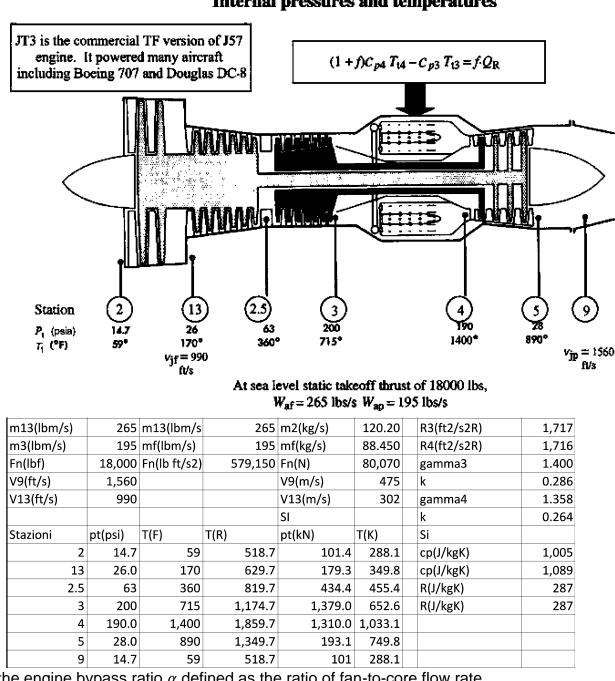
# Farokhi problem 3.2

The total pressures and temperatures of the gas are specified for a turbofan engine with separate exhaust streams (JT3D-3B from Pratt & Whitney, 1974). The mass flow rates in the engine core (or primary) and the engine fan are also specified for the sea level static operation. Calculate:



JT3D-3B Turbofan **Internal pressures and temperatures** 

a) the engine bypass ratio  $\alpha$  defined as the ratio of fan-to-core flow rate

$$\alpha = \frac{\dot{m}_{13}}{\dot{m}_3} = \frac{265}{195} = \frac{120}{88.5} = 1.36$$

b) from the total temperature rise across the burner, estimate the fuel-to-air ratio and the fuel flow rate in lbm/h, assuming the fuel heating value is  $Q_R \sim 18,600 \cdot BTU/lbm$  and the

specific heat at constant pressure is 0.24 and 0.26 *BTU/lbm*·R at the entrance and exit of the burner, respectively

$$\begin{split} \dot{m}_4 c_{p4} T_{t4} &- \dot{m}_3 c_{p3} T_{t3} = \eta_b \dot{m}_f Q_R & (1+f) c_{p4} T_{t4} - c_{p3} T_{t3} = \eta_b f Q_R \\ f &= \frac{c_{p4} T_{t4} - c_{p3} T_{t3}}{\eta_b Q_R - c_{p4} T_{t4}} = \frac{0.26 \cdot 1860 - 0.24 \cdot 1175}{1 \cdot 18.6 \cdot 10^3 - 0.26 \cdot 1860} = 0.0111 \\ \dot{m}_f &= f \dot{m}_3 = 0.0111 \cdot 195 = 2.17 \cdot \frac{lbm}{s} \end{split}$$

c) the engine static thrust based on the exhaust velocities and the mass flow rates assuming perfectly expanded nozzles and compare your answer to the specified thrust of 18,000 lbf

$$F = \dot{m}_4 V_9 + \dot{m}_{13} V_{13} = (195 + 2.17)1560 + 265 \cdot 990 = 570 \cdot 10^3 lbm \cdot \frac{ft}{s^2} = \frac{570}{32.18} \cdot 10^3 \cdot lbf$$
  
= 17.7 \cdot 10^3 \cdot lbf

d) the engine thermal efficiency  $\eta_{th}$ 

$$\eta_{th} = \frac{\dot{m}_4 V_9^2 + \dot{m}_{13} V_{13}^2}{2\dot{m}_f Q_R} = \frac{(195 + 2.17)1560^2 + 265 \cdot 990^2}{2 \cdot 2.17 \cdot 465.7 \cdot 10^6} = \frac{7.40 \cdot 10^8}{20.21 \cdot 10^8} = 36.6\%$$

e) the thermal efficiency of this engine compared to the afterburning turbojet of Problem 1. Explain the major contributors to the differences in  $\eta_{th}$  in these two engines

$$\pi_c = 13.6$$
  $\pi_{c.3.1} = 10.8$ 

f) the engine thrust specific fuel consumption in lbm/h/lbf

$$TSFC = \frac{\dot{m}_f}{F} = \frac{2.17 \cdot 3600}{17.7 \cdot 10^3} = 0.441 \frac{lbm}{h \cdot lbf}$$

g) the nondimensional engine specific thrust

$$\frac{F}{\dot{m}_{air}a_0} = \frac{570 \cdot 10^3}{(265 + 195)\sqrt{1.4 \cdot 1717 \cdot 519}} = 1.11$$

h) the Carnot efficiency corresponding to this engine

$$\eta_{Carnot} = 1 - \frac{T_0}{T_{t4}} = 72.1\%$$

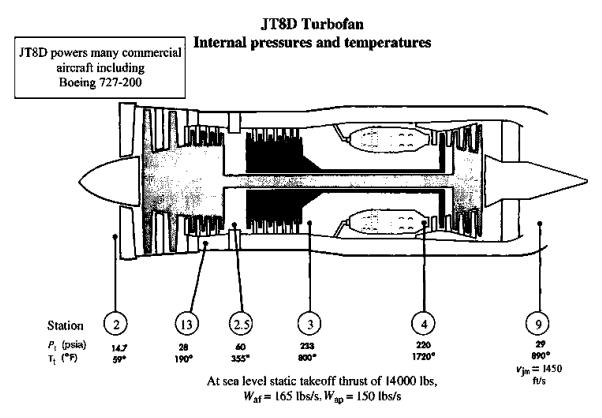
i) the engine overall pressure ratio  $p_{t3}/p_{t2}$  $\pi_c = 13.6$ 

j) fan nozzle exit Mach number (use  $T_t = T + V^2/2c_p$  to calculate local static temperature at the nozzle exit, then local speed of sound.

