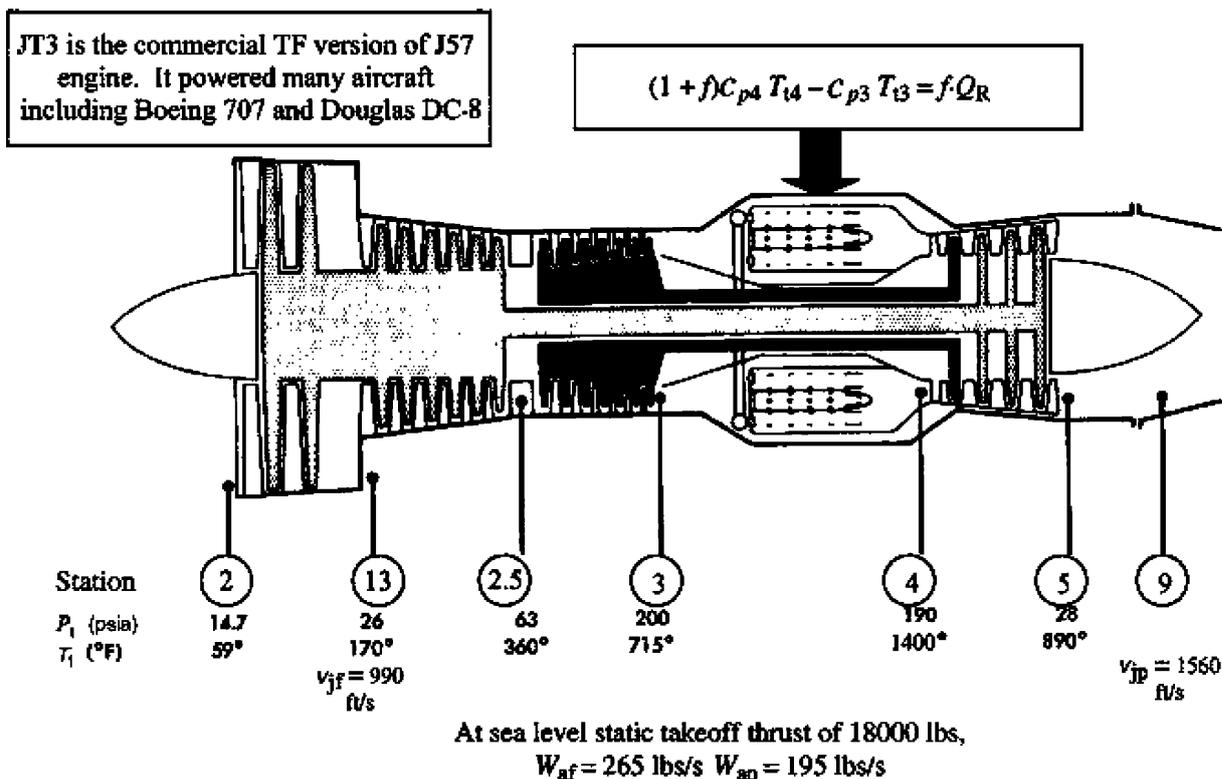


## Farokhi problem 3.2

The total pressures and temperatures of the gas are specified for a turbofan engine with separate exhaust streams (JT3D-3B from Pratt & Whitney, 1974). The mass flow rates in the engine core (or primary) and the engine fan are also specified for the sea level static operation. Calculate:

### JT3D-3B Turbofan Internal pressures and temperatures



|             |         |              |             |           |         |               |           |       |
|-------------|---------|--------------|-------------|-----------|---------|---------------|-----------|-------|
| QR(BTU/lbm) | 18,600  | QR(ft2/s2)   | 465,707,434 | QR(kj/kg) | 43266   | cp3(BTU/lbmR) | 0.24      |       |
|             |         |              |             |           |         | cp4(BTU/lbmR) | 0.26      |       |
| m13(lbm/s)  | 265     | m13(lbm/s)   | 265         | m2(kg/s)  | 120.20  | R3(ft2/s2R)   | 1,717     |       |
| m3(lbm/s)   | 195     | mf(lbm/s)    | 195         | mf(kg/s)  | 88.450  | R4(ft2/s2R)   | 1,716     |       |
| Fn(lbf)     | 18,000  | Fn(lb ft/s2) | 579,150     | Fn(N)     | 80,070  | gamma3        | 1.400     |       |
| V9(ft/s)    | 1,560   |              |             | V9(m/s)   | 475     | k             | 0.286     |       |
| V13(ft/s)   | 990     |              |             | V13(m/s)  | 302     | gamma4        | 1.358     |       |
|             |         |              |             | Si        |         | k             | 0.264     |       |
| Stazioni    | pt(psi) | T(F)         | T(R)        | pt(kPa)   | T(K)    | Si            |           |       |
|             | 2       | 14.7         | 59          | 518.7     | 101.4   | 288.1         | cp(J/kgK) | 1,005 |
|             | 13      | 26.0         | 170         | 629.7     | 179.3   | 349.8         | cp(J/kgK) | 1,089 |
|             | 2.5     | 63           | 360         | 819.7     | 434.4   | 455.4         | R(J/kgK)  | 287   |
|             | 3       | 200          | 715         | 1,174.7   | 1,379.0 | 652.6         | R(J/kgK)  | 287   |
|             | 4       | 190.0        | 1,400       | 1,859.7   | 1,310.0 | 1,033.1       |           |       |
|             | 5       | 28.0         | 890         | 1,349.7   | 193.1   | 749.8         |           |       |
|             | 9       | 14.7         | 59          | 518.7     | 101     | 288.1         |           |       |

a) the engine bypass ratio  $\alpha$  defined as the ratio of fan-to-core flow rate

$$\alpha = \frac{\dot{m}_{13}}{\dot{m}_3} = \frac{265}{195} = \frac{120}{88.5} = 1.36$$

b) from the total temperature rise across the burner, estimate the fuel-to-air ratio and the fuel flow rate in lbm/h, assuming the fuel heating value is  $Q_R \sim 18,600 \cdot BTU/lbm$  and the specific heat at constant pressure is 0.24 and 0.26  $BTU/lbm \cdot R$  at the entrance and exit of the burner, respectively

$$\dot{m}_4 c_{p4} T_{t4} - \dot{m}_3 c_{p3} T_{t3} = \eta_b \dot{m}_f Q_R \quad (1 + f) c_{p4} T_{t4} - c_{p3} T_{t3} = \eta_b f Q_R$$

$$f = \frac{c_{p4} T_{t4} - c_{p3} T_{t3}}{\eta_b Q_R - c_{p4} T_{t4}} = \frac{0.26 \cdot 1860 - 0.24 \cdot 1175}{1 \cdot 18.6 \cdot 10^3 - 0.26 \cdot 1860} = 0.0111$$

$$\dot{m}_f = f \dot{m}_3 = 0.0111 \cdot 195 = 2.17 \cdot \frac{lbm}{s}$$

c) the engine static thrust based on the exhaust velocities and the mass flow rates assuming perfectly expanded nozzles and compare your answer to the specified thrust of 18,000 lbf

$$F = \dot{m}_4 V_9 + \dot{m}_{13} V_{13} = (195 + 2.17)1560 + 265 \cdot 990 = 570 \cdot 10^3 lbm \cdot \frac{ft}{s^2} = \frac{570}{32.18} \cdot 10^3 \cdot lbf \\ = 17.7 \cdot 10^3 \cdot lbf$$

d) the engine thermal efficiency  $\eta_{th}$

$$\eta_{th} = \frac{\dot{m}_4 V_9^2 + \dot{m}_{13} V_{13}^2}{2 \dot{m}_f Q_R} = \frac{(195 + 2.17)1560^2 + 265 \cdot 990^2}{2 \cdot 2.17 \cdot 465.7 \cdot 10^6} = \frac{7.40 \cdot 10^8}{20.21 \cdot 10^8} = 36.6\%$$

e) the thermal efficiency of this engine compared to the afterburning turbojet of Problem 1. Explain the major contributors to the differences in  $\eta_{th}$  in these two engines

$$\pi_c = 13.6 \quad \pi_{c,3.1} = 10.8$$

f) the engine thrust specific fuel consumption in lbm/h/lbf

$$TSFC = \frac{\dot{m}_f}{F} = \frac{2.17 \cdot 3600}{17.7 \cdot 10^3} = 0.441 \frac{lbm}{h \cdot lbf}$$

g) the nondimensional engine specific thrust

$$\frac{F}{\dot{m}_{air} a_0} = \frac{570 \cdot 10^3}{(265 + 195) \sqrt{1.4 \cdot 1717 \cdot 519}} = 1.11$$

h) the Carnot efficiency corresponding to this engine

$$\eta_{Carnot} = 1 - \frac{T_0}{T_{t4}} = 72.1\%$$

i) the engine overall pressure ratio  $p_{t3}/p_{t2}$

$$\pi_c = 13.6$$

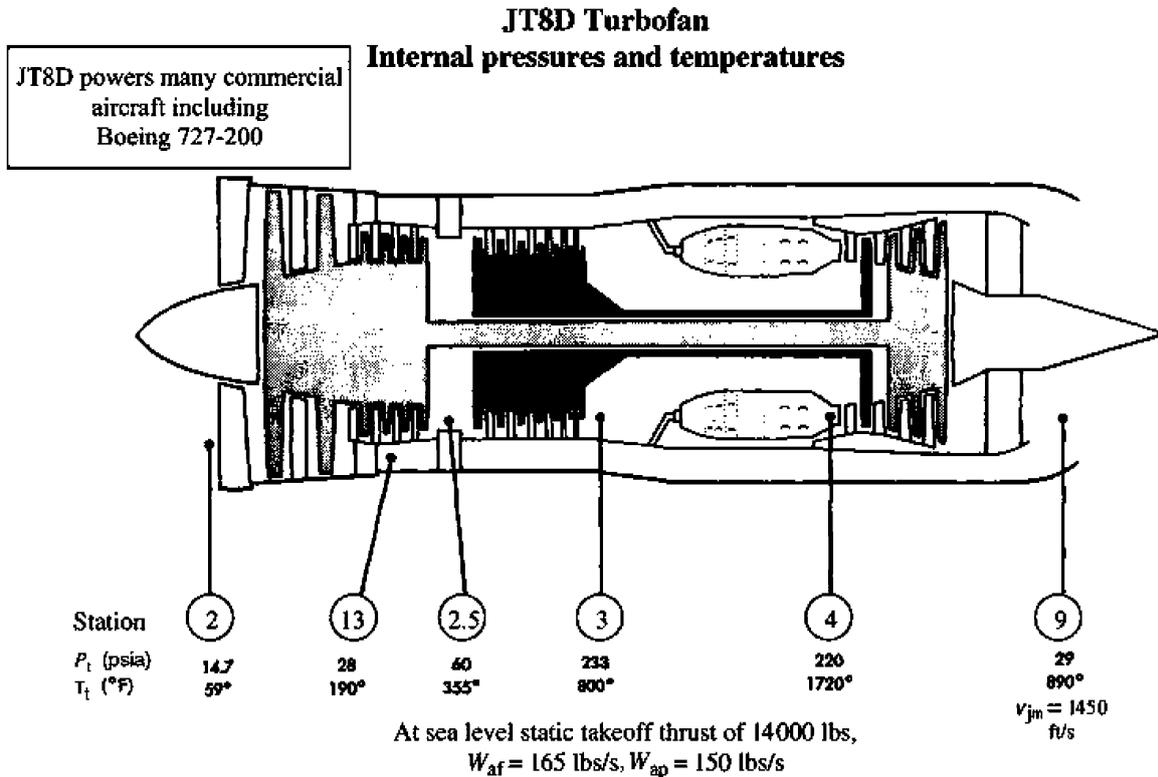
j) fan nozzle exit Mach number (use  $T_t = T + V^2/2c_p$  to calculate local static temperature at the nozzle exit, then local speed of sound.

