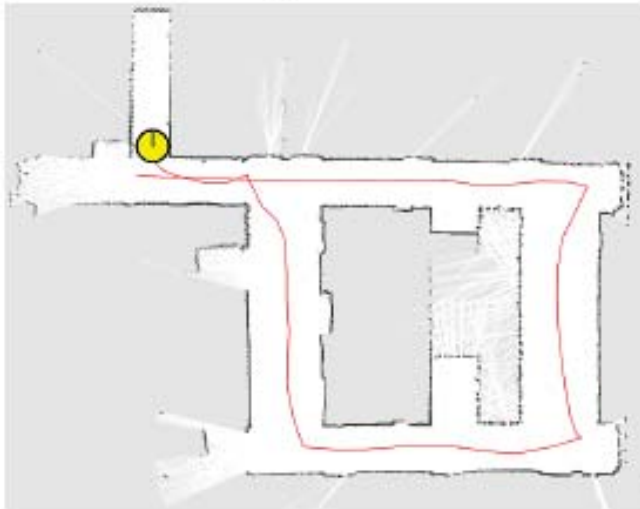
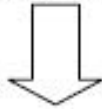
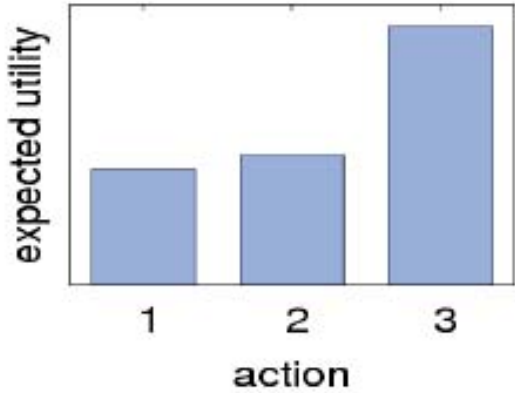
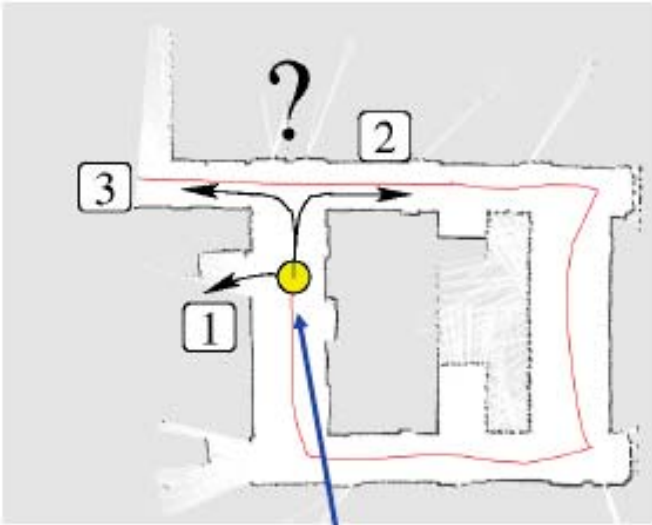


# Doppia Rappresentazione per la rilevazione di cicli

- **Trajectory graph** ("topological map") stores the **path traversed by the robot**
- **Occupancy grid** map represents the **space covered by the sensors**
- **Loops** correspond to **long paths in the trajectory graph** and **short paths in the grid map**

