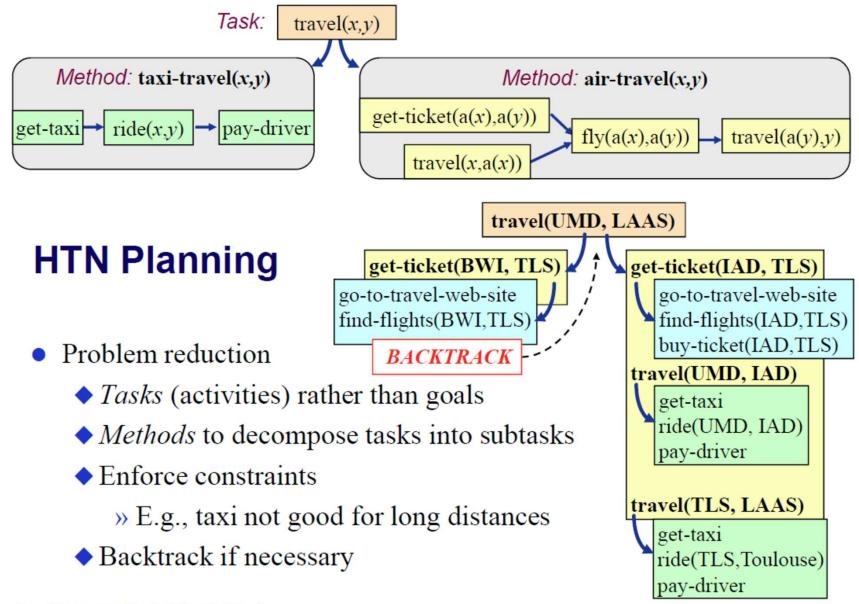
- Problem reduction
  - ◆ *Tasks* (activities) rather than goals
  - ◆ Methods to decompose tasks into subtasks
  - Enforce constraints
    - » E.g., taxi not good for long distances
  - Backtrack if necessary

Dana Nau: Lecture slides for Automated Planning

- More flexibility in modeling:
  - incorporate procedural expert knowledge (modeling means, speed up search)
- More complex behavior
  - pose complex restrictions on the desired solutions
- Easier user integration in the plan generation process
  - mixed initiative planning; MIP
- Communicate plans on different levels of abstraction
- Incorporate task abstraction in plan explanations

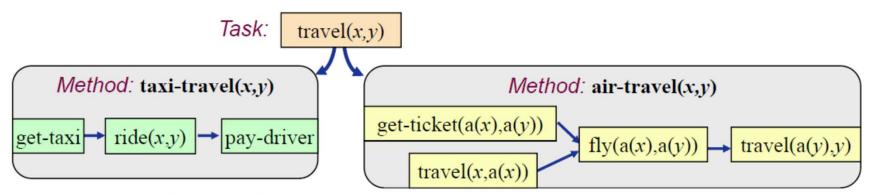


Dana Nau: Lecture slides for Automated Planning

- "HTN planners differ from classical planners in what they plan for and how they plan for it. In an HTN planner, the objective is not to achieve a set of goals but instead to perform some set of tasks." (Ghallab, Nau, and Traverso; Automated Planning: Theory and Practice)
- Main differences to classical planning problems:
  - The goal is to find a refinement of the initial task(s), not to satisfy some goal description
  - No arbitrary task insertion: decompose compound tasks using their pre-defined methods

- HTN planners may be domain-specific
- Or they may be domain-configurable
  - Domain-independent planning engine
  - Domain description that defines not only the operators, but also the methods
  - Problem description