$$T_t = T + V^2/2 \quad \rightarrow \quad T_{13} = T_{t13} - \frac{V_{13}^2}{2c_p} = 630 - \frac{990^2}{2 \cdot 0.24 \cdot 25 \cdot 10^3} = 548R$$
$$M_{13} = \frac{V_{13}}{a_{13}} = \frac{990}{\sqrt{1.4 \cdot 1717 \cdot 548}} = 0.863$$

				SI		
α	1.359			α	1.359	
f	0.011			f	0.011	
$\pi_{ ext{Fan}}$	1.769			$\pi_{ ext{cLP}}$	1.769	
$\pi_{c}$	7.692			$\pi_{ m cHP}$	7.692	
$\pi_{t}$	0.147			$\pi_{t}$	0.147	
mf	2.170			mf	0.984	
F(lb ft/s2)	569,935	Fn(lbf)	17,714	F(N)	78,796	
$\eta_{ ext{th}}$	0.366			$\eta_{ ext{th}}$	0.366	
TSFC(lbm/h lb	0.441	0.434		TSFC(mg/s N)	12.491	
$\eta_{carnot}$	0.721			$\eta_{carnot}$	0.721	
ао	1,117			ао	340	
ST/ao	1.110			ST/ao	1.110	
$\pi_{ m tot}$	13.6			$\pi_{ m tot}$	14	
T13(R)	548			T13	305	
a13(m/s)	1,148			a13	350	
M13	0.863			M13	0.863	

# Farokhi problem 3.3



A mixed exhaust turbofan engine (JT8D from Pratt and Whitney, 1974) is described by its internal pressures and temperature, as well as air mass flow rates and the mixed jet (exhaust) velocity. Let us examine a few parameters for this engine, for a ballpark approximation.

JT8D	727, dc9	, md80					
Conversioni				Cost K-F	255.37		
g(ft/s2)	32.175	ft->m	0.3048	BTU->J	1,055	BTU/lbm->ft2/s2	25,038
1lb->kg	0.45359	lbft->kgm	0.1383	psi->Pa	6,895	Conv TSFC	115,830
Dati				Si			
QR(BTU/lbm)	18,600	QR(ft2/s2)	465,707,434	QR(kJ/kg)	43266	cp3(BTU/lbmR)	0.24
				SI		cp4(BTU/lbmR)	0.26
m13(lbm/s)	165	m13(lbm/s	165	m2(kg/s)	74.84	R3(ft2/s2R)	1,717
m3(lbm/s)	150	m3(lbm/s)	150	mf(kg/s)	68.039	R4(ft2/s2R)	1,716
Fn(lbf)	14,000	Fn(lb ft/s2)	450,450	Fn(N)	62,277	gamma3	1.400
V9(ft/s)	1,450			V9(m/s)	442	k	0.286
						gamma4	1.358
				SI		k	0.264
Stazioni	pt(psi)	T(F)	T(R)	pt(kN)	Т(К)	Si	
2	14.7	59	518.7	101.4	288.1	cp(J/kgK)	1,005
13	28.0	190	649.7	193.1	360.9	cp(J/kgK)	1,089
2.5	60	355	814.7	413.7	452.6	R(J/kgK)	287
3	233	800	1,259.7	1,606.5	699.8	R(J/kgK)	287
4	220.0	1,720	2,179.7	1,516.9	1,210.9		
9	29.0	890	1,349.7	200.0	749.8		

(a) Estimate the fuel flow rate from the total temperature rise across the burner assuming the fuel heating value  $Q_R \sim 18,600 \cdot BTU/lbm$  and the specific heat at constant pressure is 0.24 and 0.26 *BTU/lbm*·R at the entrance and exit of the burner, respectively

$$f = \frac{c_{p4}T_{t4} - c_{p3}T_{t3}}{\eta_b Q_R - c_{p4}T_{t4}} = \frac{0.26 \cdot 2180 - 0.24 \cdot 1260}{1 \cdot 18.6 \cdot 10^3 - 0.26 \cdot 2180} = 0.0147$$
$$\dot{m}_f = f\dot{m}_3 = 0.0147 \cdot 150 = 2.20 \cdot \frac{lbm}{s}$$

(b) Calculate the momentum thrust at the exhaust nozzle and compare it to the specified thrust of 14,000 lbf

$$F = (\dot{m}_3 + \dot{m}_f + \dot{m}_{13})V_9 = (150 + 2.20 + 165)1450 = 460 \cdot 10^3 lbm \cdot \frac{ft}{s^2} = \frac{460}{32.18} \cdot 10^3 \cdot lbf$$
  
= 14.3 \cdot 10^3 \cdot lbf

(c) Estimate the thermal efficiency of this engine and compare it to Problems 3.1 and 3.2 as well as a Carnot cycle operating between the temperature extremes of this engine. Explain the differences

$$\eta_{th} = \frac{(\dot{m}_3 + \dot{m}_f + \dot{m}_{13})V_9^2}{2\dot{m}_f Q_R} = \frac{(150 + 2.20 + 165)1450^2}{2 \cdot 2.20 \cdot 465.7 \cdot 10^6} = \frac{6.67 \cdot 10^8}{20.5 \cdot 10^8} = 32.6\%$$
  
$$\eta_{Carnot} = 1 - \frac{T_0}{T_{t4}} = 1 - \frac{519}{2,180} = 76.2\%$$

(d) Estimate the specific fuel consumption for this engine in lbm/h/lbf

$$TSFC = \frac{\dot{m}_f}{F} = \frac{2.20 \cdot 3600}{14.3 \cdot 10^3} = 0.554 \frac{lbm}{h \cdot lbf}$$

(e) The overall pressure ratio (of the fan–compressor section)  $p_{t3}/p_{t2}$ 

$$\frac{p_{t3}}{p_{t2}} = \frac{233}{14.7} = 15.9$$

(f) What is the bypass ratio  $\alpha$  for this engine at takeoff

$$\alpha = \frac{\dot{m}_{13}}{\dot{m}_3} = \frac{165}{150} = 1.10$$

(g) What is the Carnot efficiency corresponding to this engine

$$\eta_{Carnot} = 1 - \frac{T_0}{T_{t4}} = 1 - \frac{519}{1260} = 76.2\%$$

(h) Estimate nozzle exit Mach number [look at part (j in Problem 3.2]