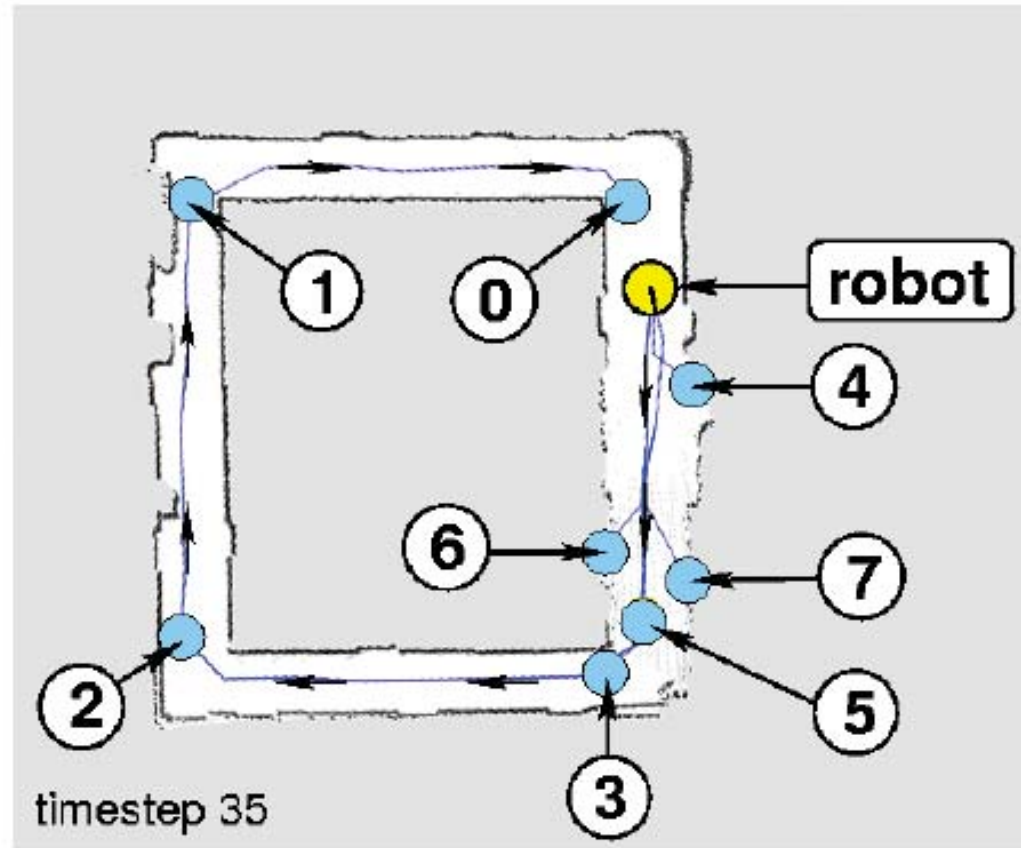
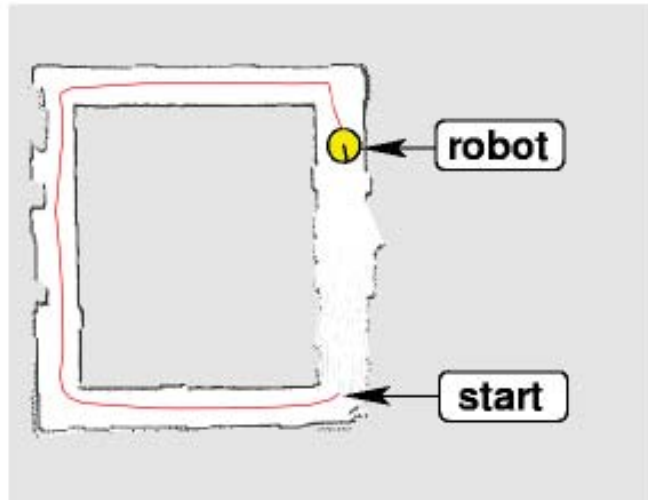


# Esempio

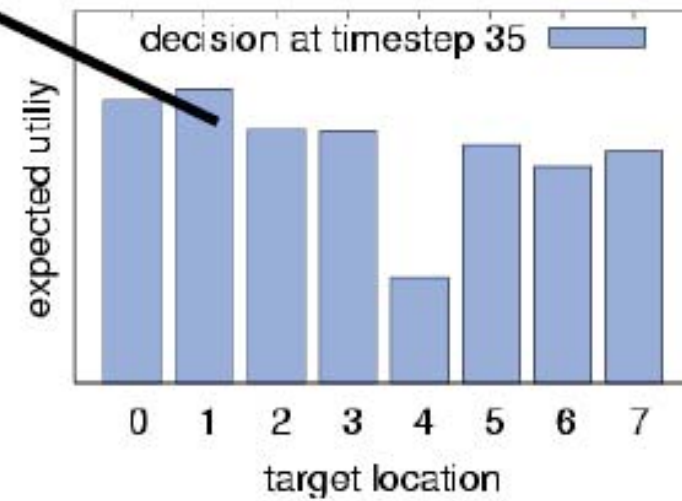
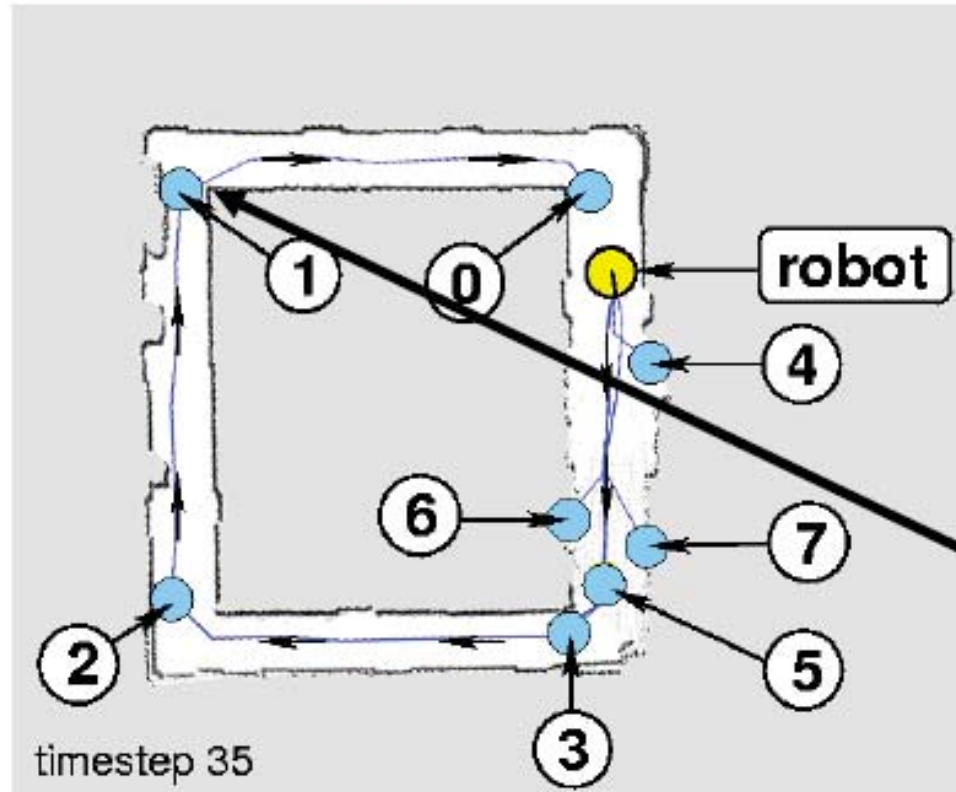