» domain description, initial state, initial task network

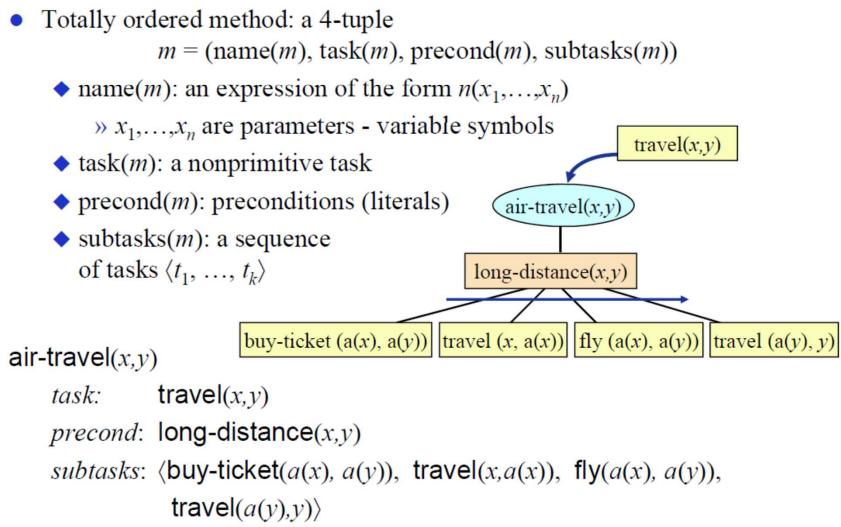


Dana Nau: Lecture slides for Automated Planning

### Simple Task Network (STN) Planning

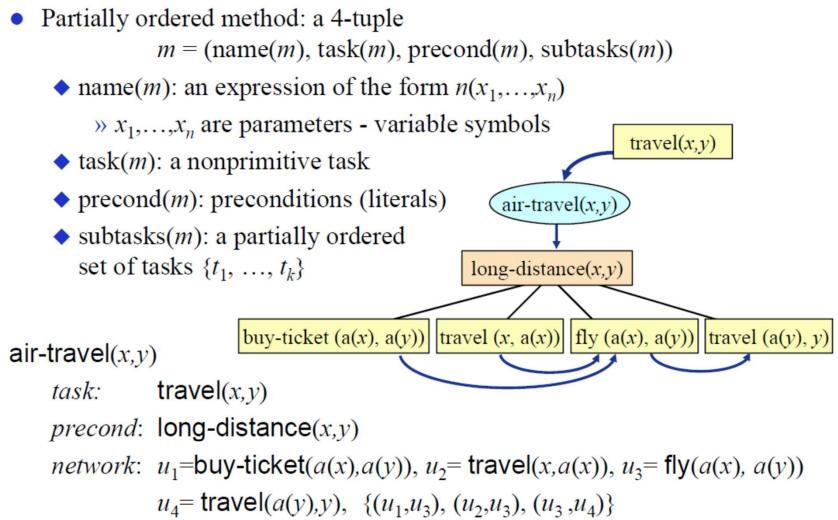
- A special case of HTN planning
- States and operators
  - ◆ The same as in classical planning
- *Task*: an expression of the form  $t(u_1, \ldots, u_n)$ 
  - $\diamond$  *t* is a *task symbol*, and each  $u_i$  is a term
  - Two kinds of task symbols (and tasks):
    - » primitive: tasks that we know how to execute directly
      - task symbol is an operator name
    - » nonprimitive: tasks that must be decomposed into subtasks
      - use *methods* (next slide)

### Methods



Dana Nau: Lecture slides for Automated Planning

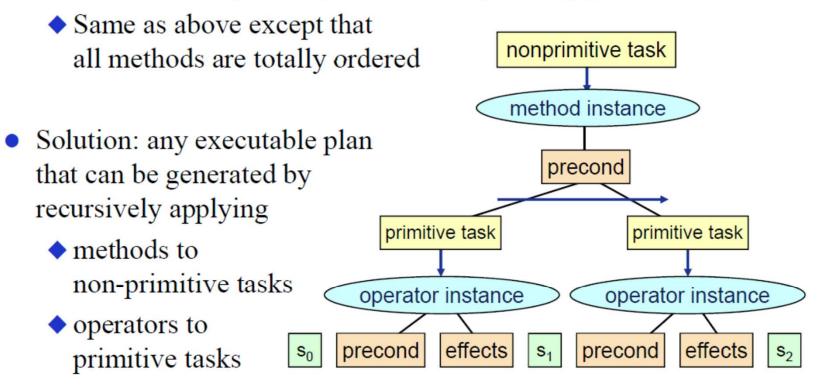
## **Methods (Continued)**



Dana Nau: Lecture slides for Automated Planning

### **Domains, Problems, Solutions**

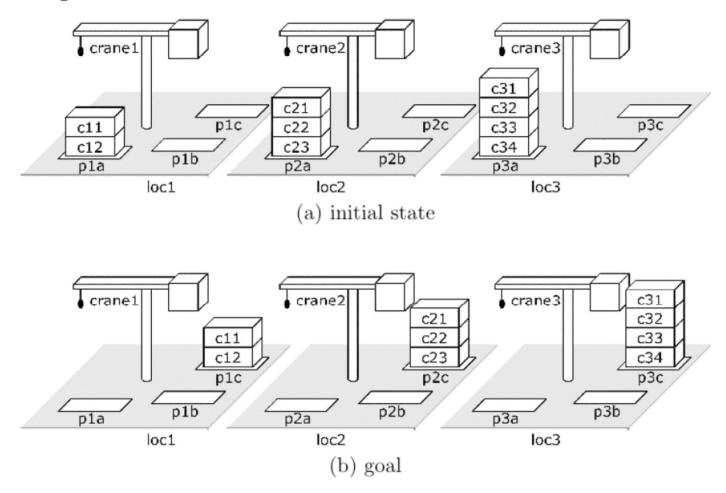
- STN planning domain: methods, operators
- STN planning problem: methods, operators, initial state, task list
- Total-order STN planning domain and planning problem:



Dana Nau: Lecture slides for Automated Planning

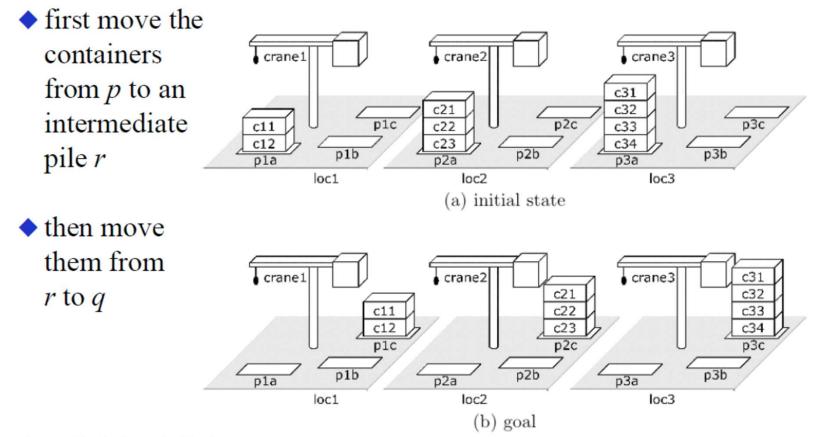
### Example

• Suppose we want to move three stacks of containers in a way that preserves the order of the containers



### **Example (continued)**

• A way to move each stack:



Dana Nau: Lecture slides for Automated Planning

```
using crane k at location l, take container c from object x1 (container or
                                                   pallet) in pile p1 and put it onto object x2 in pile p2
take-and-put(c, k, l_1, l_2, p_1, p_2, x_1, x_2):
   task:
              move-topmost-container(p_1, p_2)
                                                                    Total-Order
   precond: top(c, p_1), on(c, x_1), ; true if p_1 is not empty
                                                                   Formulation
              attached(p_1, l_1), belong(k, l_1), ; bind l_1 and k
              attached(p_2, l_2), top(x_2, p_2); bind l_2 and x_2
   subtasks: (take(k, l_1, c, x_1, p_1), put(k, l_2, c, x_2, p_2))
recursive-move(p, q, c, x):
                                                                                 crane:
   task:
              move-stack(p,q)
   precond: top(c, p), on(c, x); true if p is not empty
   subtasks: (move-topmost-container(p,q), move-stack(p,q))
                                                                                                 p1c
                                                                                ¢11
              ;; the second subtask recursively moves the rest of the stack
                                                                                c12
                                                                                            p1b
                                                                                 p1a
do-nothing(p,q)
                                                                                         loc1
   task:
              move-stack(p,q)
   precond: top(pallet, p); true if p is empty
   subtasks: () ; no subtasks, because we are done
                                                                                 crane:
move-each-twice()
   task:
              move-all-stacks()
                                                                                                  c11
   precond:
                ; no preconditions
                                                                                                 c12
                                                                                                  p1c
   subtasks:
                : move each stack twice:
              (move-stack(p1a,p1b), move-stack(p1b,p1c),
                                                                                            p1b
                                                                                 p1a
               move-stack(p2a,p2b), move-stack(p2b,p2c),
                                                                                         loc1
               move-stack(p3a, p3b), move-stack(p3b, p3c)
```

```
take-and-put(c, k, l_1, l_2, p_1, p_2, x_1, x_2):
   task:
              move-topmost-container(p_1, p_2)
                                                                  Partial-Order
   precond: top(c, p_1), on(c, x_1), ; true if p_1 is not empty
                                                                  Formulation
              attached(p_1, l_1), belong(k, l_1), ; bind l_1 and k
              \mathsf{attached}(p_2, l_2), \mathsf{top}(x_2, p_2); bind l_2 and x_2
   subtasks: (take(k, l_1, c, x_1, p_1), put(k, l_2, c, x_2, p_2))
recursive-move(p, q, c, x):
                                                                                crane1
              move-stack(p,q)
   task:
   precond: top(c, p), on(c, x); true if p is not empty
   subtasks: (move-topmost-container(p,q), move-stack(p,q))
                                                                                                p1c
                                                                               c11
              ;; the second subtask recursively moves the rest of the stack
                                                                               c12
                                                                                           p1b
                                                                                p1a
do-nothing(p,q)
                                                                                        loc1
              move-stack(p, q)
   task:
   precond: top(pallet, p); true if p is empty
   subtasks: () ; no subtasks, because we are done
                                                                                crane1
move-each-twice()
   task:
              move-all-stacks()
                                                                                                c11
   precond:
                ; no preconditions
                                                                                                c12
                                                                                                p1c
   network:
                ; move each stack twice:
              u_1 = move-stack(p1a,p1b), u_2 = move-stack(p1b,p1c),
                                                                                           p1b
                                                                                p1a
              u_3 = move-stack(p2a,p2b), u_4 = move-stack(p2b,p2c),
                                                                                        loc1
              u_5 = move-stack(p3a,p3b), u_6 = move-stack(p3b,p3c),
              \{(u_1, u_2), (u_3, u_4), (u_5, u_6)\}
                                                                                                   33
```