$$T_t = T + V^2/2 \rightarrow T_{13} = T_{t13} - \frac{V_{13}^2}{2c_p} = 630 - \frac{990^2}{2 \cdot 0.24 \cdot 25 \cdot 10^3} = 548R$$

$$M_{13} = \frac{V_{13}}{a_{13}} = \frac{990}{\sqrt{1.4 \cdot 1717 \cdot 548}} = 0.863$$

|                          |         |         |        | SI              |        |
|--------------------------|---------|---------|--------|-----------------|--------|
| $\alpha$                 | 1.359   |         |        | $\alpha$        | 1.359  |
| f                        | 0.011   |         |        | f               | 0.011  |
| $\pi_{Fan}$              | 1.769   |         |        | $\pi_{cLP}$     | 1.769  |
| $\pi_c$                  | 7.692   |         |        | $\pi_{cHP}$     | 7.692  |
| $\pi_t$                  | 0.147   |         |        | $\pi_t$         | 0.147  |
| mf                       | 2.170   |         |        | mf              | 0.984  |
| F(lb ft/s <sup>2</sup> ) | 569,935 | Fn(lbf) | 17,714 | F(N)            | 78,796 |
| $\eta_{th}$              | 0.366   |         |        | $\eta_{th}$     | 0.366  |
| TSFC(lbm/h lb)           | 0.441   | 0.434   |        | TSFC(mg/s N)    | 12.491 |
| $\eta_{carnot}$          | 0.721   |         |        | $\eta_{carnot}$ | 0.721  |
| ao                       | 1,117   |         |        | ao              | 340    |
| ST/ao                    | 1.110   |         |        | ST/ao           | 1.110  |
| $\pi_{tot}$              | 13.6    |         |        | $\pi_{tot}$     | 14     |
| T13(R)                   | 548     |         |        | T13             | 305    |
| a13(m/s)                 | 1,148   |         |        | a13             | 350    |
| M13                      | 0.863   |         |        | M13             | 0.863  |

## Farokhi problem 3.3



A mixed exhaust turbofan engine (JT8D from Pratt and Whitney, 1974) is described by its internal pressures and temperature, as well as air mass flow rates and the mixed jet (exhaust) velocity. Let us examine a few parameters for this engine, for a ballpark approximation.

|             |         |                                      |             |           |         |                                       |           |       |
|-------------|---------|--------------------------------------|-------------|-----------|---------|---------------------------------------|-----------|-------|
| QR(BTU/lbm) | 18,600  | QR(ft <sup>2</sup> /s <sup>2</sup> ) | 465,707,434 | QR(kJ/kg) | 43266   | cp3(BTU/lbmR)                         | 0.24      |       |
|             |         |                                      |             | SI        |         | cp4(BTU/lbmR)                         | 0.26      |       |
| m13(lbm/s)  | 165     | m13(lbm/s)                           | 165         | m2(kg/s)  | 74.84   | R3(ft <sup>2</sup> /s <sup>2</sup> R) | 1,717     |       |
| m3(lbm/s)   | 150     | m3(lbm/s)                            | 150         | m3(kg/s)  | 68.039  | R4(ft <sup>2</sup> /s <sup>2</sup> R) | 1,716     |       |
| Fn(lbf)     | 14,000  | Fn(lb ft/s <sup>2</sup> )            | 450,450     | Fn(N)     | 62,277  | gamma3                                | 1.400     |       |
| V9(ft/s)    | 1,450   |                                      |             | V9(m/s)   | 442     | k                                     | 0.286     |       |
|             |         |                                      |             |           |         | gamma4                                | 1.358     |       |
|             |         |                                      |             | SI        |         | k                                     | 0.264     |       |
| Stazioni    | pt(psi) | T(F)                                 | T(R)        | pt(kPa)   | T(K)    | Si                                    |           |       |
|             | 2       | 14.7                                 | 59          | 518.7     | 101.4   | 288.1                                 | cp(J/kgK) | 1,005 |
|             | 13      | 28.0                                 | 190         | 649.7     | 193.1   | 360.9                                 | cp(J/kgK) | 1,089 |
|             | 2.5     | 60                                   | 355         | 814.7     | 413.7   | 452.6                                 | R(J/kgK)  | 287   |
|             | 3       | 233                                  | 800         | 1,259.7   | 1,606.5 | 699.8                                 | R(J/kgK)  | 287   |
|             | 4       | 220.0                                | 1,720       | 2,179.7   | 1,516.9 | 1,210.9                               |           |       |
|             | 9       | 29.0                                 | 890         | 1,349.7   | 200.0   | 749.8                                 |           |       |

(a) Estimate the fuel flow rate from the total temperature rise across the burner assuming the fuel heating value  $Q_R \sim 18,600 \cdot \text{BTU}/\text{lbm}$  and the specific heat at constant pressure is 0.24 and 0.26  $\text{BTU}/\text{lbm} \cdot \text{R}$  at the entrance and exit of the burner, respectively

$$f = \frac{c_{p4}T_{t4} - c_{p3}T_{t3}}{\eta_b Q_R - c_{p4}T_{t4}} = \frac{0.26 \cdot 2180 - 0.24 \cdot 1260}{1 \cdot 18.6 \cdot 10^3 - 0.26 \cdot 2180} = 0.0147$$

$$\dot{m}_f = f \dot{m}_3 = 0.0147 \cdot 150 = 2.20 \cdot \frac{\text{lbm}}{\text{s}}$$

(b) Calculate the momentum thrust at the exhaust nozzle and compare it to the specified thrust of 14,000 lbf

$$F = (\dot{m}_3 + \dot{m}_f + \dot{m}_{13})V_9 = (150 + 2.20 + 165)1450 = 460 \cdot 10^3 \text{lbm} \cdot \frac{\text{ft}}{\text{s}^2} = \frac{460}{32.18} \cdot 10^3 \cdot \text{lbf} \\ = 14.3 \cdot 10^3 \cdot \text{lbf}$$

(c) Estimate the thermal efficiency of this engine and compare it to Problems 3.1 and 3.2 as well as a Carnot cycle operating between the temperature extremes of this engine. Explain the differences

$$\eta_{\text{th}} = \frac{(\dot{m}_3 + \dot{m}_f + \dot{m}_{13})V_9^2}{2\dot{m}_f Q_R} = \frac{(150 + 2.20 + 165)1450^2}{2 \cdot 2.20 \cdot 465.7 \cdot 10^6} = \frac{6.67 \cdot 10^8}{20.5 \cdot 10^8} = 32.6\%$$

$$\eta_{\text{Carnot}} = 1 - \frac{T_0}{T_{t4}} = 1 - \frac{519}{2,180} = 76.2\%$$

(d) Estimate the specific fuel consumption for this engine in lbm/h/lbf

$$TSFC = \frac{\dot{m}_f}{F} = \frac{2.20 \cdot 3600}{14.3 \cdot 10^3} = 0.554 \frac{\text{lbm}}{\text{h} \cdot \text{lbf}}$$

(e) The overall pressure ratio (of the fan-compressor section)  $p_{t3}/p_{t2}$

$$\frac{p_{t3}}{p_{t2}} = \frac{233}{14.7} = 15.9$$

(f) What is the bypass ratio  $\alpha$  for this engine at takeoff

$$\alpha = \frac{\dot{m}_{13}}{\dot{m}_3} = \frac{165}{150} = 1.10$$

(g) What is the Carnot efficiency corresponding to this engine

$$\eta_{\text{Carnot}} = 1 - \frac{T_0}{T_{t4}} = 1 - \frac{519}{1260} = 76.2\%$$

(h) Estimate nozzle exit Mach number [look at part (j) in Problem 3.2]

$$T_t = T + V^2/2 \rightarrow T_9 = T_{t9} - \frac{V_9^2}{2c_p} = 1350 - \frac{1450^2}{2 \cdot 0.26 \cdot 25 \cdot 10^3} = 1188 \cdot R$$

$$M_9 = \frac{V_9}{a_9} = \frac{1450}{\sqrt{1.4 \cdot 1716 \cdot 1188}} = 0.86$$

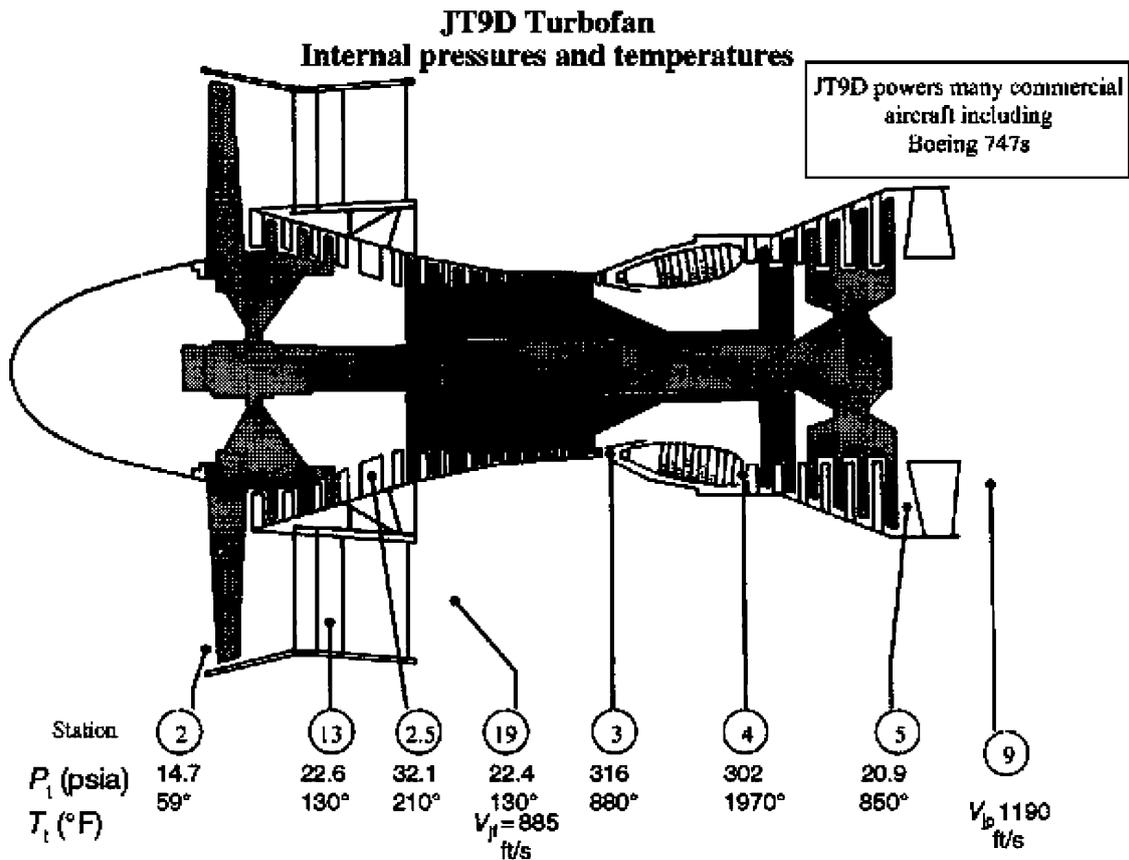
(i) What is the low-pressure compressor (LPC) pressure ratio  $p_{t25}/p_{t2}$