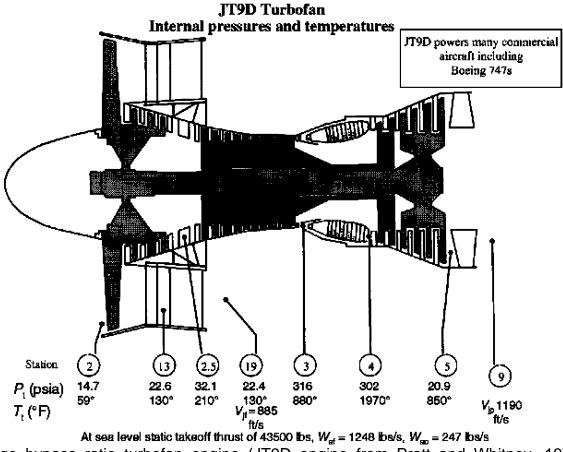
$$T_t = T + V^2/2 \quad \rightarrow \quad T_9 = T_{t9} - \frac{V_9^2}{2c_p} = 1350 - \frac{1450^2}{2 \cdot 0.26 \cdot 25 \cdot 10^3} = 1188 \cdot R$$
$$M_9 = \frac{V_9}{a_9} = \frac{1450}{\sqrt{1.4 \cdot 1716 \cdot 1188}} = 0.86$$

(i) What is the low-pressure compressor (LPC) pressure ratio  $p_{t25}/p_{t2}$ (j) What is the high-pressure compressor (HPC) pressure ratio  $p_{t3}/p_{t25}$ 

$$\frac{p_{t25}}{p_{t2}} = \frac{60}{14.7} = 4.08 \qquad \frac{p_{t3}}{p_{t25}} = \frac{233}{60} = 3.88$$

				SI		
α	1.100			α	1.100	
f	0.0147			f	0.0147	
$\pi_{ t LPC+Fan}$	4.082			$\pi_{ ext{cLP}}$	1.905	
$\pi_{c}$	3.883			$\pi_{ m cHP}$	8.321	
$\pi_{t}$	0.132			$\pi_{t}$	0.132	
mf	2.199			mf	0.998	
F(lb ft/s2)	459,939	Fn(lbf)	14,295	F(N)	63 <i>,</i> 588	
${\eta_{ ext{th}}}$	0.326			$\eta_{ ext{th}}$	0.156	
TSFC(lbm/h lb	0.554			TSFC(mg/s N)	15.687	
$\eta_{carnot}$	0.762			$\eta_{carnot}$	0.762	
ао	1,117			ао	340	
ST/ao	1.308			ST/ao	1.308	
$\pi_{ m tot}$	16			$\pi_{ m tot}$	16	
T9(R)	1,188			T13	660	
a9(ft/s)	1,664			a13	515	
M9	0.871			M13	0.858	

# Farokhi problem 3.4



At see level static takeoff thrust of 43500 lbs,  $W_{sf} = 1248$  lbs/s,  $W_{sc} = 247$  lbs/s A large bypass ratio turbofan engine (JT9D engine from Pratt and Whitney, 1974) is described by its fan and core engine gas flow properties.

, ,		0 0				
747, A310,	767					
			Cost K-F	255.37		
32.175	ft->m	0.3048	BTU->J	1,055	BTU/lbm->ft2/s2	25,038
0.45359	lbft->kgm	0.1383	psi->Pa	6,895	Conv TSFC	115,830
			Si			
18,600	QR(ft2/s2)	465,707,434	QR(kJ/kg)	43266	cp3(BTU/lbmR)	0.24
			SI		cp4(BTU/lbmR)	0.26
1,248	m13(lbm/s	1,248	m2(kg/s)	566.08	R3(ft2/s2R)	1,717
247	mf(lbm/s)	247	m3(kg/s)	112.037	R4(ft2/s2R)	1,716
43,500	Fn(lb ft/s2)	1,399,613	Fn(N)	193,502	gamma3	1.400
1,190			V9(m/s)	363	k	0.286
885			V19(m/s)	270	gamma4	1.358
			SI		k	0.264
pt(psi)	T(F)	T(R)	pt(kN)	Т(К)	Si	
14.7	59	518.7	101.4	288.1	cp(J/kgK)	1,005
22.6	130	589.7	155.8	327.6	cp(J/kgK)	1,089
32	210	669.7	221.3	372.0	R(J/kgK)	287
316	880	1,339.7	2,178.8	744.3	R(J/kgK)	287
302.0	1,970	2,429.7	2,082.3	1,349.8		
20.9	850	1,309.7	144.1	727.6		
14.7	850	1,309.7	101	727.6		
22.4	130	589.7	154	327.6		
	32.175 0.45359 18,600 1,248 247 43,500 1,190 885 pt(psi) 14.7 22.6 32 316 302.0 20.9 14.7	247     mf(lbm/s)       43,500     Fn(lb ft/s2)       1,190        885        pt(psi)     T(F)       14.7     59       22.6     130       316     880       302.0     1,970       20.9     850       14.7     850	32.175         ft->m         0.3048           0.45359         lbft->kgm         0.1383           18,600         QR(ft2/s2)         465,707,434           18,600         QR(ft2/s2)         465,707,434           11,248         m13(lbm/s)         1,248           247         mf(lbm/s)         247           43,500         Fn(lb ft/s2)         1,399,613           1,190         1,399,613         1,190           885         1,399,613         1,190           pt(psi)         T(F)         T(R)           14.7         59         518.7           22.6         130         589.7           32         210         669.7           316         880         1,339.7           302.0         1,970         2,429.7           20.9         850         1,309.7           14.7         850         1,309.7	Image         Image <thimage< th=""> <thi< td=""><td>Image         Image         <th< td=""><td>Image: system in the system in the</td></th<></td></thi<></thimage<>	Image         Image <th< td=""><td>Image: system in the system in the</td></th<>	Image: system in the