## **Solving Total-Order STN Planning Problems**

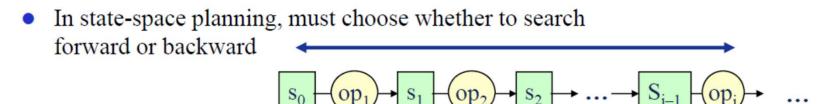
Total-order Forward Decomposition (TFD)  $\mathsf{TFD}(s, \langle t_1, \ldots, t_k \rangle, O, M)$ if k = 0 then return () (i.e., the empty plan) if  $t_1$  is primitive then active  $\leftarrow \{(a, \sigma) \mid a \text{ is a ground instance of an operator in } O,$  $\sigma$  is a substitution such that *a* is relevant for  $\sigma(t_1)$ , and *a* is applicable to sif *active* =  $\emptyset$  then return failure state s; task list  $T=(|\mathbf{t_1}|, \mathbf{t_2}, ...)$ nondeterministically choose any  $(a, \sigma) \in active$  $\pi \leftarrow \mathsf{TFD}(\gamma(s, a), \sigma(\langle t_2, \ldots, t_k \rangle), O, M)$ action a if  $\pi$  = failure then return failure state  $\gamma(s,a)$ ; task list T=(t<sub>2</sub>,...) else return  $a, \pi$ else if  $t_1$  is nonprimitive then active  $\leftarrow \{m \mid m \text{ is a ground instance of a method in } M,$  $\sigma$  is a substitution such that m is relevant for  $\sigma(t_1)$ . and *m* is applicable to stask list T= $(\mathbf{t_1}, \mathbf{t_2}, \dots)$ if *active* =  $\emptyset$  then return failure method instance mnondeterministically choose any  $(m, \sigma) \in active$  $w \leftarrow \text{subtasks}(m), \sigma(\langle t_2, \ldots, t_k \rangle)$ task list T=( $[\mathbf{u}_1,\ldots,\mathbf{u}_k], t_2,\ldots$ ) return TFD(s, w, O, M)

Dana Nau: Lecture slides for Automated Planning

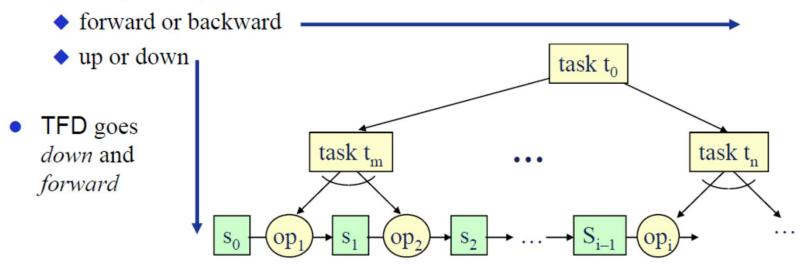
# **Applicability and Relevance**

- A method instance m is <u>applicable</u> in a state s if – precond(m) satisfied in s
- A method instance m is <u>relevant</u> for a task t if
   there is a substitution σ such that σ(t) = task(m).
- The decomposition of a task t by a relevant method m under  $\sigma$  is
  - $-\delta(t,m,\sigma) = \sigma(network(m))$  or
  - $-\delta(t,m,\sigma) = \sigma(\langle subtasks(m) \rangle)$  if m is totally ordered.