(j) What is the high-pressure compressor (HPC) pressure ratio  $p_{t3}/p_{t25}$

$$\frac{p_{t25}}{p_{t2}} = \frac{60}{14.7} = 4.08 \quad \frac{p_{t3}}{p_{t25}} = \frac{233}{60} = 3.88$$

|                          |         |         |        | SI              |        |
|--------------------------|---------|---------|--------|-----------------|--------|
| $\alpha$                 | 1.100   |         |        | $\alpha$        | 1.100  |
| f                        | 0.0147  |         |        | f               | 0.0147 |
| $\pi_{LPC+Fan}$          | 4.082   |         |        | $\pi_{LPC+Fan}$ | 4.082  |
| $\pi_{cHP}$              | 3.883   |         |        | $\pi_{cHP}$     | 3.883  |
| $\pi_c$                  | 15.850  |         |        | $\pi_c$         | 15.850 |
| $\pi_t$                  | 0.132   |         |        | $\pi_t$         | 0.132  |
| mf                       | 2.199   |         |        | mf              | 0.998  |
| F(lb ft/s <sup>2</sup> ) | 459,939 | Fn(lbf) | 14,295 | F(N)            | 63,588 |
| $\eta_{th}$              | 0.326   |         |        | $\eta_{th}$     | 0.156  |
| TSFC(lbm/h lb)           | 0.554   |         |        | TSFC(mg/s N)    | 15.687 |
| $\eta_{carnot}$          | 0.762   |         |        | $\eta_{carnot}$ | 0.762  |
| ao                       | 1,117   |         |        | ao              | 340    |
| ST/ao                    | 1.308   |         |        | ST/ao           | 1.308  |
| $\pi_{tot}$              | 16      |         |        | $\pi_{tot}$     | 16     |
| T9(R)                    | 1,188   |         |        | T13             | 660    |
| a9(ft/s)                 | 1,664   |         |        | a13             | 515    |
| M9                       | 0.871   |         |        | M13             | 0.858  |

## Farokhi problem 3.4



At sea level static takeoff thrust of 43500 lbs,  $W_{af} = 1248$  lb/s,  $W_{co} = 247$  lb/s

A large bypass ratio turbofan engine (JT9D engine from Pratt and Whitney, 1974) is described by its fan and core engine gas flow properties.

|             |         |                                      |             |           |         |                                       |       |
|-------------|---------|--------------------------------------|-------------|-----------|---------|---------------------------------------|-------|
| QR(BTU/lbm) | 18,600  | QR(ft <sup>2</sup> /s <sup>2</sup> ) | 465,707,434 | QR(kJ/kg) | 43266   | cp3(BTU/lbmR)                         | 0.24  |
|             |         |                                      |             | Si        |         | cp4(BTU/lbmR)                         | 0.26  |
| m13(lbm/s)  | 1,248   | m13(lbm/s)                           | 1,248       | m2(kg/s)  | 566.08  | R3(ft <sup>2</sup> /s <sup>2</sup> R) | 1,717 |
| m3(lbm/s)   | 247     | mf(lbm/s)                            | 247         | m3(kg/s)  | 112.037 | R4(ft <sup>2</sup> /s <sup>2</sup> R) | 1,716 |
| Fn(lbf)     | 43,500  | Fn(lb ft/s <sup>2</sup> )            | 1,399,613   | Fn(N)     | 193,502 | gamma3                                | 1.400 |
| V9(ft/s)    | 1,190   |                                      |             | V9(m/s)   | 363     | k                                     | 0.286 |
| V19(ft/s)   | 885     |                                      |             | V19(m/s)  | 270     | gamma4                                | 1.358 |
|             |         |                                      |             | Si        |         | k                                     | 0.264 |
| Stazioni    | pt(psi) | T(F)                                 | T(R)        | pt(kPa)   | T(K)    | Si                                    |       |
| 2           | 14.7    | 59                                   | 518.7       | 101.4     | 288.1   | cp(J/kgK)                             | 1,005 |
| 13          | 22.6    | 130                                  | 589.7       | 155.8     | 327.6   | cp(J/kgK)                             | 1,089 |
| 2.5         | 32      | 210                                  | 669.7       | 221.3     | 372.0   | R(J/kgK)                              | 287   |
| 3           | 316     | 880                                  | 1,339.7     | 2,178.8   | 744.3   | R(J/kgK)                              | 287   |
| 4           | 302.0   | 1,970                                | 2,429.7     | 2,082.3   | 1,349.8 |                                       |       |
| 5           | 20.9    | 850                                  | 1,309.7     | 144.1     | 727.6   |                                       |       |
| 9           | 14.7    | 850                                  | 1,309.7     | 101       | 727.6   |                                       |       |
| 19          | 22.4    | 130                                  | 589.7       | 154       | 327.6   |                                       |       |

(a) What is the overall pressure ratio (OPR) of this engine

$$\pi_c = \frac{p_{t3}}{p_{t2}} = \frac{316}{14.7} = 21.5$$

(b) Estimate the fan gross thrust  $F_{g,fan}$  in lbf

$$F_{Fan} = \dot{m}_{19} V_{19} = 1248 \cdot 885 = 1.10 \cdot 10^6 \text{ lbm} \cdot \frac{ft}{s^2} = \frac{1.10}{32.18} \cdot 10^6 \cdot \text{lbf} = 34.3 \cdot 10^3 \cdot \text{lbf}$$

(c) Estimate the fuel-to-air ratio based on the energy balance across the burner, assuming the fuel heating value is  $Q_R \sim 18,600 \cdot \text{BTU/lbm}$  and the specific heat at constant pressure is 0.24 and 0.26  $\text{BTU/lbm}\cdot\text{R}$  at the entrance and exit of the burner, respectively

$$f = \frac{c_{p4} T_{t4} - c_{p3} T_{t3}}{\eta_b Q_R - c_{p4} T_{t4}} = \frac{0.26 \cdot 2430 - 0.24 \cdot 1340}{1 \cdot 18.6 \cdot 10^3 - 0.26 \cdot 2430} = 0.0172$$

$$\dot{m}_f = f \dot{m}_3 = 0.0172 \cdot 247 = 4.25 \cdot \frac{\text{lbm}}{s}$$

(d) Calculate the core gross thrust and compare the sum of the fan and the core thrusts to the specified engine thrust of 43,500 lbf

$$F_{Core} = \dot{m}_9 V_9 = (4.25 + 247) \cdot 1190 = 0.299 \cdot 10^6 \text{ lbm} \cdot \frac{ft}{s^2} = \frac{.299}{32.18} \cdot 10^6 \cdot \text{lbf} \\ = 9.29 \cdot 10^3 \cdot \text{lbf}$$

$$F_{Tot} = F_{Core} + F_{Fan} = (9.29 + 34.3)10^3 = 43.6 \cdot 10^3 \cdot \text{lbf} \quad \frac{F_{Core}}{F_{Tot}} = \frac{9.29}{43.6} = 21.3\%$$

(e) Calculate the engine thermal efficiency and compare it to Problems 3.1–3.3. Explain the differences

$$\eta_{th} = \frac{(\dot{m}_3 + \dot{m}_f) V_9^2 + \dot{m}_{19} V_{19}^2}{2 \dot{m}_f Q_R} = \frac{(4.25 + 247) \cdot 1190^2 + 1248 \cdot 885^2}{2 \cdot 4.25 \cdot 465.7 \cdot 10^6} = \frac{13.3 \cdot 10^8}{39.7 \cdot 10^8} = 33.5\%$$

(f) Estimate the thrust-specific fuel consumption (TSFC), in  $\text{lbm/h/lbf}$

$$TSFC = \frac{\dot{m}_f}{F} = \frac{4.25 \cdot 3600}{43.6 \cdot 10^3} = 0.352 \frac{\text{lbm}}{\text{h} \cdot \text{lbf}}$$

(g) What is the bypass ratio of this turbofan engine

$$\alpha = \frac{\dot{m}_{19}}{\dot{m}_3} = \frac{1248}{247} = 5.05$$

(h) What is the Carnot efficiency  $\eta_{Carnot}$  corresponding to this engine

$$\eta_{Carnot} = 1 - \frac{T_0}{T_{t4}} = 1 - \frac{519}{2,430} = 78.6\%$$

(i) What is the LPC pressure ratio  $p_{t25}/p_{t2}$

(j) What is the HPC pressure ratio  $p_{t3}/p_{t25}$

$$\pi_{CLP} = \frac{p_{t25}}{p_{t2}} = \frac{32}{14.7} = 2.18 \quad \pi_{CHP} = \frac{p_{t3}}{p_{t25}} = \frac{316}{32} = 9.88 \quad \pi_c = 21.5$$

(k) Estimate the fan nozzle exit Mach number [see part (j) in Problem 3.2]

$$T_t = T + V^2/2 \rightarrow T_{19} = T_{t19} - \frac{V_{19}^2}{2c_p} = 590 - \frac{885^2}{2 \cdot 0.24 \cdot 25 \cdot 10^3} = 525 \cdot R$$

$$M_{19} = \frac{V_{19}}{a_{19}} = \frac{885}{\sqrt{1.4 \cdot 1717 \cdot 525}} = 0.788$$

(l) Estimate the primary nozzle exit Mach number

$$T_t = T + V^2/2 \rightarrow T_9 = T_{t9} - \frac{V_9^2}{2c_p} = 1310 - \frac{1190^2}{2 \cdot 0.26 \cdot 25 \cdot 10^3} = 1201 \cdot R$$

$$M_{19} = \frac{V_{19}}{a_{19}} = \frac{1190}{\sqrt{1.4 \cdot 1716 \cdot 1201}} = 0.71$$

Valutare inoltre il lavoro nei vari stadi del compressore, nella turbina e il calore scambiato nella camera di combustione.

$$W_{CLP} = \dot{m}_3 c_p (T_{t25} - T_{t2}) = 247 \cdot 0.24(670 - 519) = 8,950 \cdot \frac{BTU}{lbmR} = 9,444 \cdot kW$$

$$W_{CHP} = \dot{m}_3 c_p (T_{t3} - T_{t25}) = 247 \cdot 0.24(1340 - 670) = 39.7 \cdot 10^3 \cdot \frac{BTU}{lbmR} = 41.9 \cdot 10^3 \cdot kW$$

$$W_F = \dot{m}_{13} c_p (T_{t19} - T_{t2}) = 1248 \cdot 0.24(590 - 519) = 21,230 \cdot \frac{BTU}{lbmR} = 22,400 \cdot kW$$

$$W_{tot} = W_c + W_F = 9.444 + 41.9 + 22.4 = 73.8 \cdot MW$$

$$W_t = \dot{m}_4 c_{p4} (T_{t5} - T_{t4}) = (247 + 4.25) \cdot 0.26(1310 - 2430) = 73,200 \cdot \frac{BTU}{lbmR} = 77.2 \cdot MW$$