(a) What is the overall pressure ratio (OPR) of this engine

$$\pi_c = \frac{p_{t3}}{p_{t2}} = \frac{316}{14.7} = 21.5$$

(b) Estimate the fan gross thrust Fg,fan in lbf

$$F_{Fan} = \dot{m}_{19}V_{19} = 1248 \cdot 885 = 1.10 \cdot 10^6 lbm \cdot \frac{ft}{s^2} = \frac{1.10}{32.18} \cdot 10^6 \cdot lbf = 34.3 \cdot 10^3 \cdot lbf$$

(c) Estimate the fuel-to-air ratio based on the energy balance across the burner, assuming the fuel heating value is  $Q_R \sim 18,600 \cdot BTU/lbm$  and the specific heat at constant pressure is 0.24 and 0.26 *BTU/lbm*·R at the entrance and exit of the burner, respectively

$$f = \frac{c_{p4}T_{t4} - c_{p3}T_{t3}}{\eta_b Q_R - c_{p4}T_{t4}} = \frac{0.26 \cdot 2430 - 0.24 \cdot 1340}{1 \cdot 18.6 \cdot 10^3 - 0.26 \cdot 2430} = 0.0172$$
$$\dot{m}_f = f\dot{m}_3 = 0.0172 \cdot 247 = 4.25 \cdot \frac{lbm}{s}$$

(d) Calculate the core gross thrust and compare the sum of the fan and the core thrusts to the specified engine thrust of 43,500 lbf

$$F_{Core} = \dot{m}_9 V_9 = (4.25 + 247) \cdot 1190 = 0.299 \cdot 10^6 lbm \cdot \frac{ft}{s^2} = \frac{.299}{32.18} \cdot 10^6 \cdot lbf$$
$$= 9.29 \cdot 10^3 \cdot lbf$$

$$F_{Tot} = F_{Core} + F_{Fan} = (9.29 + 34.3)10^3 = 43.6 \cdot 10^3 \cdot lbf$$
  $\frac{F_{Core}}{F_{Tot}} = \frac{9.29}{43.6} = 21.3\%$ 

(e) Calculate the engine thermal efficiency and compare it to Problems 3.1–3.3. Explain the differences

$$\eta_{th} = \frac{\left(\dot{m}_3 + \dot{m}_f\right)V_9^2 + \dot{m}_{19}V_{19}^2}{2\dot{m}_f Q_R} = \frac{(4.25 + 247) \cdot 1190^2 + 1248 \cdot 885^2}{2 \cdot 4.25 \cdot 465.7 \cdot 10^6} = \frac{13.3 \cdot 10^8}{39.7 \cdot 10^8} = 33.5\%$$

(f) Estimate the thrust-specific fuel consumption (TSFC), in lbm/h/lbf

$$TSFC = \frac{\dot{m}_f}{F} = \frac{4.25 \cdot 3600}{43.6 \cdot 10^3} = 0.352 \frac{lbm}{h \cdot lbf}$$

(g) What is the bypass ratio of this turbofan engine

$$\alpha = \frac{\dot{m}_{19}}{\dot{m}_3} = \frac{1248}{247} = 5.05$$

(h) What is the Carnot efficiency  $\eta$  Carnot corresponding to this engine

$$\eta_{Carnot} = 1 - \frac{T_0}{T_{t4}} = 1 - \frac{519}{2,430} = 78.6\%$$

(i) What is the LPC pressure ratio  $p_{t25}/p_{t2}$ (j) What is the HPC pressure ratio  $p_{t3}/p_{t25}$ 

$$\pi_{cLP} = \frac{p_{t25}}{p_{t2}} = \frac{32}{14.7} = 2.18$$
  $\pi_{cHP} = \frac{p_{t3}}{p_{t25}} = \frac{316}{32} = 9.88$   $\pi_c = 21.5$ 

(k) Estimate the fan nozzle exit Mach number [see part (j) in Problem 3.2]

$$T_t = T + V^2/2 \quad \rightarrow \quad T_{19} = T_{t19} - \frac{V_{19}^2}{2c_p} = 590 - \frac{885^2}{2 \cdot 0.24 \cdot 25 \cdot 10^3} = 525 \cdot R$$
$$M_{19} = \frac{V_{19}}{a_{19}} = \frac{885}{\sqrt{1.4 \cdot 1717 \cdot 525}} = 0.788$$

(I) Estimate the primary nozzle exit Mach number

$$T_t = T + V^2/2 \quad \rightarrow \quad T_9 = T_{t9} - \frac{V_9^2}{2c_p} = 1310 - \frac{1190^2}{2 \cdot 0.26 \cdot 25 \cdot 10^3} = 1201 \cdot R$$
$$M_{19} = \frac{V_{19}}{a_{19}} = \frac{1190}{\sqrt{1.4 \cdot 1716 \cdot 1201}} = 0.71$$

Valutare inoltre il lavoro nei vari stadi del compressore, nella turbina e il calore scambiato nella camera di combustione.

$$\begin{split} W_{cLP} &= \dot{m}_3 c_p (T_{t25} - T_{t2}) = 247 \cdot 0.24(670 - 519) = 8,950 \cdot \frac{BTU}{lbmR} = 9,444 \cdot kW \\ W_{cHP} &= \dot{m}_3 c_p (T_{t3} - T_{t25}) = 247 \cdot 0.24(1340 - 670) = 39.7 \cdot 10^3 \cdot \frac{BTU}{lbmR} = 41.9 \cdot 10^3 \cdot kW \\ W_F &= \dot{m}_{13} c_p (T_{t19} - T_{t2}) = 1248 \cdot 0.24(590 - 519) = 21,230 \cdot \frac{BTU}{lbmR} = 22,400 \cdot kW \\ W_{tot} &= W_c + W_F = 9.444 + 41.9 + 22.4 = 73.8 \cdot MW \\ W_t &= \dot{m}_4 c_{p_4} (T_{t5} - T_{t4}) = (247 + 4.25) \cdot 0.26(1310 - 2430) = 73,200 \cdot \frac{BTU}{lbmR} = 77.2 \cdot MW \\ \Delta Q_{cc} &= \dot{m}_4 c_{p_4} T_{t4} - \dot{m}_3 c_p T_{t3} = (247 + 4.25) \cdot 0.26 \cdot 2430 - 247 \cdot 0.24 \cdot 1340 = \\ &= 79,300 \cdot \frac{BTU}{lbmR} = 83.7 \cdot MW \end{split}$$