high pose uncertainty

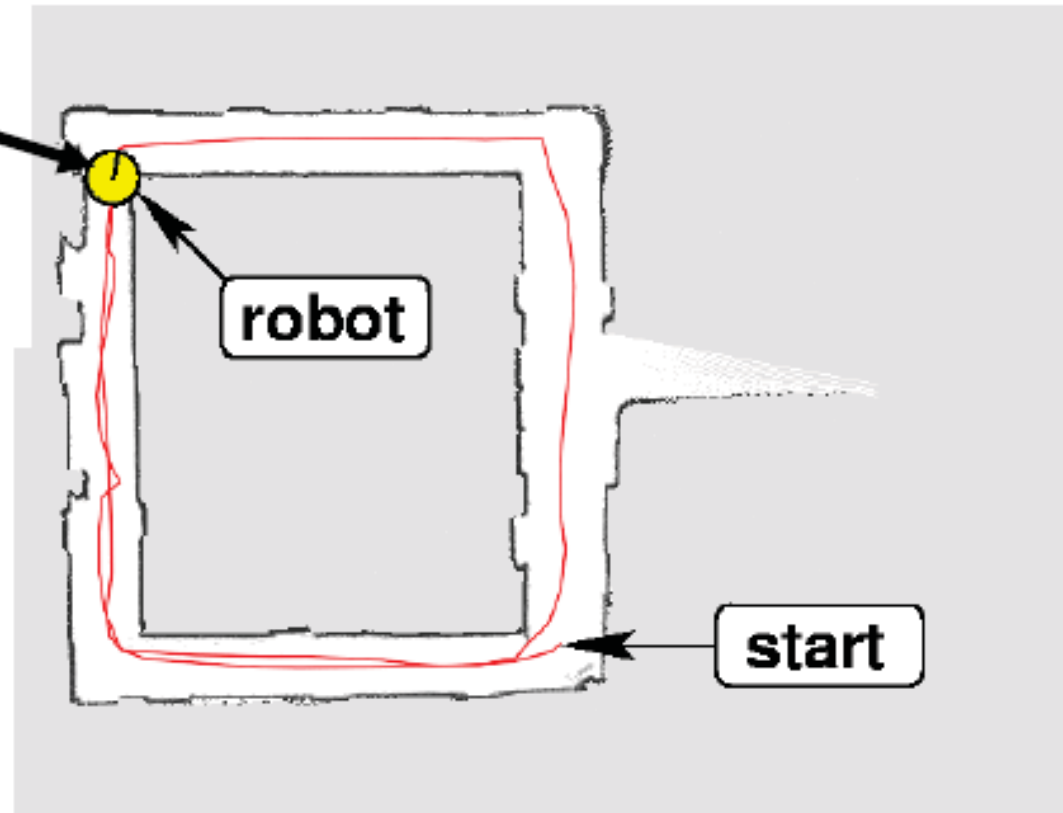
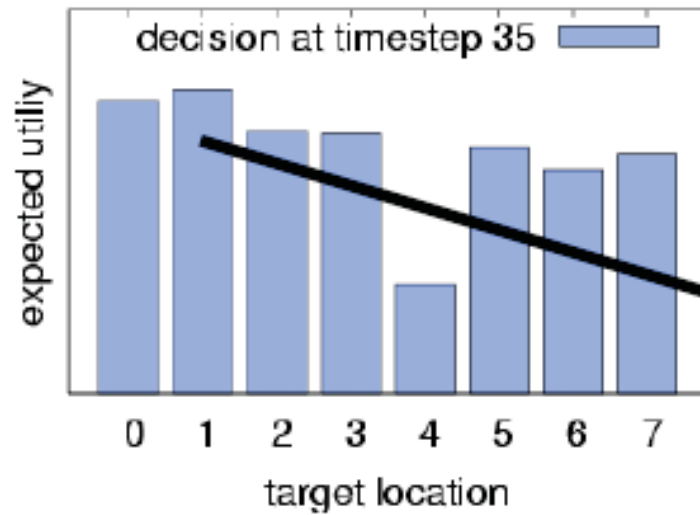
# Possibili Target