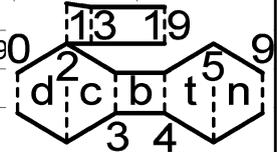
$$\Delta Q_{cc} = \dot{m}_4 c_{p4} T_{t4} - \dot{m}_3 c_p T_{t3} = (247 + 4.25) \cdot 0.26 \cdot 2430 - 247 \cdot 0.24 \cdot 1340 = \\ = 79,300 \cdot \frac{BTU}{lbmR} = 83.7 \cdot MW$$

|                              |           |                   |        |                      |         |
|------------------------------|-----------|-------------------|--------|----------------------|---------|
|                              |           |                   |        | SI                   |         |
| $\alpha$                     | 5.053     |                   |        | $\alpha$             | 5.053   |
| f                            | 0.017     |                   |        | f                    | 0.017   |
| $\pi_{LPC}$                  | 2.184     |                   |        | $\pi_{cLP}$          | 2.184   |
| $\pi_{cHP}$                  | 9.844     |                   |        | $\pi_{cHP}$          | 9.844   |
| $\pi_c$                      | 21.497    |                   |        | $\pi_c$              | 21.497  |
| $\pi_t$                      | 0.069     |                   |        | $\pi_t$              | 0.069   |
| mf                           | 4.264     |                   |        | mf                   | 1.934   |
| $F_{Fan}(\text{lb ft/s}^2)$  | 1,104,480 | $F_n(\text{lbf})$ | 34,327 | $F_{Fan}(\text{N})$  | 152,699 |
| $F_{main}(\text{lb ft/s}^2)$ | 299,004   | $F_n(\text{lbf})$ | 9,293  | $F_{main}(\text{N})$ | 41,339  |
| $F(\text{lb ft/s}^2)$        | 1,403,484 | $F_n(\text{lbf})$ | 43,620 | $F(\text{N})$        | 194,038 |
| $\eta_{th}$                  | 0.336     |                   |        | $\eta_{th}$          | 0.336   |
| Tsfc(lbm/h lb)               | 0.352     |                   |        | Tsfc(mg/s N)         | 9.968   |
| $\eta_{carnot}$              | 0.787     |                   |        | $\eta_{carnot}$      | 0.787   |
| ao                           | 1,117     |                   |        | ao                   | 340     |
| ST/ao                        | 0.841     |                   |        | ST/ao                | 0.841   |
| $\pi_{tot}$                  | 21.5      |                   |        | $\pi_{tot}$          | 21      |
| T19(R)                       | 525       |                   |        | T19                  | 291     |
| a19(ft/s)                    | 1,123     |                   |        | a19                  | 342     |
| M19                          | 0.788     |                   |        | M19                  | 0.788   |
| T9(R)                        | 1,201     |                   |        | T9                   | 667     |
| a9(ft/s)                     | 1,673     |                   |        | a9                   | 510     |
| M9                           | 0.711     |                   |        | M9                   | 0.711   |



# J79D by Tom

| JT9d By Tom     |         |      |       |            |        |          |        |
|-----------------|---------|------|-------|------------|--------|----------|--------|
|                 | 2       | 3    | 4     | 5          | 9      | 13       | 190    |
|                 | diff    | comp | CC    | Tur        | No     | Fan      | No FAn |
| $c_p$           | 1004    |      |       | 1057       |        |          |        |
| $\gamma$        | 1.4     |      |       | 1.35       |        |          |        |
| $\pi$           | 1       | 21.5 | 0.955 |            | 0.98   | 1.53     | 0.99   |
| $\eta, e_{c,t}$ |         | 0.92 | 0.95  | 0.9        |        | 0.96     |        |
| Tt              |         |      |       | 1349.8     |        |          |        |
| M0              | 0       |      |       |            | QR     | 42800    | kJ/kgK |
| T0              | 288 K   |      | p0    | 101,300 Pa |        | $\eta_m$ | 0.98   |
| alpha           | 5.053   |      |       |            |        |          |        |
| k               | 0.28571 |      |       | 0.25926    |        |          |        |
| R               | 286.857 |      |       | 274.037    | kJ/kgK |          |        |
| a0              | 340.1   | m/s  | V0    | 0.0        | m/s    |          |        |



$$k = \frac{\gamma - 1}{\gamma} = \frac{1.4 - 1}{1.4} = 0.286 \quad k_t = \frac{\gamma_t - 1}{\gamma_t} = \frac{1.35 - 1}{1.35} = 0.259$$

$$R = k c_p = 1004 \cdot 0.286 = 287 \cdot \frac{J}{kg \cdot K}$$

$$R_t = k_t c_{pt} = 1057 \cdot 0.259 \frac{J}{kg \cdot K} = 274 \cdot \frac{J}{kg \cdot K}$$

## Effetto Ram

$$a_0 = \sqrt{\gamma R T_0} = \sqrt{1.4 \cdot 287 \cdot 288} = 340 \cdot \frac{m}{s} \quad V_0 = M_0 a_0 = 0 \cdot 340 = 0 \frac{m}{s}$$

$$\tau_r = \psi_0 = 1 + \frac{\gamma - 1}{2} M_0^2 = 1 \quad T_{t0} = T_0 \tau_r = 288 \cdot 1 = 288 \cdot K$$

$$p_{t0} = p_0 \tau_r^{\frac{1}{k}} = 1.013 \cdot 10^5 \cdot 1^{\frac{1}{0.286}} = 1.013 \cdot 10^5 \cdot Pa$$

## Diffusore

$$p_{t2} = p_{t0} \pi_d = 1.013 \cdot 10^5 \cdot 1 = 1.013 \cdot 10^5 Pa$$

## Compressore

$$\tau_c = \pi_c^{\frac{k}{\gamma}} = 21.5^{\frac{0.286}{0.92}} = 2.60 \quad p_{t3} = p_{t2} \pi_c = 1.013 \cdot 10^5 \cdot 21.5 = 2.18 \cdot 10^6 \cdot Pa$$

$$T_{t3} = \tau_c T_{t2} = 2.60 \cdot 288 = 749 \cdot K$$

## Camera di Combustione

$$\tau_\lambda = \frac{c_{pt} T_{t4}}{c_p T_0} = \frac{1057 \cdot 1350}{1004 \cdot 288} = 4.93$$

$$f = \frac{\tau_\lambda - \tau_c \tau_r}{Q_R \eta_b / (c_p T_0) - \tau_\lambda} = \frac{4.93 - 2.60 \cdot 1}{\frac{42.8 \cdot 10^6 \cdot 0.95}{1004 \cdot 288} - 4.93} = 0.01717$$

$$\tau_b = \frac{\tau_\lambda}{\tau_c \tau_r} = \frac{4.93}{2.60 \cdot 1} = 1.896$$

$$p_{t4} = p_{t3} \pi_b = 2.18 \cdot 10^6 \cdot 0.955 = 2.08 \cdot 10^6 \cdot Pa$$

## Fan

$$\tau_f = \pi_f^{\frac{k}{e_f}} = 1.53^{\frac{0.286}{0.96}} = 1.135 \quad p_{t13} = p_{t2} \pi_f = 1.013 \cdot 10^5 \cdot 1.53 = 1.550 \cdot 10^6 \cdot Pa$$

$$T_{t13} = T_{t2} \tau_f = 288 \cdot 1.135 = 327 \cdot K$$

## Turbina

$$\tau_t = 1 - \frac{\tau_r [(\tau_c - 1) + \alpha(\tau_f - 1)]}{\eta_m (1 + f) \tau_\lambda} = 1 - \frac{1[1.60 + 5.05 \cdot 0.135]}{0.98 \cdot 1.017 \cdot 4.93} = 0.536$$

$$\pi_t = \tau_t^{\frac{1}{k_t e_t}} = 0.536^{\frac{1}{0.259 \cdot 0.90}} = 0.0689$$

$$p_{t5} = p_{t4} \pi_t = 2.08 \cdot 10^6 \cdot 0.0689 = 0.1433 \cdot 10^6 \cdot Pa \quad T_{t5} = T_{t4} \tau_t = 1350 \cdot 0.536 = 724 \cdot K$$

## Ugello

$$p_{t9} = p_{t5} \pi_n = 0.1433 \cdot 10^6 \cdot 0.98 = 0.1404 \cdot 10^6 \cdot Pa \quad T_{t9} = T_{t5} = 724 \cdot K$$

$$\frac{p_{t9}}{p_9} = \pi_n \pi_t \pi_b \pi_c \pi_d \pi_r \frac{p_0}{p_9} = \frac{p_{t9} p_0}{p_0 p_9} = \frac{1.404}{1.013} \cdot 1 = 1.386$$

$$\psi_9 = \frac{T_{t9}}{T_9} = 1 + \frac{\gamma_t - 1}{2} M_9^2 = \left( \frac{p_{t9}}{p_9} \right)^{k_t} = (1.386)^{0.259} = 1.088$$

$$M_9 = \sqrt{\frac{2}{\gamma_t - 1} (\psi_9 - 1)} = \sqrt{\frac{2}{0.35} (1.088 - 1)} = 0.710$$

$$T_9 = \frac{T_9}{T_{t9}} T_{t9} = \frac{724}{1.088} = 665 \cdot K$$

$$a_9 = \sqrt{\gamma_t R_9 T_9} = \sqrt{1.35 \cdot 274 \cdot 665} = 496 \cdot \frac{m}{s} \quad V_9 = M_9 a_9 = 0.710 \cdot 496 = 352 \cdot \frac{m}{s}$$

$$V_{9,e} = V_9 \left( 1 + \frac{1 - \frac{p_0}{p_9}}{\gamma_9 M_9^2} \right) = V_9 \quad \frac{V_9}{a_0} = \frac{352}{340} = 1.035$$

## Ugello Fan

$$p_{t19} = p_{t13} \pi_{nf} = 1.550 \cdot 10^5 \cdot 0.99 = 1.535 \cdot 10^5 \cdot Pa \quad T_{t19} = T_{t13} = 327 \cdot K$$

$$\frac{p_{t19}}{p_{19}} = \frac{p_{t19} p_0}{p_0 p_{19}} = \frac{153.5}{101.3} \cdot 1 = 1.515 \quad \psi_{19} = \frac{T_{t19}}{T_{19}} = \left( \frac{p_{t19}}{p_{19}} \right)^k = (1.515)^{0.286} = 1.126$$

$$M_{19} = \sqrt{\frac{2}{\gamma - 1} (\psi_{19} - 1)} = \sqrt{\frac{2}{0.4} (1.126 - 1)} = 0.794$$

$$T_{19} = \frac{T_{19}}{T_{t19}} T_{t19} = \frac{327}{1.126} = 290 \cdot K \quad a_{19} = \sqrt{\gamma R T_{19}} = \sqrt{1.40 \cdot 287 \cdot 290} = 341 \frac{m}{s}$$

$$V_{19} = M_{19} a_{19} = 0.794 \cdot 341 = 271 \cdot \frac{m}{s}$$

$$V_{19,e} = V_{19} \left( 1 + \frac{1 - \frac{p_0}{p_{19}}}{\gamma M_{19}^2} \right) = V_{19} \quad \frac{V_{19}}{a_0} = \frac{271}{340} = 0.797$$