				SI		
α	5.053			α	5.053	
f	0.017			f	0.017	
$\pi_{ t LPC}$	2.184			$\pi_{ ext{cLP}}$	2.184	
$\pi_{cHP}$	9.844			$\pi_{ m cHP}$	9.844	
$\pi_{t}$	0.069			$\pi_{t}$	0.069	
mf	4.264			mf	1.934	
F <sub>Fan</sub> (lb ft/s2)	1,104,480	Fn(lbf)	34,327	F <sub>Fan</sub> (N)	152,699	
F <sub>main</sub> (lb ft/s2)	299,004	Fn(lbf)	9,293	F <sub>main</sub> (N)	41,339	
F(lb ft/s2)	1,403,484	Fn(lbf)	43,620	F(N)	194,038	
$\eta_{th}$	0.336			$\eta_{ ext{th}}$	0.336	
TSFC(lbm/h lb	0.352			TSFC(mg/s N)	9.968	
$\eta_{carnot}$	0.787			$\eta_{carnot}$	0.787	
ао	1,117			ао	340	
ST/ao	0.841			ST/ao	0.841	
$\pi_{ m tot}$	21.5			$\pi_{tot}$	21	
T19(R)	525			T19	291	
a19(ft/s)	1,123			a19	342	
M19	0.788			M19	0.788	
T9(R)	1,201			Т9	667	
a9(ft/s)	1,673			a9	510	
M9	0.711			M9	0.711	

# J79D by Tom

JT9d By T	om							নির	19
	2	3	4	5	9	13	19		<u> </u>
	diff	comp	CC	Tur	No	Fan	No FAn	[dfc]]	o[tĭn]
c <sub>p</sub>	1004			1057				$\sqrt{3}$	4
γ	1.4			1.35					
$\pi$	1	21.5	0.955		0.98	1.53	0.99		
η, e <sub>c,t</sub>		0.92	0.95	0.9		0.96			
Tt				1349.8					
M0	0				QR	42800	kJ/kgK		
то	288	К	p0	101,300	Ра	$\eta_m$	0.98		
alpha	5.053								
k	0.28571			0.25926					
R	286.857			274.037	kJ/kgK				
a0	340.1	m/s	V0	0.0	m/s				

$$k = \frac{\gamma - 1}{\gamma} = \frac{1.4 - 1}{1.4} = 0.2857 \qquad k_t = \frac{\gamma_t - 1}{\gamma_t} = \frac{1.35 - 1}{1.35} = 0.2593$$
$$R = kc_p = 1004 \cdot 0.2857 = 287 \cdot \frac{J}{kg \cdot K}$$
$$R_t = k_t c_{pt} = 1057 \cdot 0.2593 \frac{J}{kg \cdot K} = 274 \cdot \frac{J}{kg \cdot K}$$

## **Effetto Ram**

$$a_0 = \sqrt{\gamma R T_0} = \sqrt{1.4 \cdot 287 \cdot 288} = 340 \cdot \frac{m}{s} \qquad V_0 = M_0 a_0 = 0 \cdot 340 = 0 \frac{m}{s}$$
  
$$\tau_r = \psi_0 = 1 + \frac{\gamma - 1}{2} M_0^2 = 1 \qquad T_{t0} = T_0 \tau_r = 288 \cdot 1 = 288 \cdot K$$
  
$$p_{t0} = p_0 \tau_r^{\frac{1}{k}} = 1.013 \cdot 10^5 \cdot 1^{\frac{1}{0.2857}} = 1.013 \cdot 10^5 \cdot Pa$$

## Diffusore

 $p_{t2} = p_{t0}\pi_d = 1.013 \cdot 10^5 \cdot 1 = 1.013 \cdot 10^5 Pa$ 

## Compressore

 $\begin{aligned} \tau_c &= \pi_c^{\frac{k}{e_c}} = 21.5^{\frac{0.286}{0.92}} = 2.60 \qquad p_{t3} = p_{t2}\pi_c = 1.013 \cdot 10^5 \cdot 21.5 = 2.18 \cdot 10^6 \cdot Pa \\ T_{t3} &= \tau_c T_{t2} = 2.60 \cdot 288 = 749 \cdot K \end{aligned}$ 

## Camera di Combustione

$$\tau_{\lambda} = \frac{c_{pt} T_{t4}}{c_p T_0} = \frac{1057 \cdot 1350}{1004 \cdot 288} = 4.93$$

$$f = \frac{\tau_{\lambda} - \tau_c \tau_r}{Q_R \eta_b / (c_p T_0) - \tau_{\lambda}} = \frac{4.93 - 2.60 \cdot 1}{\frac{42.8 \cdot 10^6 \cdot 0.95}{1004 \cdot 288} - 4.93} = 0.01717$$
  
$$\tau_b = \frac{\tau_{\lambda}}{\tau_c \tau_r} = \frac{4.93}{2.59 \cdot 1} = 1.896$$
  
$$p_{t4} = p_{t3} \pi_b = 2.18 \cdot 10^6 \cdot 0.955 = 2.08 \cdot 10^6 \cdot Pa$$

### Fan

 $\tau_f = \pi_f^{\frac{k}{e_f}} = 1.53^{\frac{0.2857}{0.96}} = 1.135 \qquad p_{t13} = p_{t2}\pi_f = 1.013 \cdot 10^5 \cdot 1.53 = 1.550 \cdot 10^6 \cdot Pa$  $T_{t13} = T_{t2}\tau_f = 288 \cdot 1.135 = 327 \cdot K$ 