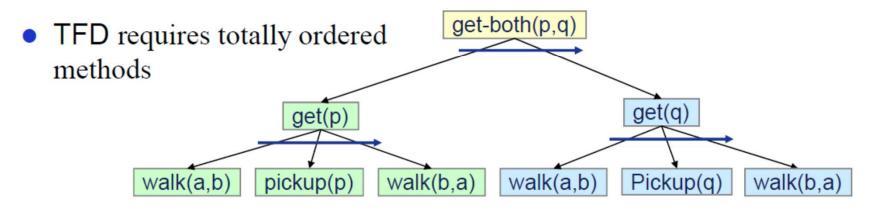
### Comparison to Forward and Backward Search



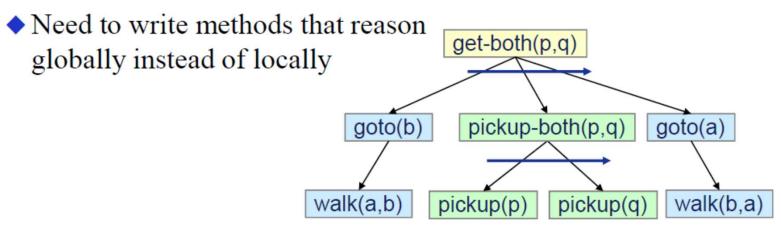
• In HTN planning, there are *two* choices to make about direction:



### **Limitation of Ordered-Task Planning**



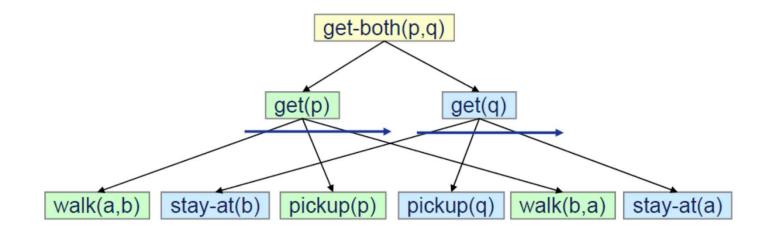
- Can't interleave subtasks of different tasks
- Sometimes this makes things awkward



Dana Nau: Lecture slides for Automated Planning

### **Partially Ordered Methods**

• With partially ordered methods, the subtasks can be interleaved



- Fits many planning domains better
- Requires a more complicated planning algorithm

### PFD(s, w, O, M) if $w = \emptyset$ then return the empty plan nondeterministically choose any $u \in w$ that has no predecessors in w if $t_u$ is a primitive task then $active \leftarrow \{(a, \sigma) \mid a \text{ is a ground instance of an operator in } O, \\ \sigma \text{ is a substitution such that name}(a) = \sigma(t_u), \\ and a \text{ is applicable to } s\}$

if *active* =  $\emptyset$  then return failure nondeterministically choose any  $(a, \sigma) \in active$  $\pi \leftarrow PFD(\gamma(s, a), \sigma(w - \{u\}), O, M)$ if  $\pi$  = failure then return failure

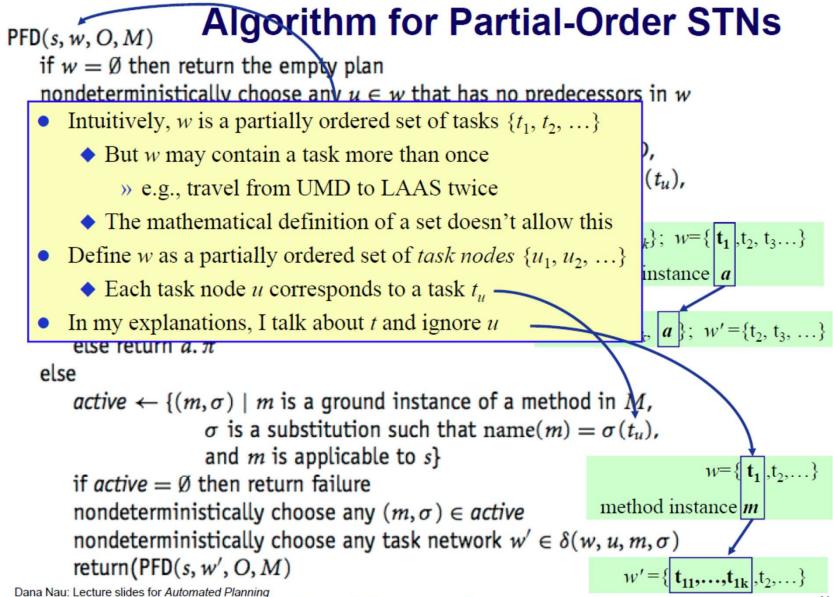
```
\pi = \{a_1, \dots, a_k\}; \ w = \{ \mathbf{t}_1, \mathbf{t}_2, \mathbf{t}_3 \dots \}
operator instance a
\pi = \{a_1, \dots, a_k, \mathbf{a}\}; \ w' = \{\mathbf{t}_2, \mathbf{t}_3, \dots \}
```

else

```
active \leftarrow \{(m, \sigma) \mid m \text{ is a ground instance of a method in } M, \\ \sigma \text{ is a substitution such that name}(m) = \sigma(t_u), \\ and m \text{ is applicable to } s \} \\ \text{if active} = \emptyset \text{ then return failure} \\ \text{nondeterministically choose any } (m, \sigma) \in active \\ \text{nondeterministically choose any task network } w' \in \delta(w, u, m, \sigma) \\ \text{return}(\text{PFD}(s, w', O, M)) \\ w' = \{t_{11}, \dots, t_{1k}, t_2, \dots\}
```