## Spinta e rendimenti

$$\frac{F_u}{\dot{m}_{air} a_0} = \frac{F_{u,core}}{\dot{m}_{air} a_0} + \frac{F_{u,Fan}}{\dot{m}_{air} a_0} = \frac{(1+f) V_{9,e}}{1+\alpha} + \frac{\alpha V_{19,e}}{1+\alpha} - M_0$$

$$\frac{F_{u,core}}{\dot{m}_{air} a_0} = \frac{(1+f) V_{9,e}}{1+\alpha} - \frac{M_0}{1+\alpha} = \frac{1.017}{6.05} 1.035 - 0 = 0.1740$$

$$\frac{F_{u,Fan}}{\dot{m}_{air} a_0} = \frac{\alpha V_{19,e}}{1+\alpha} - \frac{\alpha M_0}{1+\alpha} = \frac{5.05}{6.05} 0.797 - 0 = 0.665$$

$$\frac{F_u}{\dot{m}_{air} a_0} = \frac{F_{u,core}}{\dot{m}_{air} a_0} + \frac{F_{u,Fan}}{\dot{m}_{air} a_0} = 0.1740 + 0.665 = 0.839$$

$$\frac{F_{u,core}}{F_u} = \frac{0.1740}{0.839} = 21\% \quad \frac{F_{u,Fan}}{F_u} = \frac{0.665}{0.839} = 79.3\%$$

$$\frac{F_u}{\dot{m}_0} = D = (1+f)V_{9,e} + \alpha V_{19,e} - (1+\alpha)V_0 = 1.017 \cdot 352 + 5.05 \cdot 271 - 6.05 \cdot 0 = 1727 \cdot \frac{s}{m}$$

$$TSFC = \frac{\dot{m}_f}{F_u} = \frac{f}{F_u/\dot{m}_0} = \frac{f}{(1+f)V_{9,e} + \alpha V_{19,e} - (1+\alpha)V_0} = \frac{0.01717}{1727} = 9.94 \cdot 10^{-6} \cdot \frac{kg}{sN}$$

$$N = (1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2 = 1.017 \cdot 352^2 + 5.05 \cdot 271^2 - 6.05 \cdot 0$$

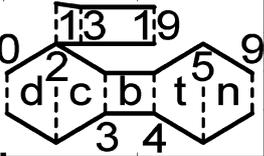
$$= 4.97 \cdot 10^5 \cdot \frac{m^2}{s^2}$$

$$\eta_{th} = \frac{\Delta K \dot{E}}{\mathcal{P}_t} = \frac{(1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2}{2fQ_R} = \frac{4.97 \cdot 10^5}{2 \cdot 0.01717 \cdot 42.8 \cdot 10^6} = 33.8\%$$

$$\eta_p = \frac{F_u V_0}{\Delta K \dot{E}} = \frac{2V_0[(1+f)V_{9,e} + \alpha V_{19,e} - (1+\alpha)V_0]}{(1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2} = 0$$

|          |         |         |          |           |         |          |         |          |  |
|----------|---------|---------|----------|-----------|---------|----------|---------|----------|--|
| Section  | c       | f       | t        | $\lambda$ |         | t        |         |          |  |
| $\tau$   | 2.59299 | 1.13493 | 0.53755  | 4.93422   | $\pi$   | 0.06993  |         |          |  |
| Section  | 0       | 2       | 3        | 4         | 5       | 9        | 13      | 19       |  |
| Tt       | 288.0   | 288     | 746.8    | 1349.8    | 725.586 | 725.586  | 326.859 | 326.859  |  |
| pt       | 101,300 | 101,300 | 2.18E+06 | 2.08E+06  | 145,448 | 142,539  | 154,989 | 153,439  |  |
| Core     |         | f       | 0.01726  |           |         |          |         |          |  |
| Pt9/p9   | M9      | M9 Eff  | Tt9/T9   | P9        | po/p9   |          |         |          |  |
|          | 1.4071  | 0.72735 | 0.72735  | 1.09258   | 101300  | 1        |         |          |  |
| T9       | a9      | V9      | V9/a0    | V9/a0 eff | F/ma0   | F/maira0 |         | Fc/Ft    |  |
|          | 664.102 | 495.666 | 360.524  | 1.06009   | 1.06009 | 1.07838  | 0.17816 | 0.21127  |  |
| Fan      |         |         |          |           |         |          |         |          |  |
| Pt19/p19 | M19     | M19 Eff | Tt19/T19 | P19       | po/p19  |          |         |          |  |
|          | 1.5147  | 0.79359 | 0.79359  | 1.12596   | 101300  | 1        |         |          |  |
| T19      | a19     | V19     | V19/a0   | V19/a0 ef | F/ma0   | F/maira0 |         | FF/Ft    |  |
|          | 290.294 | 341.441 | 270.965  | 0.79675   | 0.79675 | 4.02595  | 0.66512 | 0.78873  |  |
| Num      | Section | t       | th       | p         | 0       | TSFC*1e3 | F/ma0   | F/maira0 |  |
| 5.03E+05 | $\eta$  | 0.9281  | 0.3407   | 0         | 0       | 0.0099   | 5.10433 | 0.84327  |  |

## J79D by Tom M0=0.85

| JT9d By Tom     |       |      |       |         |      |          |  |  |
|-----------------|-------|------|-------|---------|------|----------|---|--|
|                 | 2     | 3    | 4     | 5       | 9    | 13       | 190   |  |
|                 | diff  | comp | CC    | Tur     | No   | Fan      | No FAn  |  |
| $c_p$           | 1004  |      |       | 1057    |      |          |   |  |
| $\gamma$        | 1.4   |      |       | 1.35    |      |          |   |  |
| $\pi$           | 1     | 21.5 | 0.955 |         | 0.98 | 1.53     | 0.99  |  |
| $\eta, e_{c,t}$ |       | 0.92 | 0.95  | 0.9     |      | 0.96     |   |  |
| Tt              |       |      |       | 1349.8  |      |          |   |  |
| M0              | 0.85  |      |       |         | QR   | 42800    | kJ/kgK  |  |
| T0              | 288 K |      | p0    | 101,300 | Pa   | $\eta_m$ | 0.98  |  |
| alpha           | 5.053 |      |       |         |      |          |   |  |

$$k = \frac{\gamma - 1}{\gamma} = \frac{0.4}{1.4} = 0.287 \quad k_5 = \frac{\gamma_5 - 1}{\gamma_5} = \frac{0.35}{1.35} = 0.259$$

$$R = k c_p = 0.287 \cdot 1004 = 287 \text{ J/kgK} \quad R_5 = 0.259 \cdot 1057 = 274 \text{ J/kgK}$$

$$a_0 = \sqrt{\gamma R T_0} = 1.4 \cdot 287 \cdot 288 = 340 \text{ m/s}$$

$$V_0 = M_0 \cdot a_0 = 0.85 \cdot 340 = 289 \text{ m/s}$$

### Preso d'aria

$$\tau_r = \psi_0 = 1 + \frac{\gamma - 1}{2} M_0^2 = 1 + 0.2 \cdot 0.85^2 = 1.145$$

$$T_{t0} = T_{t2} = T_0 \tau_r = 288 \cdot 1.145 = 330 \text{ K} \quad p_{t0} = \tau_r^{\frac{1}{k}} p_0 = 1.145^{\frac{1}{0.287}} 1.013 \cdot 10^5 = 162.6 \text{ kPa}$$

$$p_{t2} = p_{t0} \pi_d = 162.6 \cdot 1 = 162.6 \text{ kPa}$$

### Compressore

$$\tau_c = \pi_c^{\frac{k}{e_c}} = 21.5^{\frac{0.287}{0.92}} = 2.60$$

$$p_{t3} = p_{t2} \pi_c = 162.6 \cdot 21.5 \cdot 10^3 = 3500 \text{ kPa} \quad T_{t3} = T_{t2} \tau_c = 330 \cdot 2.60 = 858 \cdot \text{K}$$

### Camera di combustione

$$p_{t4} = p_{t3} \pi_b = 3500 \cdot 0.955 \cdot 10^3 = 3334 \text{ kPa} \quad \tau_\lambda = \frac{c_{p5} T_{t4}}{c_p T_0} = \frac{1057 \cdot 1350}{288 \cdot 1004} = 4.93$$

$$f = \frac{\tau_\lambda - \tau_c \tau_r}{Q_R \eta_b / (c_p T_0) - \tau_\lambda} = \frac{4.93 - 2.600 \cdot 1.145}{42.8 \cdot 10^6 \cdot 0.95 / (288 \cdot 1004) - 4.93} = 0.01439$$

### Fan

$$\tau_f = \pi_f^{\frac{k}{e_f}} = 1.53^{\frac{0.287}{0.96}} = 1.135$$

$$p_{t13} = p_{t2} \pi_f = 162.6 \cdot 1.53 \cdot 10^3 = 249 \cdot \text{kPa} \quad T_{t13} = T_{t2} \tau_f = 330 \cdot 1.135 = 375 \cdot \text{K}$$

## Turbina

$$\tau_t = 1 - \frac{\tau_r[(\tau_c - 1) + \alpha(\tau_f - 1)]}{\eta_m(1+f)\tau_\lambda} = 1 - \frac{1.145[1.60 + 5.05 \cdot 0.135]}{0.98 \cdot 1.014 \cdot 4.93} = 0.467$$

$$\pi_t = \tau_t^{\frac{1}{k_5 e_t}} = 0.467^{\frac{1}{0.259 \cdot 0.900}} = 0.0381$$

$$p_{t5} = p_{t4} \pi_t = 334 \cdot 0.0381 \cdot 10^3 = 127.3 \cdot kPa$$

$$T_{t5} = T_{t4} \tau_t = 1350 \cdot 0.467 = 630 \cdot K$$

## Ugello

$$p_{t9} = p_{t5} \pi_n = 127.3 \cdot 0.98 \cdot 10^3 = 124.8 \cdot kPa$$

$$\frac{p_{t9}}{p_9} = \frac{124.8}{101.3} = 1.232 \quad \psi_9 = \left(\frac{p_{t9}}{p_9}\right)^{k_5} = 1.232^{0.259} = 1.056$$

$$M_9 = \sqrt{\frac{2}{\gamma_5 - 1} [\psi_9 - 1]} = \sqrt{\frac{2}{1.35} [1.056 - 1]} = 0.566$$

$$M_9 < 1 \rightarrow p_9 = p_0 \text{ (OK)}$$

$$T_9 = T_{t9} / \psi_9 = T_{t5} / \psi_9 = 630 / 1.056 = 597 \cdot K$$

$$a_9 = \sqrt{\gamma_5 R_5 T_9} = \sqrt{1.35 \cdot 274 \cdot 597} = 470 \cdot m/s$$

$$V_9 = M_9 \cdot a_9 = 0.566 \cdot 470 = 266 \cdot m/s \quad \frac{V_9}{a_0} = \frac{266}{340} = 0.782 < M_0 \text{ (??)}$$

## Ugello Fan

$$p_{t19} = \pi_{nf} p_{t13} = 0.99 \cdot 249.0 = 247 \cdot kPa \quad T_{t19} = T_{t13} = 375 \cdot K$$

$$\frac{p_{t19}}{p_{19}} = \frac{p_{t19}}{p_0} \frac{p_0}{p_{19}} = \frac{247}{101.3} = 2.44 \quad \psi_{19} = \frac{T_{t19}}{T_{19}} = \left(\frac{p_{t19}}{p_{19}}\right)^k = (2.44)^{0.286} = 1.291$$

$$M_{19} = \sqrt{\frac{2}{\gamma - 1} (\psi_{19} - 1)} = \sqrt{\frac{2}{0.4} (1.291 - 1)} = 1.205$$