#### Turbina

$$\begin{aligned} \tau_t &= 1 - \frac{\tau_r \left[ (\tau_c - 1) + \alpha \left( \tau_f - 1 \right) \right]}{\eta_m (1 + f) \tau_\lambda} = 1 - \frac{1 \left[ 1.60 + 5.05 \cdot 0.135 \right]}{0.98 \cdot 1.017 \cdot 4.93} = 0.536 \\ \pi_t &= \tau_t^{\frac{1}{k_t e_t}} = 0.536 \frac{1}{0.259 \cdot 0.90} = 0.0689 \\ p_{t5} &= p_{t4} \pi_t = 2.08 \cdot 10^6 \cdot 0.0689 = 0.1433 \cdot 10^6 \cdot Pa \qquad T_{t5} = T_{t4} \tau_t = 1350 \cdot 0.536 = 724 \cdot K \end{aligned}$$

#### Ugello

$$p_{t9} = p_{t5}\pi_n = 0.1433 \cdot 10^6 \cdot 0.98 = 0.1404 \cdot 10^6 \cdot Pa \qquad T_{t9} = T_{t5} = 724 \cdot K$$

$$\frac{p_{t9}}{p_9} = \pi_n \pi_t \pi_b \pi_c \pi_d \pi_r \frac{p_0}{p_9} = \frac{p_{t9}}{p_0} \frac{p_0}{p_9} = \frac{1.404}{1.013} \cdot 1 = 1.386$$

$$\psi_9 = \frac{T_{t9}}{T_9} = 1 + \frac{\gamma_t - 1}{2} M_9^2 = \left(\frac{p_{t9}}{p_9}\right)^{k_t} = (1.386)^{0.259} = 1.088$$

$$M_9 = \sqrt{\frac{2}{\gamma_t - 1}} (\psi_9 - 1) = \sqrt{\frac{2}{0.35}} (1.088 - 1) = 0.710$$

$$T_9 = \frac{T_9}{T_{t9}} T_{t9} = \frac{724}{1.088} = 665 \cdot K$$

$$a_9 = \sqrt{\gamma_t R_9 T_9} = \sqrt{1.35 \cdot 274 \cdot 665} = 496 \cdot \frac{m}{s} \qquad V_9 = M_9 a_9 = 0.710 \cdot 496 = 352 \cdot \frac{m}{s}$$

$$V_{9.e} = V_9 \left(1 + \frac{1 - \frac{p_0}{p_9}}{\gamma_9 M_9^2}\right) = V_9 \qquad \frac{V_9}{a_0} = \frac{352}{340} = 1.035$$

### **Ugello Fan**

 $p_{t19} = p_{t13}\pi_{nf} = 1.550 \cdot 10^5 \cdot 0.99 = 1.534 \cdot 10^5 \cdot Pa \qquad T_{t19} = T_{t13} = 327 \cdot K$   $\frac{p_{t19}}{p_{19}} = \frac{p_{t19}}{p_0} \frac{p_0}{p_{19}} = \frac{153.5}{101.3} 1 = 1.515 \qquad \psi_{19} = \frac{T_{t19}}{T_{19}} = \left(\frac{p_{t19}}{p_{19}}\right)^k = (1.515)^{0.286} = 1.126$   $M_{19} = \sqrt{\frac{2}{\gamma - 1}(\psi_{19} - 1)} = \sqrt{\frac{2}{0.4}(1.126 - 1)} = 0.794$ 

$$T_{19} = \frac{T_{19}}{T_{t19}} T_{t19} = \frac{327}{1.126} = 290 \cdot K \qquad a_{19} = \sqrt{\gamma R T_{19}} = \sqrt{1.40 \cdot 287 \cdot 290} = 341 \frac{m}{s}$$
$$V_{19} = M_{19} a_{19} = 0.794 \cdot 341 = 271 \cdot \frac{m}{s}$$
$$V_{19.e} = V_{19} \left( 1 + \frac{1 - \frac{p_0}{p_{19}}}{\gamma M_{19}^2} \right) = V_{19} \qquad \frac{V_{19}}{a_0} = \frac{271}{340} = 0.797$$