Dana Nau: Lecture slides for Automated Planning

else return  $a, \pi$ 



## **Algorithm for Partial-Order STNs**

```
PFD(s, w, O, M)

if w = \emptyset then return the empty plan

nondeterministically choose any u \in

if t_u is a primitive task then
```

```
nondeterministically choose any u \in w that has no predecessors in w

if t_u is a primitive task then

active \leftarrow \{(a, \sigma) \mid a \text{ is a ground instance of an operator in } O,

\sigma is a substitution such that name(a) = \sigma(t_u),

and a is applicable to s}

if active = \emptyset then return failure

nondeterministically choose any (a, \sigma) \in active

\pi = \{a_1, \dots, a_k\}; w = \{\mathbf{t}_1, \mathbf{t}_2, \mathbf{t}_3 \dots\}
```

```
\pi \leftarrow \mathsf{PFD}(\gamma(s, a), \sigma(w - \{u\}), O, M)
```

```
if \pi = failure then return failure
```

```
else return a. \pi
```

```
\pi = \{a_1, \dots, a_k\}; \ w = \{ \mathbf{t}_1, \mathbf{t}_2, \mathbf{t}_3 \dots \}
operator instance a
\pi = \{a_1, \dots, a_k, \mathbf{a}\}; \ w' = \{\mathbf{t}_2, \mathbf{t}_3, \dots \}
```

#### else

```
active \leftarrow \{(m,\sigma) \mid m \text{ is a ground instance of a method in } M, \\ \sigma \text{ is a substitution such that } name(m) = \sigma(t_u), \\ and m \text{ is applicable to } s \} \\ \text{if } active = \emptyset \text{ then return failure} \\ nondeterministically choose any } (m,\sigma) \in active \\ nondeterministically choose any task network <math>w' \in \delta(w, u, m, \sigma) 
 return(PFD(s, w', O, M) \\ w' = \{t_{11}, \dots, t_{1k}, t_{2}, \dots\}
```

Dana Nau: Lecture slides for Automated Planning

## **Algorithm for Partial-Order STNs**

PFD(s, w, O, M)if  $w = \emptyset$  then return the empty plan nondeterministically choose any  $u \in w$  that has no predecessors in w if  $t_{\mu}$  is a primitive task then active  $\leftarrow \delta(w, u, m, \sigma)$  has a complicated definition in the book. Here's what it means: • We nondeterministically selected  $t_1$  as the task to do first if active • Must do  $t_1$ 's first subtask before the first subtask of every  $t_i \neq t_1$ nondeter • Insert ordering constraints to ensure that this happens  $\pi \leftarrow \text{PFI}$ if  $\pi =$  failure then return failure  $\pi = \{a_1, \ldots, a_k, |a|\}; w' = \{t_2, t_3, \ldots\}$ else return  $a.\pi$ else active  $\leftarrow \{(m, \sigma) \mid m \text{ is a ground instance of a method in } M,$  $\sigma$  is a substitution such that name  $m = \sigma(t_u)$ , and *m* is applicable to *s*}  $w = \{ t_1, t_2, \dots \}$ if *active* =  $\emptyset$  then return failure method instance mnondeterministically choose any  $(m, \sigma) \in active$ nondeterministically choose any task network  $w' \in \delta(w, u, m, \sigma)$ return(PFD(s, w', O, M)

Dana Nau: Lecture slides for Automated Planning

## **Comparison to Classical Planning**

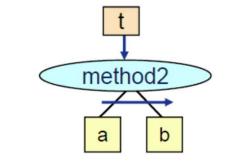
STN planning is strictly more expressive than classical planning

- Any classical planning problem can be translated into an orderedtask-planning problem in polynomial time
- Several ways to do this. One is roughly as follows:
  - For each goal or precondition e, create a task  $t_e$
  - For each operator o and effect e, create a method  $m_{o,e}$ 
    - » Task:  $t_e$
    - » Subtasks:  $t_{c1}$ ,  $t_{c2}$ , ...,  $t_{cn}$ , o, where  $c_1$ ,  $c_2$ , ...,  $c_n$  are the preconditions of o
    - » Partial-ordering constraints: each  $t_{ci}$  precedes o
- (I left out some details, such as how to handle deleted-condition interactions)