Se l'ugello non è convergente divergente allora  $\frac{p_0}{p_{19}} \neq 1$ . Si impone  $M_{19} = 1$

$$\frac{T_{t19}}{T_{19}} = \psi_{19} = 1 + \frac{\gamma - 1}{2} M_{19}^2 = 1 + \frac{0.4}{2} = 1.200 \quad T_{19} = \frac{T_{t19}}{T_{t19}} T_{t19} = \frac{375}{1.200} = 313 \cdot K$$

$$\frac{p_{t19}}{p_{19}} = \left(\frac{T_{t19}}{T_{19}}\right)^{\frac{1}{k}} = 1.200^{\frac{1}{0.286}} = 1.892$$

$$p_{19} = \frac{p_{t19}}{p_{t19}} p_{t19} = \frac{247}{1.892} = 130.5 \cdot kPa \quad \frac{p_0}{p_{19}} = \frac{101.3}{130.5} = 0.776$$

$$a_{19} = \sqrt{\gamma R T_{19}} = \sqrt{1.40 \cdot 287 \cdot 313} = 355 \cdot \frac{m}{s} \quad V_{19} = M_{19} a_{19} = 1 \cdot 355 = 355 \cdot \frac{m}{s}$$

$$V_{19.e} = V_{19} \left(1 + \frac{1 - \frac{p_0}{p_{19}}}{\gamma M_{19}^2}\right) = 355 \left(1 + \frac{1 - 0.776}{1.4 \cdot 1^2}\right) = 412 \cdot \frac{m}{s} \quad \frac{V_{19.e}}{a_0} = \frac{412}{340} = 1.211$$

## Spinta

$$\frac{F_u}{\dot{m}_{air} a_0} = \frac{F_{u.core}}{\dot{m}_{air} a_0} + \frac{F_{u.Fan}}{\dot{m}_{air} a_0} = \frac{(1+f)}{1+\alpha} \frac{V_{9.e}}{a_0} + \frac{\alpha}{1+\alpha} \frac{V_{19.e}}{a_0} - M_0$$

$$\frac{F_{u.core}}{\dot{m}_{air} a_0} = \frac{(1+f)}{1+\alpha} \frac{V_{9.e}}{a_0} - \frac{M_0}{1+\alpha} = \frac{1.014}{6.05} \cdot 0.782 - \frac{0.85}{6.05} = -0.00943$$

$$\frac{F_{u.Fan}}{\dot{m}_{air} a_0} = \frac{\alpha}{1+\alpha} \frac{V_{19.e}}{a_0} - \frac{\alpha M_0}{1+\alpha} = \frac{5.05}{6.05} (1.211 - 0.85) = 0.301$$

$$\frac{F_u}{\dot{m}_{air} a_0} = \frac{F_{u.core}}{\dot{m}_{air} a_0} + \frac{F_{u.Fan}}{\dot{m}_{air} a_0} = -0.0094 + 0.301 = 0.292$$

$$\frac{F_{u.core}}{F_u} = \frac{-0.00943}{0.292} = -3.23\% \quad \frac{F_{u.Fan}}{F_u} = \frac{0.301}{0.292} = 103.1\%$$

$$\frac{F_u}{\dot{m}_0} = D = (1+f)V_{9.e} + \alpha V_{19.e} - (1+\alpha)V_0 = 1.014 \cdot 266 + 5.05 \cdot 412 - 6.05 \cdot 289 = 602 \cdot \frac{s}{m}$$

$$TSFC = \frac{\dot{m}_f}{F_u} = \frac{f}{F_u/\dot{m}_0} = \frac{f}{(1+f)V_{9.e} + \alpha V_{19.e} - (1+\alpha)V_0} = \frac{0.01439}{611} = 2.39 \cdot 10^{-5} \cdot \frac{kg}{sN}$$

$$N = (1+f)V_{9.e}^2 + \alpha V_{19.e}^2 - (1+\alpha)V_0^2 = 1.014 \cdot 280^2 + 5.05 \cdot 411^2 - 6.05 \cdot 289^2 = 4.23 \cdot 10^5$$

$$\eta_{th} = \frac{\Delta K \dot{E}}{\mathcal{P}_t} = \frac{(1+f)V_{9.e}^2 + \alpha V_{19.e}^2 - (1+\alpha)V_0^2}{2fQ_R} = \frac{4.23 \cdot 10^5}{2 \cdot 0.01439 \cdot 42.8 \cdot 10^6} = 34.3\%$$

$$\eta_p = \frac{F_u V_0}{\Delta K \dot{E}} = \frac{2V_0[(1+f)V_{9.e} + \alpha V_{19.e} - (1+\alpha)V_0]}{(1+f)V_{9.e}^2 + \alpha V_{19.e}^2 - (1+\alpha)V_0^2} = \frac{2 \cdot 289 \cdot 602}{4.23 \cdot 10^5} = 82.3\%$$

$$\eta_0 = \eta_p \eta_{th} = .343 \cdot .823 = 28.2\%$$

|                       |         |         |          |           |         |          |          |          |
|-----------------------|---------|---------|----------|-----------|---------|----------|----------|----------|
| k                     | 0.28571 |         |          | 0.25926   |         |          |          |          |
| R                     | 286.857 |         |          | 274.037   | kJ/kgK  |          |          |          |
| a0                    | 340.1   | m/s     | V0       | 289.1     | m/s     |          |          |          |
| $\tau_r = T_{t0} = 0$ | 1.1445  |         |          |           |         |          |          |          |
| Section               | c       | f       | t        | $\lambda$ |         | t        |          |          |
| $\tau$                | 2.59299 | 1.13493 | 0.46929  | 4.93422   | $\pi$   | 0.03907  |          |          |
| Section               | 0       | 2       | 3        | 4         | 5       | 9        | 13       | 19       |
| Tt                    | 329.6   | 329.616 | 854.7    | 1349.8    | 633.443 | 633.443  | 374.09   | 374.0899 |
| pt                    | 162,467 | 162,467 | 3.49E+06 | 3.34E+06  | 130,342 | 127,735  | 248,574  | 246,089  |
| Core                  |         | f       | 0.01449  |           |         |          |          |          |
| Pt9/p9                | M9      | M9 Eff  | Tt9/T9   | P9        | po/p9   |          |          |          |
|                       | 1.26096 | 0.59502 | 1.06196  | 101300    | 1       |          |          |          |
| T9                    | a9      | V9      | V9/a0    | V9/a0 eff | F/ma0   | F/maira0 |          | Fc/Ft    |
|                       | 596.486 | 469.755 | 279.513  | 0.82188   | 0.82188 | -0.01621 | -0.00268 | -0.00913 |
| Fan                   |         |         |          |           |         |          |          |          |
| Pt19/p19              | M19     | M19 Eff | Tt19/T19 | P19       | po/p19  |          |          |          |
|                       | 2.4293  | 1.20137 | 1        | 1.2       | 130004  | 0.77921  |          |          |
| T19                   | a19     | V19     | V19/a0   | V19/a0 ef | F/ma0   | F/maira0 |          | FF/Ft    |
|                       | 311.742 | 353.83  | 353.83   | 1.0404    | 1.20448 | 1.7912   | 0.29592  | 1.00913  |
| Num                   | Section | t       | th       | p         | 0       | TSFC*1e3 | F/ma0    | F/maira0 |
| 4.21E+05              | $\eta$  | 0.93345 | 0.3396   | 0.82835   | 0.28131 | 0.0240   | 1.775    | 0.293243 |

## Farokhi Example 4.16

|                 | 2      | 3    | 4     | 5       | 13     | 15                | 6      | 7         | 9      |
|-----------------|--------|------|-------|---------|--------|-------------------|--------|-----------|--------|
|                 | diff   | comp | CC    | Tur     | Fan    |                   | Mixer  |           | No     |
| $c_p$           | 1004   |      |       | 1152    |        |                   |        | 1241      |        |
| $\gamma$        | 1.4    |      |       | 1.33    |        |                   |        | 1.3       |        |
| $\pi$           | 0.9    | 13   | 0.95  |         | 1.9    | 0.99              | 0.9709 | 0.92      | 0.95   |
| $\eta, e_{c,t}$ |        | 0.9  | 0.98  | 0.8     | 0.9    |                   |        | 0.98      |        |
| $T_t$           |        |      | 1600  |         |        |                   |        | 2000      |        |
| $M_0$           | 2.0000 |      |       |         | QR     | 42000             | kJ/kgK |           |        |
| $T_0$           | 223.0  | K    | $p_0$ | 10000.0 | Pa     | $\eta_m$          | 0.95   | $p_9/p_0$ | 3.8    |
| $k$             | 0.2857 |      |       | 0.2481  |        |                   |        | 0.2308    |        |
| $R$             | 286.9  |      |       | 285.8   | kJ/kgK |                   |        | 286.4     | kJ/kgK |
| $a_0$           | 299.3  | m/s  | $V_0$ | 598.5   | m/s    | $\tau_r = (\psi)$ | 1.8    |           |        |

$$k = \frac{\gamma - 1}{\gamma} = \frac{1.4 - 1}{1.4} = 0.286 \quad k_t = \frac{\gamma_t - 1}{\gamma_t} = \frac{1.33 - 1}{1.33} = 0.248$$

$$k_9 = \frac{\gamma_9 - 1}{\gamma_9} = \frac{1.3 - 1}{1.3} = 0.231 \quad R = k c_p = 1004 \cdot 0.286 = 287 \cdot \frac{J}{kg \cdot K}$$

$$R_t = k_t c_{pt} = 1152 \cdot 0.248 \frac{J}{kg \cdot K} = 286 \cdot \frac{J}{kg \cdot K}$$

$$R_9 = k_9 c_{p9} = 286 \cdot \frac{J}{kg \cdot K} \quad p_0 = 10 \cdot kPa$$

### Effetto Ram

$$a_0 = \sqrt{\gamma R T_0} = \sqrt{1.4 \cdot 287 \cdot 223} = 299 \cdot \frac{m}{s}$$

$$V_0 = M_0 a_0 = 2.0 \cdot 299 = 598 \frac{m}{s} \quad \tau_r = \psi_0 = 1 + \frac{\gamma - 1}{2} M_0^2 = 1.8$$

$$T_{t0} = T_0 \tau_r = 223 \cdot 1.8 = 401 \cdot K$$

$$p_{t0} = p_0 \tau_r^{\frac{1}{k}} = 10 \cdot 1.8^{\frac{1}{0.286}} = 78.1 \cdot kPa$$