# Spinta e rendimenti

$ \begin{array}{ll} \frac{F_u}{m_{air}a_0} = \frac{F_{u,core}}{m_{air}a_0} + \frac{F_{u,Fan}}{m_{air}a_0} = \frac{(1+f)}{1+\alpha} \frac{V_{9,e}}{a_0} + \frac{\alpha}{1+\alpha} \frac{V_{19,e}}{a_0} - M_0 \\ \frac{F_{u,core}}{m_{air}a_0} = \frac{(1+f)}{1+\alpha} \frac{V_{9,e}}{a_0} - \frac{M_0}{1+\alpha} = \frac{1.017}{6.05} 1.035 - 0 = 0.1740 \\ \frac{F_{u,ran}}{m_{air}a_0} = \frac{\alpha}{1+\alpha} \frac{V_{19,e}}{a_0} - \frac{\alpha M_0}{1+\alpha} = \frac{5.05}{6.05} 0.797 - 0 = 0.665 \\ \frac{F_u}{F_u} = \frac{F_{u,core}}{m_{air}a_0} + \frac{F_{u,Fan}}{m_{air}a_0} = 0.1740 + 0.665 = 0.839 \\ \frac{F_{u,core}}{F_u} = \frac{0.1740}{0.839} = 21\%  \frac{F_{u,Fan}}{F_u} = \frac{0.665}{0.839} = 79\% \\ \frac{F_u}{m_0} = D = (1+f)V_{9,e} + \alpha V_{19,e} - (1+\alpha)V_0 = 1.017 \cdot 352 + 5.05 \cdot 271 - 6.05 \cdot 0 = 1727 \cdot \frac{S}{m} \\ N = (1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2 = 1.017 \cdot 352^2 + 5.05 \cdot 271^2 - 6.05 \cdot 0 \\ = 4.97 \cdot 10^5 \cdot \frac{m^2}{S^2} \\ \eta_{th} = \frac{\Delta K\dot{E}}{P_t} = \frac{(1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2}{2fQ_R} = \frac{4.97 \cdot 10^5}{2 \cdot 0.01717 \cdot 42.8 \cdot 10^6} = 33.8\% \\ \eta_p = \frac{F_uV_0}{\Delta K\dot{E}} = \frac{2V_0[(1+f)V_{9,e} + \alpha V_{19,e} - (1+\alpha)V_0^2}{(1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2} = 0 \\ \\ \frac{\text{Section}}{1 \times 2.59299} \frac{1.13493}{1.3493} \frac{0.53755}{0.53755} \frac{4.93422}{\pi} \frac{1}{0.06993} \\ \frac{1}{1.4071} \frac{1}{0.72735} \frac{1.292}{0.01727} \frac{1}{0.9258} \frac{1}{0.01726} \\ \frac{1}{1.4071} \frac{1}{0.72735} \frac{1.09258}{0.01300} \frac{1}{1.4948} \frac{1}{325.86} \frac{725.86}{325.86} \frac{326.859}{326.859} \frac{1}{9} \\ \frac{1}{1.4071} \frac{1}{0.72735} \frac{1.09258}{0.072735} \frac{1.09258}{0.0099} \frac{1.0300}{0} \frac{1}{1} \\ \frac{1}{19} \frac{1}{19} \frac{1}{19} \frac{1}{15147} \frac{1}{0.97599} \frac{1}{0.999} \frac{1}{0.90919} \\ \frac{1.4071}{0.72735} \frac{0.72735}{0.72735} \frac{1.09258}{0.10300} \frac{1}{0.7838} \frac{1}{0.7816} \frac{1}{0.21127} \\ \frac{1}{7} \frac{1}{7$										
$\begin{split} N &= (1+f)V_{9,e}^2 + aV_{19,e}^2 - (1+a)V_0^2 = 1.017 \cdot 352^2 + 5.05 \cdot 271^2 - 6.05 \cdot 0 \\ &= 4.97 \cdot 10^5 \cdot \frac{m^2}{s^2} \\ \eta_{th} &= \frac{\Delta K \dot{E}}{\mathcal{P}_t} = \frac{(1+f)V_{9,e}^2 + aV_{19,e}^2 - (1+a)V_0^2}{2fQ_R} = \frac{4.97 \cdot 10^5}{2 \cdot 0.01717 \cdot 42.8 \cdot 10^6} = 33.8\% \\ \eta_p &= \frac{F_U V_0}{\Delta K \dot{E}} = \frac{2V_0[(1+f)V_{9,e} + aV_{19,e}^2 - (1+a)V_0^2]}{(1+f)V_{9,e}^2 + aV_{19,e}^2 - (1+a)V_0^2} = 0 \\ \hline \\ \hline \\ \hline \\ Section & c & f & t & \lambda & t & \\ \tau & 2.59299 & 1.13493 & 0.53755 & 4.93422 & \pi & 0.06993 \\ \hline \\ Section & 0 & 2 & 3 & 4 & 5 & 9 & 13 & 19 \\ \hline \\ Tt & 288.0 & 288 & 746.8 & 1349.8 & 725.586 & 725.586 & 326.859 & 326.859 \\ pt & 101,300 & 101,300 & 2.18E+06 & 2.08E+06 & 145,448 & 142,539 & 154,989 & 153,439 \\ \hline \\ Core & f & 0.01726 & & & \\ \hline \\ Pt9/p9 & M9 & M9 Eff & Tt9/T9 & P9 & po/p9 & & & \\ \hline \\ T9 & a9 & V9 & V9/a0 & V9/a0 eff & F/ma0 & F/maira0 & Fc/Ft \\ \hline \\ 664.102 & 495.666 & 360.524 & 1.06009 & 1.07838 & 0.17816 & 0.21127 \\ \hline \\ Fan & & & & \\ \hline \\ Pt19/p19 & M19 & M19 Eff & Tt19/T19 & P19 & po/p19 & & \\ \hline \\ T19 & a19 & V19 & V19/a0 & V19/a0 ef & F/ma0 & F/maira0 & Fc/Ft \\ \hline \\ 290.294 & 341.441 & 270.965 & 0.79675 & 0.79675 & 4.02595 & 0.66512 & 0.78873 \\ \hline \\ Num & Section & t & th p & 0 & TSFC*1e3 F/ma0 & F/maira0 & F/maira0 \\ \hline \\ \hline \\ \end{array}$	$\frac{F_{u.core}}{\dot{m}_{air}a_0} = \frac{F_{u.Fan}}{\dot{m}_{air}a_0} = \frac{F_u}{\dot{m}_{air}a_0} = \frac{F_u}{F_u} = \frac{F_{u.core}}{F_u} = D = 0$	$\frac{\frac{(1+f)}{1+\alpha}}{\frac{\alpha}{1+\alpha}} \frac{V_{1}}{\alpha}$ $\frac{F_{u.core}}{m_{air}a_{0}}$ $\frac{0.1740}{0.839} = (1+f)^{1}$	$\frac{V_{9,e}}{a_0} - \frac{M}{1+1}$ $\frac{H_{9,e}}{a_0} - \frac{\alpha M}{1+1}$ $- \frac{F_{u.Fan}}{\dot{m}_{air}a_0}$ $21\%$ $V_{9,e} + \alpha V_{1}$	$\frac{t_0}{r_0} = \frac{1.0}{6.0}$ $\frac{t_0}{\alpha} = \frac{5.05}{6.05}$ $= 0.1740$ $\frac{F_{u.Fan}}{F_u}$ $t_{19.e} - (1 - 1)$	$\frac{17}{95} 1.035 + 0.797 - 0 + 0.665 = \frac{0.665}{0.839} = + \alpha)V_0 =$	-0 = 0.1 0 = 0.665 = 0.839 = 79% $1.017 \cdot 35$	740 ; 52 + 5.05	$\cdot 271 - 6$	$5.05 \cdot 0 =$ 4 \cdot 10^{-6} \cdot 4	$1727 \cdot \frac{s}{m}$ <u>kg</u>