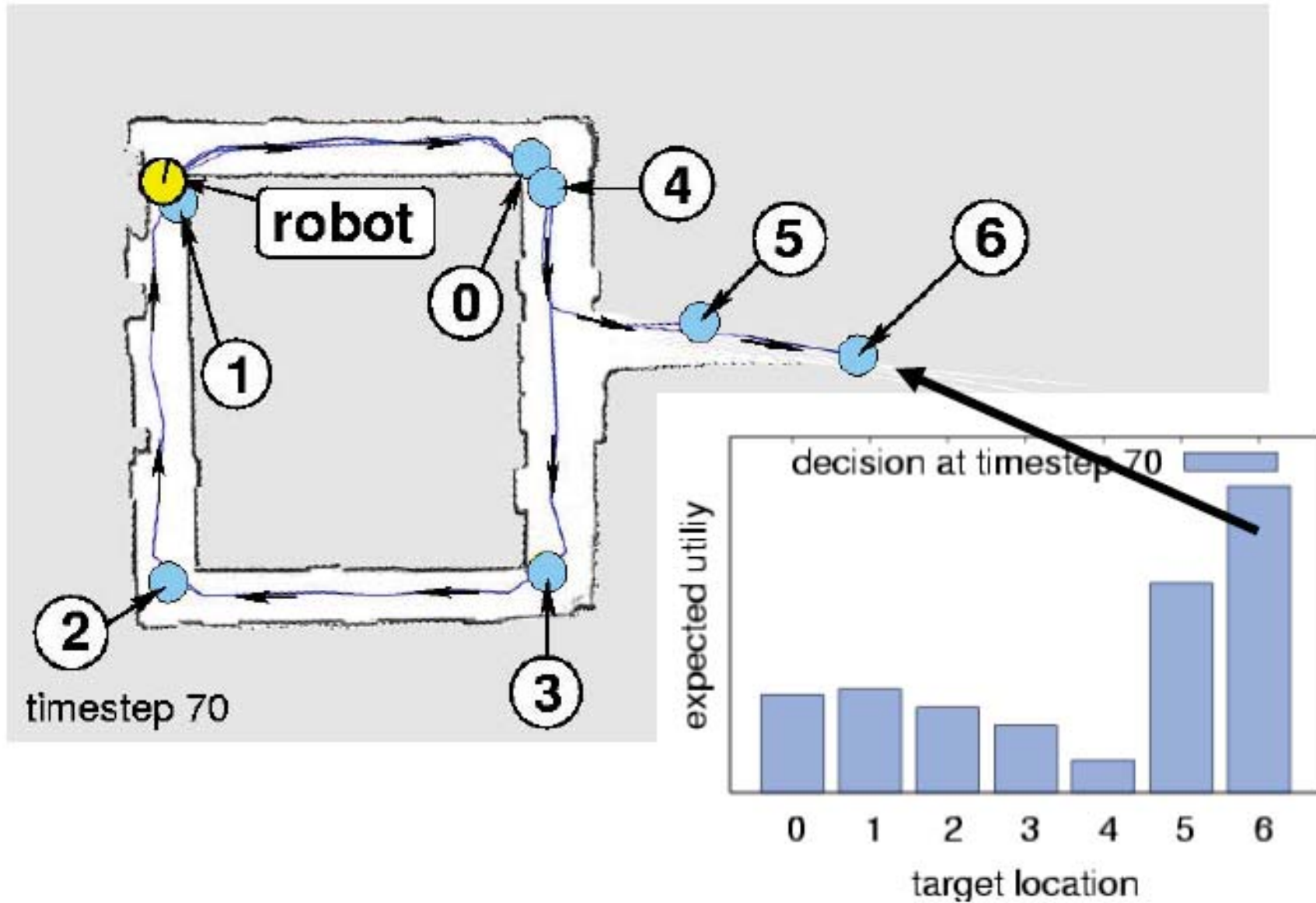
# Valutazione dei Target



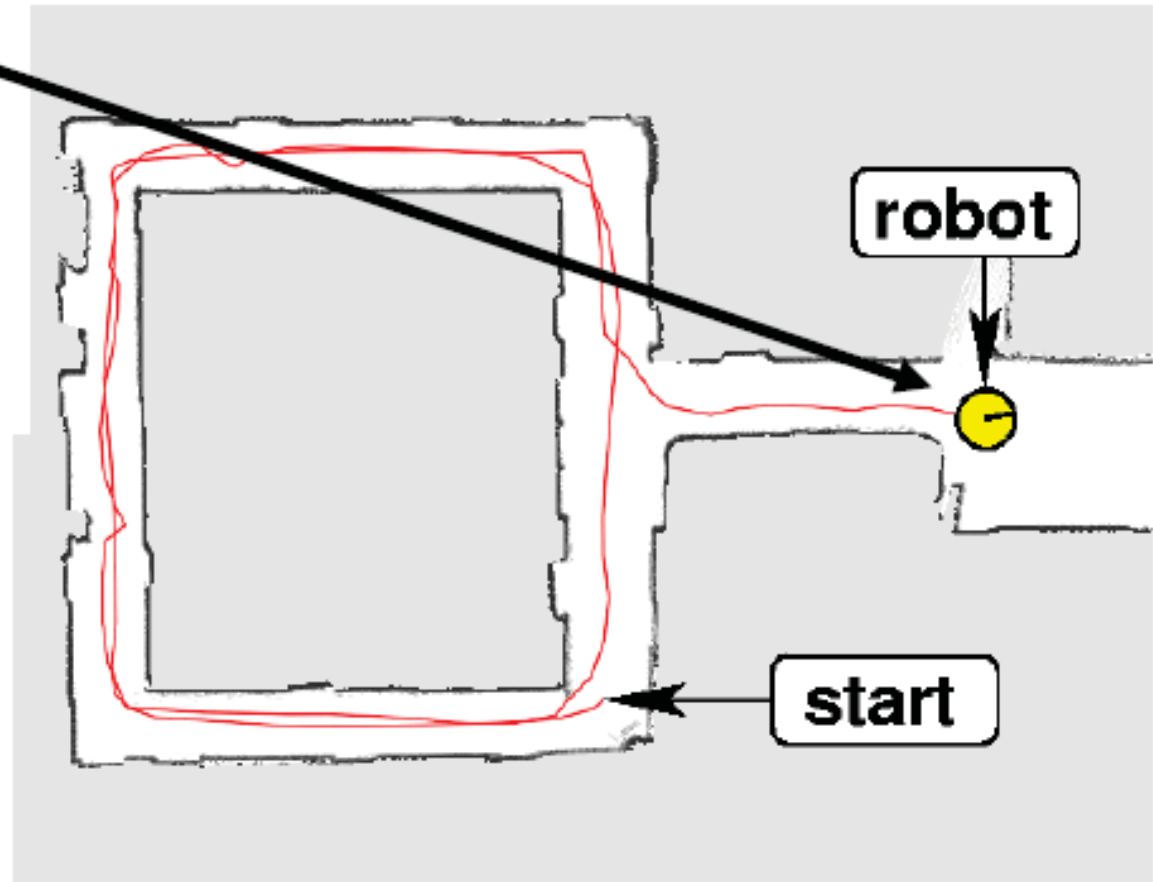
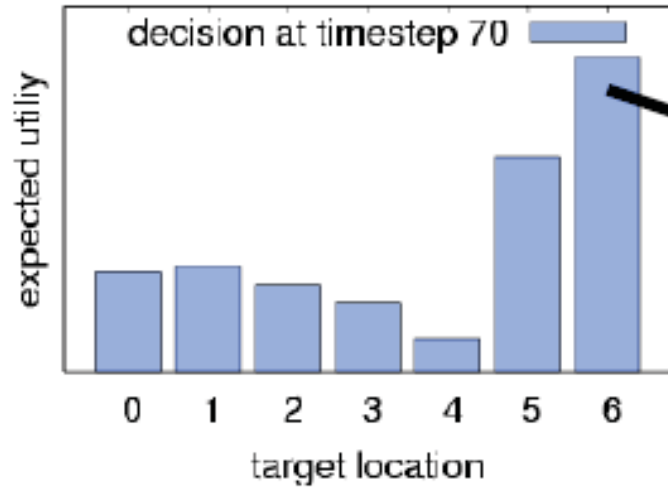
# Spostamento sul Target