### Diffusore

$$p_{t2} = p_{t0} \pi_d = 78.1 \cdot 0.9 = 70.3 \cdot kPa$$

### Compressore

$$\tau_c = \pi_c^{\frac{k}{\gamma_c}} = 13^{\frac{0.286}{0.90}} = 2.26 \quad p_{t3} = p_{t2} \pi_c = 70.3 \cdot 13 = 914 \cdot kPa$$

$$T_{t3} = T_{t2} \tau_c = 401 \cdot 2.26 = 906 \cdot K$$

### Camera di Combustione

$$\tau_\lambda = \frac{c_{pt} T_{t4}}{c_p T_0} = \frac{1152 \cdot 1600}{1004 \cdot 223} = 8.23$$

$$f = \frac{\tau_\lambda - \tau_c \tau_r}{Q_R \eta_b / (c_p T_0) - \tau_\lambda} = \frac{8.23 - 2.26 \cdot 1.8}{\frac{42.0 \cdot 10^6 \cdot 0.98}{1004 \cdot 223} - 8.23} = 0.0237$$

$$\tau_b = \frac{\tau_\lambda}{\tau_c \tau_r} = \frac{8.23}{2.26 \cdot 1.8} = 2.02$$

$$p_{t4} = p_{t3} \pi_b = 914 \cdot 0.95 = 868 \cdot kPa$$

## Fan

$$\tau_f = \pi_f^{\frac{k}{\gamma}} = 1.90^{\frac{0.286}{0.90}} = 1.226 \quad p_{t13} = p_{t2} \pi_f = 70.3 \cdot 1.90 = 133.6 \cdot kPa$$

$$T_{t13} = T_{t2} \tau_f = 401 \cdot 1.226 = 492 \cdot K$$

## Turbina

$$\pi_t = \frac{\pi_f \pi_c}{\pi_b \pi_c} = \frac{0.99 \cdot 1.90}{0.95 \cdot 13} = 0.1523 \quad \tau_t = \pi_t^{k_t e_t} = 0.1523^{0.2481 \cdot 0.8} = 0.688$$

$$p_{t5} = p_{t4} \pi_t = 868 \cdot 0.1523 = 132.6 \cdot kPa \quad T_{t5} = T_{t4} \tau_t = 1600 \cdot 0.688 = 1101 \cdot K$$

## Mixer

$$\alpha = \frac{\eta_m (1+f)(1-\tau_t) \tau_\lambda - \tau_r (\tau_c - 1)}{\tau_r (\tau_f - 1)} = \frac{0.95 \cdot 1.02374 (1 - 0.688) 8.23 - 1.8 (2.26 - 1)}{1.8 (1.226 - 1)} = 0.563$$

$$\tau_M = \frac{\frac{\alpha \tau_f \tau_r}{\tau_t \tau_\lambda} + (1+f)}{1 + \alpha + f} = \frac{0.563 \frac{1.226 \cdot 1.8}{0.688 \cdot 8.23} + 1.024}{1.024 + 0.563} = 0.783$$

$$p_{t6} = p_{t5} \pi_M = 132.6 \cdot 0.9709 = 128.4 \cdot kPa \quad T_{t6} \sim T_{t5} \tau_M = 1101 \cdot 0.783 = 862 \cdot K$$

## Post Bruciatore

$$\tau_{\lambda AB} \frac{c_{p9} T_{t7}}{c_p T_0} = \frac{1241 \cdot 2000}{1004 \cdot 223} = 11.09$$

$$f_{AB} = \left(1 + \frac{f}{1 + \alpha}\right) \frac{\tau_{\lambda AB} - \tau_M \tau_t \tau_\lambda}{\frac{Q_{R,AB} \eta_{AB}}{c_p T_0} - \tau_{\lambda,AB}} = \left(1 + \frac{0.0237}{1.565}\right) \frac{11.09 - 0.783 \cdot 0.688 \cdot 8.23}{\frac{42 \cdot 10^6 \cdot 0.98}{1004 \cdot 223} - 11.09} = 0.0391$$

$$p_{t7} = p_{t6} \cdot \pi_{Ab} = 128.4 \cdot 0.92 = 118.1 \cdot kPa$$

$$f_{tot} = \frac{f}{1 + \alpha} + f_{AB} = \frac{0.0237}{1.563} + 0.0391 = 0.0543$$

## Ugello

$$p_{t9} = p_{t7} \pi_n = 118.1 \cdot 0.95 = 112.2 \cdot kPa \quad T_{t9} = T_{t7} = 2000 \cdot K$$

$$\frac{p_{t9}}{p_9} = \frac{p_{t9} p_0}{p_0 p_9} = \frac{112.2}{10} \frac{1}{3.8} = 2.95 \quad \frac{T_{t9}}{T_9} = \left(\frac{p_{t9}}{p_9}\right)^{k_9} = 2.95^{0.231} = 1.284$$

$$M_9 = \sqrt{\frac{2}{\gamma_9 - 1} \left[ \left(\frac{p_{t9}}{p_9}\right)^{k_9} - 1 \right]} = \sqrt{\frac{2}{0.3} (1.284 - 1)} = 1.376$$

$$T_9 = \frac{T_9}{T_{t9}} T_{t9} = \frac{2000}{1.284} = 1558 \cdot K \quad a_9 = \sqrt{\gamma_9 R_9 T_9} = \sqrt{1.3 \cdot 287 \cdot 1558} = 762 \cdot \frac{m}{s}$$

$$V_9 = M_9 a_9 = 1.378 \cdot 762 = 1049 \cdot \frac{m}{s}$$

$$V_{9,e} = V_9 \left( 1 + \frac{1 - \frac{p_0}{p_9}}{\gamma_9 M_9^2} \right) = 1049 \left( 1 + \frac{1 - \frac{1}{3.8}}{1.3 \cdot 1.378^2} \right) = 1363 \cdot \frac{m}{s}$$

$$\frac{V_{9,e}}{a_0} = \frac{1363}{299} = 4.56$$

## Spinta e rendimenti

$$\frac{F_u}{\dot{m}_{air} a_0} = (1 + f_{tot}) \frac{V_{9,e}}{a_0} - M_0 = 1.054 \cdot 4.56 - 2 = 2.81$$

$$TSFC = \frac{\dot{m}_{f_{tot}}}{F_u} = \frac{\dot{m}_f / \dot{m}_{air}}{\frac{F_u}{\dot{m}_{air} a_0}} = \frac{f_{tot}}{\frac{F_u}{\dot{m}_{air} a_0}} = \frac{0.0543}{2.81 \cdot 299} = 6.46 \cdot 10^{-5} \cdot \frac{kg}{sN}$$

$$\eta_{th} = \frac{\Delta K \dot{E}}{\mathcal{P}_t} = \frac{a_0^2 \left[ (1 + f_{tot}) \left( \frac{V_{9,e}}{a_0} \right)^2 - M_0^2 \right]}{2 f_{tot} Q_R} = \frac{B}{2 f_{tot} Q_R}$$

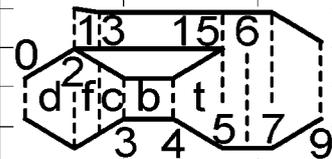
$$\eta_p = \frac{F_u V_0}{\Delta K \dot{E}} = \frac{\frac{2 F_u V_0}{\dot{m}_{air}}}{a_0^2 \left[ (1 + f_{tot}) \left( \frac{V_{9,e}}{a_0} \right)^2 - M_0^2 \right]} = \frac{\frac{2 F_u a_0 V_0}{\dot{m}_{air} a_0}}{B}$$

$$B = a_0^2 \left[ (1 + f_{tot}) \left( \frac{V_{9,e}}{a_0} \right)^2 - M_0^2 \right] = 299^2 [1.054 \cdot 4.56^2 - 2^2] = 1.602 \cdot 10^6 \cdot \frac{m^2}{s^2}$$

$$\eta_{th} = \frac{B}{2 f_{tot} Q_R} = \frac{1.602 \cdot 10^6}{2 \cdot 0.0543 \cdot 42.0 \cdot 10^6} = 35.1\%$$

$$\eta_p = \frac{2 V_0 a_0 \frac{F_u}{\dot{m}_{air} a_0}}{B} = \frac{2 \cdot 598 \cdot 299 \cdot 2.81}{1.602 \cdot 10^6} = 62.7\% \quad \eta_0 = \eta_{th} \eta_p = 0.351 \cdot 0.627 = 22\%$$

| Section | c       | f       | t       | $\lambda$ | M       | $\lambda_{AB}$ |         |           |         |
|---------|---------|---------|---------|-----------|---------|----------------|---------|-----------|---------|
| $\tau$  | 2.258   | 1.2260  | 0.6883  | 8.233     | 0.78147 | 11.0857        |         |           |         |
| Section | 0       | 2       | 3       | 4         | 5       | 6              | 7       | 9         | 13      |
| Tt      | 401.4   | 401.4   | 906.2   | 1600      | 1101.27 | 860.61         | 2000    | 2000      | 492.12  |
| pt      | 78,244  | 70,420  | 915,461 | 869,688   | 132,460 | 128,606        | 118,317 | 112,401   | 133,798 |
| $\pi_t$ | 0.15231 | f       | 0.02374 | $\alpha$  | 0.5707  | $f_{AB}$       | 0.03912 | $f_{tot}$ | 0.05424 |
| Pt9/p9  | M9      | M9 Eff  | Tt9/T9  | P9        | po/p9   |                |         |           |         |
|         | 2.958   | 1.377   | 1.377   | 1.28437   | 38000   | 0.26316        |         |           |         |
| T9      | a9      | V9      | V9/a0   | V9/a0 eff | F/ma0   | F/maira0       |         |           |         |
|         | 1557.19 | 761.407 | 1048.36 | 3.50318   | 4.551   | 4.39376        | 2.79736 |           |         |
| Num     | Section | t       | th      | p         |         | 0              | TSFC*e3 |           |         |
| 1.6E+06 | $\eta$  | 0.83551 | 0.3505  | 0.6275    | 0.21996 | 0.06479        |         | 64.787    |         |



## Farokhi Example 4.38

|         |      |      |      |        |       |       |        |
|---------|------|------|------|--------|-------|-------|--------|
|         | 2    | 3    | 4    | 4.5    | 5     | 9     |        |
|         | diff | comp | CC   | Tur    | Tur   | No    | Prop   |
| cp      | 1004 |      |      | 1152   | J/kgK |       |        |
| g       | 1.4  |      |      | 1.33   |       |       |        |
| p       | 0.99 | 35   | 0.96 |        |       |       |        |
| h, ec,t |      | 0.92 | 0.99 | 0.8    | 0.859 | 0.95  | 0.85   |
| Tt      |      |      |      | 1650   |       |       |        |
| M0      | 0.82 |      |      |        | QR    | 42000 | kJ/kgK |
| T0      | 258  | K    | p0   | 30,000 | Pa    |       |        |
| alpha   | 0.75 | m0   | 50   | kg/s   |       |       |        |

$$k = \frac{\gamma - 1}{\gamma} = \frac{0.4}{1.4} = 0.286 \quad k_5 = \frac{\gamma_5 - 1}{\gamma_5} = \frac{0.33}{1.33} = 0.248$$

$$R = kc_p = 0.286 \cdot 1004 = 287 \text{ J/kgK} \quad R_5 = 0.248 \cdot 1152 = 286 \text{ J/kgK}$$

$$a_0 = \sqrt{\gamma RT_0} = 1.4 \cdot 287 \cdot 258 = 322 \text{ m/s}$$

$$V_0 = M_0 \cdot a_0 = 0.82 \cdot 322 = 264 \text{ m/s}$$

### Effetto Ram

$$\tau_r = \psi_0 = 1 + \frac{\gamma - 1}{2} M_0^2 = 1 + 0.2 \cdot 0.82^2 = 1.134$$

$$T_{t0} = T_0 \tau_r = 258 \cdot 1.134 = 293 \text{ K} \quad p_{t0} = \tau_r^{\frac{1}{k}} p_0 = 1.134^{\frac{1}{0.286}} 30.0 \cdot 10^3 = 46.6 \text{ kPa}$$