Dana Nau: Lecture slides for Automated Planning

## **Comparison to Classical Planning (cont.)**

- Some STN planning problems aren't expressible in classical planning
- Example:
  - Two STN methods:
    - » No arguments
    - » No preconditions
- a t b



- Two operators, a and b
  - » Again, no arguments and no preconditions
- Initial state is empty, initial task is t
- Set of solutions is  $\{a^nb^n \mid n \ge 0\}$
- No classical planning problem has this set of solutions
  - » The state-transition system is a finite-state automaton
  - » No finite-state automaton can recognize  $\{a^nb^n \mid n \ge 0\}$
- Can even express undecidable problems using STNs

## SHOP2

- SHOP2: implementation of PFD-like algorithm + generalizations
  - Won one of the top four awards in the AIPS-2002 Planning Competition
  - Freeware, open source
  - Implementation available at
    - http://www.cs.umd.edu/projects/shop

- HTN planning is even more general
  - Can have constraints associated with tasks and methods
    - » Things that must be true before, during, or afterwards
  - Some algorithms use causal links and threats like those in PSP

- Hierarchical Task Networks generalise Simple Task Networks:
  - no forward decomposition is necessary, a task network w consists of a set of task nodes and a set of constraints
- (HTN Planning Problem) An HTN planning problem is a 3-tuple  $P = (s_0, w_0, D)$  where  $s_0$  is the initial state,  $w_0$  is a task network called the initial task network, and D is the HTN planning domain which consists of a set of operators and methods.
- A plan  $\pi = [a_1, ..., a_k]$  is a solution for a planning problem if there is a ground instance  $(U_0, C_0)$  of (U, C) and a total ordering  $[u_1, ..., u_k]$  of the nodes of U0 such that
  - the plan  $\pi$  is executable in  $s_o$  and the total ordering fulfills all constraints.

- Hierarchical Task Networks generalise Simple Task Networks:
  - no forward decomposition is necessary, a task network w consists of a set of task nodes and a set of constraints
- A (hierarchical) task network is a pair w=(U,C), where:
- U is a set of tasks and
- C is a set of constraints of the following types:
  - t1<t2: precedence constraint between tasks satisfied if in every solution  $\pi$ : last({t}, $\pi$ ) < first({t}, $\pi$ );
  - before(U',I): satisfied if in every solution  $\pi$ : literal I holds in the state just before first(U', $\pi$ );
  - after(U',I): satisfied if in every solution  $\pi$ : literal I holds in the state just after last(U', $\pi$ );
  - between(U',U'',I): satisfied if in every solution  $\pi$ : literal I holds in every state after last(U', $\pi$ ) and before first(U'', $\pi$ ).

```
<u>first(U',π)</u> = the action a_i \in A(U') that occurs first in π;
and
<u>last(U',π)</u> = the action a_i \in A(U') that occurs last in π.
```

- Hierarchical Task Networks generalise Simple Task Networks:
  - no forward decomposition is necessary, a task network w consists of a set of task nodes and a set of constraints
- Let MS be a set of method symbols. An HTN method is a 4tuple m=(name(m),task(m),subtasks(m),constr(m)) where:
  - name(m): the name of the method
    - syntactic expression of the form n(x1,...,xk)
    - n∈MS: method symbol
    - x1,...,xk: variable symbols that occur in m;
  - task(m): a non-primitive task;
  - (subtasks(m),constr(m)): a task network.

take-and-put( $c,k,l,p_o,p_d,x_o,x_d$ )

- task: move-topmost(p<sub>o</sub>,p<sub>d</sub>)
- network:
  - subtasks: {t<sub>1</sub>=take(k,l,c,x<sub>o</sub>,p<sub>o</sub>), t<sub>2</sub>=put(k,l,c,x<sub>d</sub>,p<sub>d</sub>)}
  - constraints: { $t_1 \prec t_2$ , before({ $t_1$ }, top( $c, p_o$ )), before({ $t_1$ }, on( $c, x_o$ )), before({ $t_1$ }, attached( $p_o, l$ )), before({ $t_1$ }, belong(k, l)), before({ $t_2$ }, attached( $p_d, l$ )), before({ $t_2$ }, top( $x_d, p_d$ ))}

recursive-move $(p_o, p_d, c, x_o)$ 

- task: move-stack(p<sub>o</sub>,p<sub>d</sub>)
- network:
  - subtasks: {t<sub>1</sub>=move-topmost(p<sub>o</sub>,p<sub>d</sub>), t<sub>2</sub>=move-stack(p<sub>o</sub>,p<sub>d</sub>)}
  - constraints: { $t_1 \prec t_2$ , before({ $t_1$ }, top( $c, p_o$ )), before({ $t_1$ }, on( $c, x_o$ ))}