# Valutazione dei Target

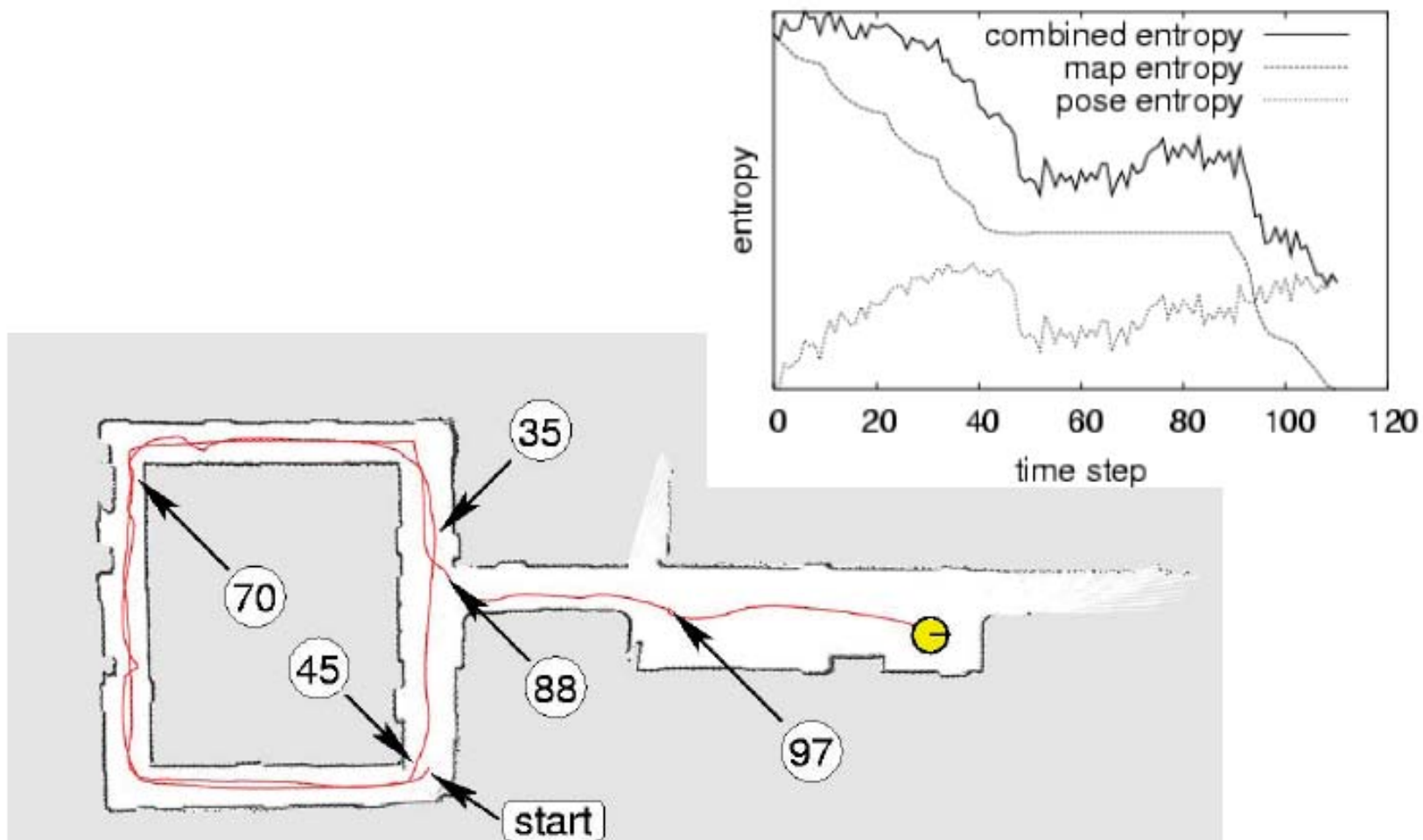


# Movimento Robot



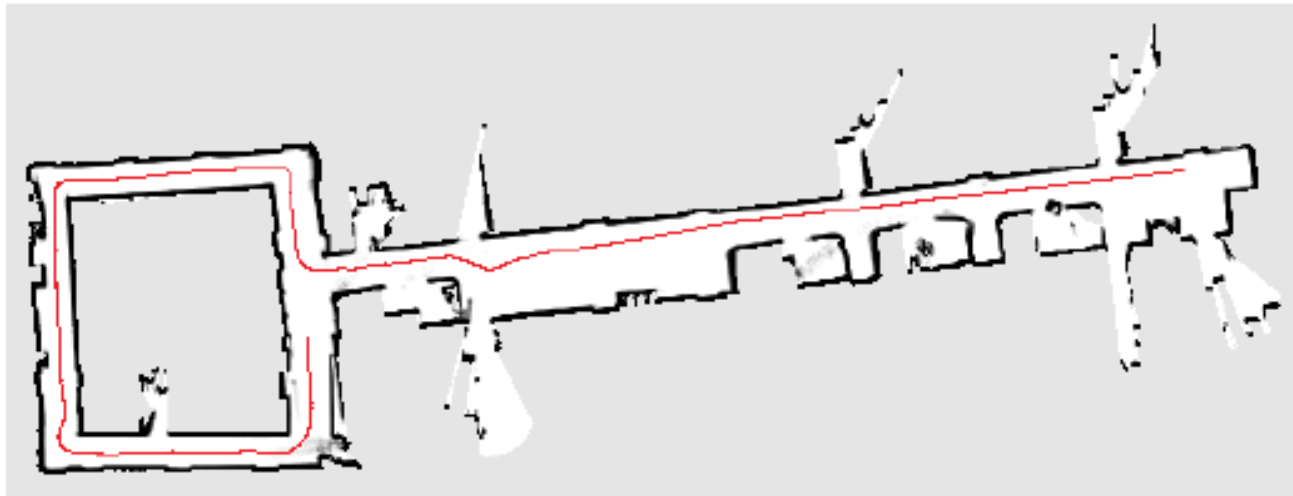


# Evoluzione dell'entropia

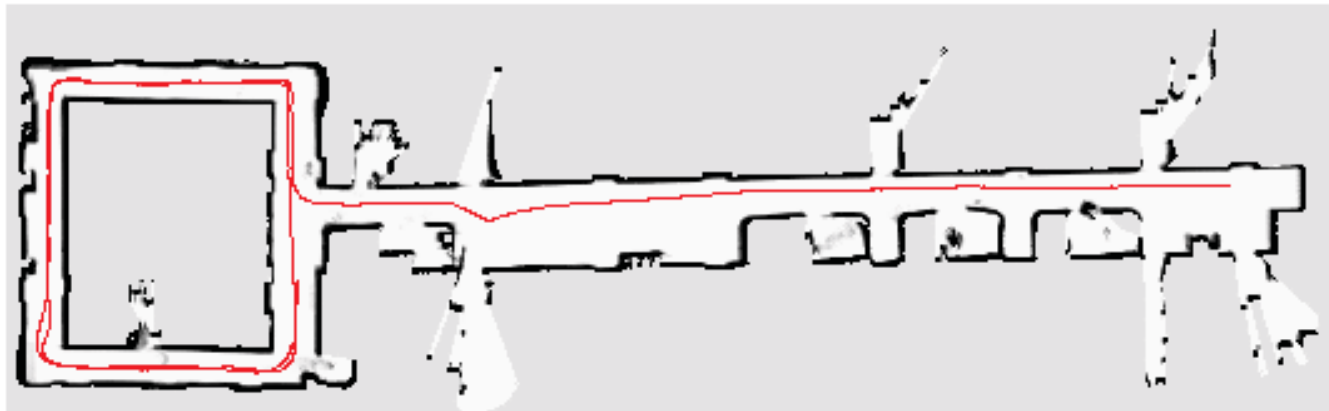


# Confronto

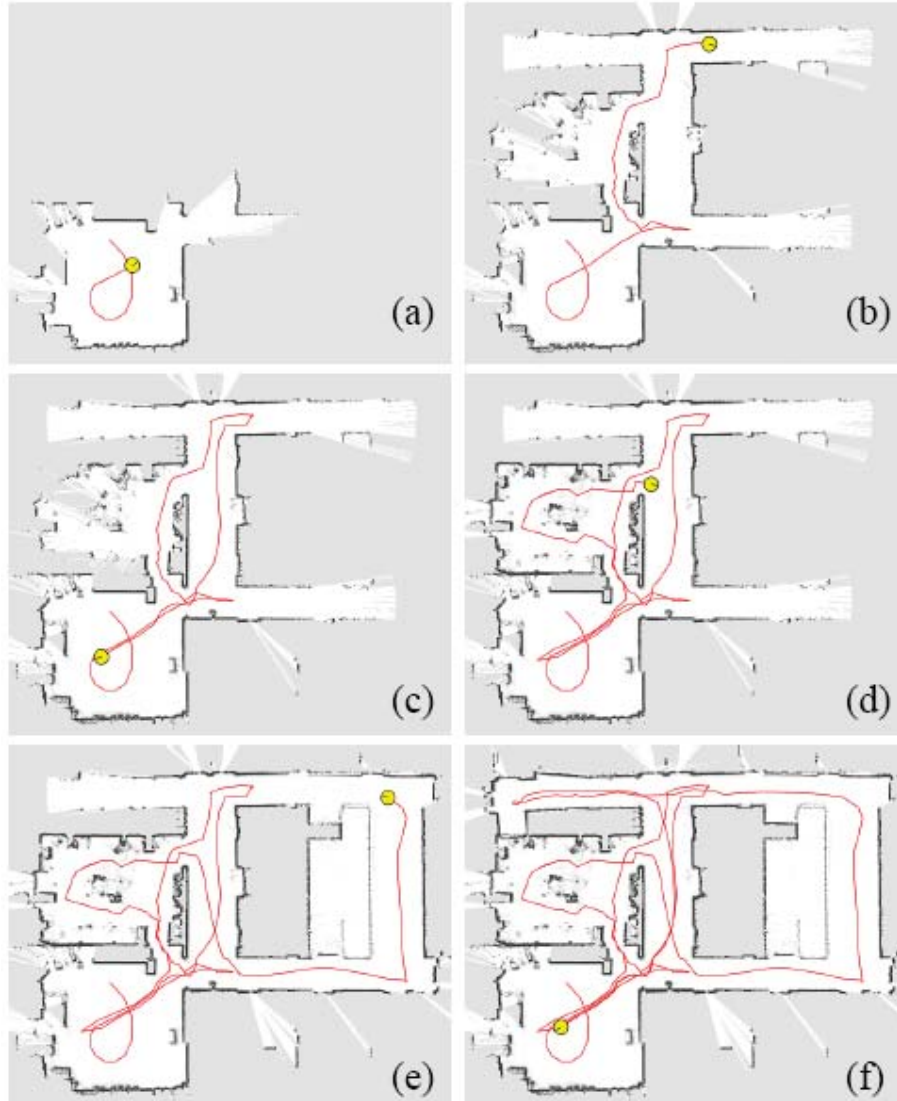
Map uncertainty only:



After loop closing action:

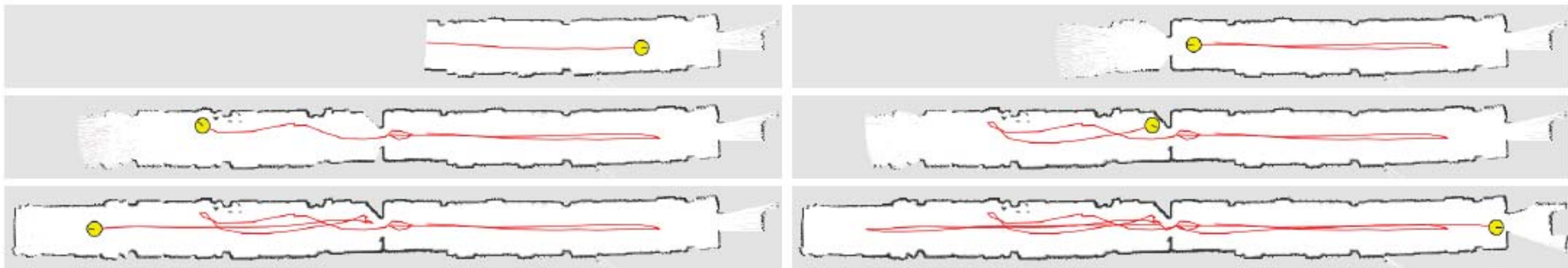


# Esplorazione



# Esplorazione Corridoio

Torna indietro per rilocalizzarsi



# Riassunto

- A decision-theoretic approach to exploration in the context of RBPF-SLAM
- The approach utilizes the factorization of the Rao-Blackwellization to efficiently calculate the expected information gain
- Reasons about measurements obtained along the path of the robot
- Considers a reduced action set consisting of exploration, loop-closing, and place-revisiting actions
- Experimental results demonstrate the usefulness of the overall approach