### Diffusore

$$p_{t2} = p_{t0} \pi_d = 46.6 \cdot 0.99 \cdot 10^3 = 46.1 \text{ kPa} \quad T_{t0} = T_{t2}$$

### Compressore

$$\tau_c = \pi_c^{\frac{k}{\gamma}} = 35^{\frac{0.286}{0.92}} = 3.02$$

$$p_{t3} = p_{t2} \pi_c = 46.1 \cdot 35 \cdot 10^3 = 1614 \text{ kPa} \quad T_{t3} = T_{t2} \tau_c = 293 \cdot 3.02 = 885 \text{ K}$$

### Camera di combustione

$$p_{t4} = p_{t3} \pi_b = 1614 \cdot 0.96 = 1549 \text{ kPa} \quad \tau_\lambda = \frac{c_{p5} T_{t4}}{c_p T_0} = \frac{1152 \cdot 1650}{258 \cdot 1004} = 7.34$$

$$f = \frac{\tau_\lambda - \tau_c \tau_r}{Q_R \eta_b / (c_p T_0) - \tau_\lambda} = \frac{7.34 - 3.02 \cdot 1.134}{42.0 \cdot 10^6 \cdot 0.99 / (258 \cdot 1004) - 7.34} = 0.0256$$

### Turbina HP

$$\tau_{tH} = 1 - \frac{\tau_r (\tau_c - 1)}{\eta_{mH} (1 + f) \tau_\lambda} = 1 - \frac{1.134 (3.02)}{0.99 \cdot 1.026 \cdot 7.34} = 0.693$$

$$\pi_{tH} = \tau_{tH}^{\frac{1}{k_5 e_{tH}}} = 0.693^{\frac{1}{0.248 \cdot 0.800}} = 0.1575$$

$$p_{t45} = p_{t4} \pi_{tH} = 1549 \cdot 0.1575 \cdot 10^3 = 244 \cdot kPa \quad T_{t45} = T_{t4} \tau_{tH} = 1650 \cdot 0.693 = 1143 \cdot K$$

## Turbina LP

Supponendo funzionamento corretto nell'ugello:  $\frac{p_9}{p_0} = 1$

$$\tau_{tL} = 1 - \eta_{tL} \alpha_p \left[ 1 - \left( \frac{p_0}{p_{t45}} \right)^{k_5} \right] = 1 - \eta_{tL} 0.75 \left[ 1 - \left( \frac{30}{244} \right)^{0.248} \right]$$

$$\tau_{tL} = 1 - \eta_{tL} 0.75 [1 - 0.594] = 1 - \eta_{tL} 0.304$$

$$\text{Supponendo } \eta_{tL} = 1 \rightarrow \tau_{tL} = 0.696 \quad \eta_{tL} = \frac{1 - \tau_{tL}}{1 - \tau_{tL}^{\frac{1}{e_{tL}}}} = \frac{1 - 0.696}{1 - 0.696^{0.859}} = 0.883$$

Iterando si ha in sequenza:  $\tau_{tL} = 0.732$ ,  $\eta_{tL} = 0.880$ ,  $\tau_{tL} = 0.733$ ,

$$\pi_{tL} = \tau_{tL}^{\frac{1}{k_5 e_{tL}}} = 0.732^{\frac{1}{0.248 \cdot 0.859}} = 0.233$$

$$p_{t5} = p_{t45} \pi_{tL} = 244 \cdot 0.233 \cdot 10^3 = 56.9 \cdot kPa \quad T_{t5} = T_{t45} \tau_{tL} = 1143 \cdot 0.732 = 838 \cdot K$$

## Ugello

$$\eta_n = \frac{\left( \frac{p_{t5}}{p_9} \right)^{k_5} - \pi_n^{-k_5}}{\left( \frac{p_{t5}}{p_9} \right)^{k_5} - 1} \rightarrow \pi_n = \left\{ \left( \frac{p_{t5}}{p_9} \right)^{k_5} - \eta_n \left[ \left( \frac{p_{t5}}{p_9} \right)^{k_5} - 1 \right] \right\}^{-\frac{1}{k_5}}$$

$$\left( \frac{p_{t5}}{p_9} \right)^{k_5} = \left( \frac{p_{t5}}{p_0} \right)^{k_5} = \left( \frac{56.9}{30} \right)^{0.248} = 1.172$$

$$\pi_n = \{ 1.169 - 0.95 [1.169 - 1] \}^{-\frac{1}{0.248}} = 0.966$$

$$p_{t9} = p_{t5} \pi_n = 56.9 \cdot 0.966 \cdot 10^3 = 55.0 \cdot kPa \quad \frac{p_{t9}}{p_9} = \frac{55.0}{30} = 1.833$$

$$\psi_9 = \left( \frac{p_{t9}}{p_9} \right)^{k_5} = 1.833^{0.248} = 1.162 \quad M_9 = \sqrt{\frac{2}{\gamma_5 - 1} [\psi_9 - 1]} = \sqrt{\frac{2}{.33} [1.160 - 1]} = 0.991$$

$$M_9 < 1 \rightarrow p_9 = p_0 \text{ (OK)}$$

$$T_9 = T_{t9} / \psi_9 = T_{t5} / \psi_9 = 837 / 1.162 = 721 \cdot K$$

$$a_9 = \sqrt{\gamma_5 R_5 T_9} = 1.33 \cdot 286 \cdot 721 = 524 \cdot m/s$$

$$V_9 = M_9 \cdot a_9 = 0.991 \cdot 524 = 519 \cdot m/s \quad \frac{V_9}{a_0} = \frac{519}{322} = 1.612 > M_0 \text{ (OK)}$$

## Propeller

$$\frac{\mathcal{P}_s}{\dot{m}_0} = (1 + f) \eta_{gb} \eta_{m_{tL}} (1 - \tau_{tL}) c_{p5} T_{t45} =$$

$$\frac{\mathcal{P}_s}{\dot{m}_0} = 1.026 \cdot 0.995 \cdot 0.99 \cdot (1 - 0.733) \cdot 1152 \cdot 1143 = 355 \cdot \frac{kJ}{kg}$$

## Spinta

$$\frac{F_{u.c}}{\dot{m}_0 a_0} = (1 + f) \frac{V_{9.e}}{a_0} - M_0 = 1.026 \cdot 1.612 - 0.82 = 0.833$$

$$\frac{F_{u.p}}{\dot{m}_0 a_0} = \frac{\eta_{prop} \mathcal{P}_s}{\dot{m}_0 V_0 a_0} = \frac{0.85 \cdot 355}{264 \cdot 322} 10^3 = 3.55$$

$$\frac{F_u}{\dot{m}_0 a_0} = \left( \frac{F_{u.c}}{\dot{m}_0 a_0} + \frac{F_{u.o}}{\dot{m}_0 a_0} \right) = 0.824 + 3.57 = 4.38$$

$$TSFC = \frac{f}{F_u/\dot{m}_0} = \frac{0.0256 \cdot 10^3}{4.38 \cdot 322} = 0.01815 \cdot \frac{g}{s} \frac{1}{N}$$

$$\eta_{th} = \frac{a_0^2 [(1 + f) V_{9.e}^2 / a_0^2 - M_0^2] + 2 \mathcal{P}_s / \dot{m}_0}{2 f Q_R} =$$

$$\eta_{th} = \frac{322^2 [1.026 \cdot 1.612^2 - 0.82^2] + 2 \cdot 355 \cdot 10^3}{2 \cdot 0.0256 \cdot 42.0 \cdot 10^6} = \frac{9.17 \cdot 10^5}{2.15 \cdot 10^6} = 0.426$$

$$\eta_p = \frac{2 \frac{F_u}{\dot{m}_0 a_0} a_0 V_0}{a_0^2 [(1 + f) V_{9.e}^2 / a_0^2 - M_0^2] + 2 \mathcal{P}_s / \dot{m}_0} = \frac{2 \cdot 4.38 \cdot 264 \cdot 322}{9.17 \cdot 10^5} = 0.812$$

$$\eta_0 = \eta_{th} \eta_p = 0.424 \cdot 0.812 = 0.346$$

|   |             |         |             |           |             |          |             |        |
|---|-------------|---------|-------------|-----------|-------------|----------|-------------|--------|
| k   | 0.28571     |         |             | 0.24812   |             |          |             |        |
| R   | 286.857     |         |             | 285.835   | kJ/kgK      |          |             |        |
| a0  | 321.9       | m/s     | V0          | 263.9     | m/s         |          |             |        |
| $\tau_r = T_{t0} = 0$                           | 1.13448     |         |             |           |             |          |             |        |
| Section   | c           | tH      | tL          | $\lambda$ |             | tH       | tL          |        |
| $\tau$  | 3.01665     | 0.69292 | 0.73216     | 7.33809   | $\pi$       | 0.15754  | 0.23161     |        |
| Section   | 0           | 2       | 3           | 4         | 4.5         | 5        | 9           |        |
| Tt  | 292.7       | 292.696 | 883.0       | 1650      | 1143.32     | 837.102  | 837.102     |        |
| pt  | 46,656      | 46,190  | 1.62E+06    | 1.55E+06  | 244,499     | 56,629   | 54,722      |        |
| Core  |             | f       | 0.02556     |           |             |          |             |        |
| Pt9/p9  | M9          | M9 Eff  | Tt9/T9      | P9        | po/p9       |          |             |        |
|   | 1.82407     | 0.98729 | 1.16083     | 30000     | 1           |          |             |        |
| T9  | a9          | V9      | V9/a0       | V9/a0 eff | F/ma0       | Fc/Ft    |             |        |
|   | 721.122     | 523.585 | 516.931     | 1.60593   | 1.60593     | 0.82698  | 0.18828     |        |
| Prop  |             |         |             |           |             |          |             |        |
| PS/mo   |             |         |             |           | F/ma0       | FP/Ft    |             |        |
|   | 356,378     | J/kg    |             |           | 3.56535     | 0.81172  |             |        |
| Num   | Section     | t       | th          | p         | 0           | TSFC*1e3 | F/ma0       |        |
| 9.17E+05  | $\eta$      | 0.83491 | 0.42712     | 0.8138    | 0.34759     | 0.01808  | 4.39233     |        |
| Calcolo iterativo rendimento TL partendo da eTL |             |         |             |           |             |          |             |        |
| p9/pt45   | $\eta_{TL}$ | $\tau$  | $\eta_{TL}$ | $\tau$    | $\eta_{TL}$ | $\tau$   | $\eta_{TL}$ | $\tau$ |
|   | 0.1227      | 1       | 0.69564     | 0.88325   | 0.73117     | 0.88008  | 0.73214     | 0.88   |
|   |             | 0.88    | 0.73216     | 0.88      | 0.73216     | 0.88     | 0.73216     | 0.88   |
| Calcolo $\pi_n$ partendo da $\eta_n$            |             |         |             |           |             |          |             |        |
| Tt5/T0  | 1.17074     | $\pi_n$ | 0.96632     |           |             |          |             |        |