 $move-one(p_o, p_d, c)$ 

- task: move-stack(p<sub>o</sub>,p<sub>d</sub>)
- network:
  - subtasks: {t<sub>1</sub>=move-topmost(p<sub>o</sub>,p<sub>d</sub>)}
  - constraints: {before({t<sub>1</sub>}, top(c,p<sub>o</sub>)), before({t<sub>1</sub>}, on(c,pallet))}

Let (U,C) be a primitive HTN. A plan  $\pi = \langle a_1, ..., a_n \rangle$  is a solution for  $\mathcal{P}=(s_i, (U,C), O, M)$  if there is a ground instance  $(\sigma(U), \sigma(C))$  of (U,C) and a total ordering  $\langle t_1, ..., t_n \rangle$  of tasks in  $\sigma(U)$  such that:

- for *i*=1...*n*: name(*a<sub>i</sub>*) = *t<sub>i</sub>*;
- *π* is executable in s<sub>i</sub>, i.e. γ(s<sub>i</sub>, π) is defined;
- the ordering of (t<sub>1</sub>,...,t<sub>n</sub>) respects the ordering constraints in σ(C);
- for every constraint before(U',I) in σ(C) where t<sub>k</sub>=first(U',π): I
  must hold in γ(s<sub>i</sub>, (a<sub>1</sub>,...,a<sub>k-1</sub>));
- for every constraint after(U',I) in σ(C) where t<sub>k</sub>=last(U',π): I must hold in γ(s<sub>i</sub>, (a<sub>1</sub>,...,a<sub>k</sub>));
- for every constraint between(U',U",I) in σ(C) where t<sub>k</sub>=first(U',π) and t<sub>m</sub>=last(U",π): I must hold in every state γ(s<sub>i</sub>, ⟨a<sub>1</sub>,...,a<sub>j</sub>⟩), j∈{k...m-1}.

Let w = (U,C) be a non-primitive HTN. A plan  $\pi = \langle a_1, ..., a_n \rangle$  is a solution for  $\mathcal{P}=(s_i, w, O, M)$  if there is a sequence of task decompositions that can be applied to *w* such that:

- the result of the decompositions is a primitive HTN w'; and
- $\pi$  is a solution for  $\mathcal{P}'=(s_i, w', O, M)$ .

function Abstract-HTN(s,U,C,O,M)
if (U,C).isInconsistent() then return failure
if U.isPrimitive() then
 return extractSolution(s,U,C,O)
else
 return decomposeTask(s,U,C,O,M)

function extractSolution(*s*,*U*,*C*,*O*)  $\langle t_1,...,t_n \rangle \leftarrow U.chooseSequence($ *C*)  $\langle a_1,...,a_n \rangle \leftarrow$   $\langle t_1,...,t_n \rangle.chooseGrounding($ *s*,*C*,*O*)if  $\langle a_1,...,a_n \rangle.satisfies($ *C*) then return  $\langle a_1,...,a_n \rangle$ return failure

function decomposeTask(s, U, C, O, M)  $t \leftarrow U$ .nonPrimitives().selectOne()  $methods \leftarrow \{(m, \sigma) \mid m \in M \text{ and } \sigma(task(m)) = \sigma(t)\}$ if methods.isEmpty() then return failure  $(m, \sigma) \leftarrow methods.chooseOne()$   $(U', C') \leftarrow \delta((U, C), t, m, \sigma)$   $(U', C') \leftarrow (U', C').applyCritic()$ return Abstract-HTN(s, U', C', O, M)

## Domain-Configurable Planners Compared to Classical Planners

- Disadvantage: writing a knowledge base can be more complicated than just writing classical operators
- Advantage: can encode "recipes" as collections of methods and operators
  - Express things that can't be expressed in classical planning

Specify standard ways of solving problems

- » Otherwise, the planning system would have to derive these again and again from "first principles," every time it solves a problem
- » Can speed up planning by many orders of magnitude (e.g., polynomial time versus exponential time)

Dana Nau: Lecture slides for Automated Planning

- HTN are particularly well-suited for planning in dynamic worlds (e.g., robotics [Bevacqua et al. 2015], games [Neil Wallace 2004, p.235])
- Planning is performed at multiple levels within a hierarchy.
- The search space is reduced. Invalid plans can often be ruled out early on. Hierarchical planners support replanning on the fly and can be used in dynamic worlds.

## **HTN Extension**

- Hybrid Planning
- Task Insertion
- Temporal/resource constraints
- State Abstraction
- .