$\begin{split} N &= (1+f)V_{9,e}^2 + aV_{19,e}^2 - (1+a)V_0^2 = 1.017 \cdot 352^2 + 5.05 \cdot 271^2 - 6.05 \cdot 0 \\ &= 4.97 \cdot 10^5 \cdot \frac{m^2}{s^2} \\ \eta_{th} &= \frac{\Delta K \dot{E}}{\mathcal{P}_t} = \frac{(1+f)V_{9,e}^2 + aV_{19,e}^2 - (1+a)V_0^2}{2fQ_R} = \frac{4.97 \cdot 10^5}{2 \cdot 0.01717 \cdot 42.8 \cdot 10^6} = 33.8\% \\ \eta_p &= \frac{F_U V_0}{\Delta K \dot{E}} = \frac{2V_0[(1+f)V_{9,e} + aV_{19,e}^2 - (1+a)V_0^2]}{(1+f)V_{9,e}^2 + aV_{19,e}^2 - (1+a)V_0^2} = 0 \\ \hline \\ \hline \\ \hline \\ Section & c & f & t & \lambda & t & \\ \tau & 2.59299 & 1.13493 & 0.53755 & 4.93422 & \pi & 0.06993 \\ \hline \\ Section & 0 & 2 & 3 & 4 & 5 & 9 & 13 & 19 \\ \hline \\ Tt & 288.0 & 288 & 746.8 & 1349.8 & 725.586 & 725.586 & 326.859 & 326.859 \\ pt & 101,300 & 101,300 & 2.18E+06 & 2.08E+06 & 145,448 & 142,539 & 154,989 & 153,439 \\ \hline \\ Core & f & 0.01726 & & & \\ \hline \\ Pt9/p9 & M9 & M9 Eff & Tt9/T9 & P9 & po/p9 & & & \\ \hline \\ T9 & a9 & V9 & V9/a0 & V9/a0 eff & F/ma0 & F/maira0 & Fc/Ft \\ \hline \\ 664.102 & 495.666 & 360.524 & 1.06009 & 1.07838 & 0.17816 & 0.21127 \\ \hline \\ Fan & & & & \\ \hline \\ Pt19/p19 & M19 & M19 Eff & Tt19/T19 & P19 & po/p19 & & \\ \hline \\ T19 & a19 & V19 & V19/a0 & V19/a0 ef & F/ma0 & F/maira0 & Fc/Ft \\ \hline \\ 290.294 & 341.441 & 270.965 & 0.79675 & 0.79675 & 4.02595 & 0.66512 & 0.78873 \\ \hline \\ Num & Section & t & th p & 0 & TSFC*1e3 F/ma0 & F/maira0 & F/maira0 \\ \hline \\ \hline \\ \end{array}$	ISFC = -	$\frac{f}{F} = \frac{1}{F/2}$	$\frac{1}{n_0} = \frac{1}{(1 + 1)^2}$	$(f)V_{a}$	$\alpha V_{10} =$	$(1 \pm \alpha)V$	$\frac{1}{2} = \frac{1}{172}$	$\frac{1}{100} = 9.9$	$4 \cdot 10$ ° ·	sN
$\begin{split} \eta_{th} &= \frac{\Delta K \dot{E}}{\mathcal{P}_t} = \frac{(1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2}{2fQ_R} = \frac{4.97 \cdot 10^5}{2 \cdot 0.01717 \cdot 42.8 \cdot 10^6} = 33.8\% \\ \eta_p &= \frac{F_u V_0}{\Delta K \dot{E}} = \frac{2V_0 [(1+f)V_{9,e} + \alpha V_{19,e} - (1+\alpha)V_0]}{(1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2} = 0 \\ \hline \\$	$N = (1 + 1)^{-1}$	$f)V_{9.e}^2 +$	$\alpha V_{19.e}^2 - ($	$(1+\alpha)V_0^2$	$uv_{19.e} = 1.017$	(1 + u) $\cdot 352^2 +$	$5.05 \cdot 271$	$l^2 - 6.05$	· 0	511
$\begin{split} \eta_{th} &= \frac{\Delta K \dot{E}}{\mathcal{P}_t} = \frac{(1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2}{2fQ_R} = \frac{4.97 \cdot 10^5}{2 \cdot 0.01717 \cdot 42.8 \cdot 10^6} = 33.8\% \\ \eta_p &= \frac{F_u V_0}{\Delta K \dot{E}} = \frac{2V_0 [(1+f)V_{9,e} + \alpha V_{19,e} - (1+\alpha)V_0]}{(1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2} = 0 \\ \hline \\$		= 4.9	$97 \cdot 10^5 \cdot$	$\frac{m^2}{r^2}$						
t       2.39299       1.13493       0.33735       4.93422       t       0.00993       c       c       c         Section       0       2       3       4       5       9       13       19         Tt       288.0       288       746.8       1349.8       725.586       725.586       326.859       326.859         pt       101,300       101,300       2.18E+06       2.08E+06       145,448       142,539       154,989       153,439         Core       f       0.01726               Pt9/p9       M9       M9 Eff       Tt9/T9       P9       po/p9 <td>ΛK</td> <td>Ė (1⊥</td> <td><math>f V^2 \perp</math></td> <td><math>\alpha V^2</math> –</td> <td><math>(1 \perp \alpha) V^2</math></td> <td>2</td> <td>1.97.10</td> <td>5</td> <td></td> <td></td>	ΛK	Ė (1⊥	$f V^2 \perp$	$\alpha V^2$ –	$(1 \perp \alpha) V^2$	2	1.97.10	5		
t       2.39299       1.13493       0.33735       4.93422       t       0.00993       c       c       c         Section       0       2       3       4       5       9       13       19         Tt       288.0       288       746.8       1349.8       725.586       725.586       326.859       326.859         pt       101,300       101,300       2.18E+06       2.08E+06       145,448       142,539       154,989       153,439         Core       f       0.01726               Pt9/p9       M9       M9 Eff       Tt9/T9       P9       po/p9 <td><math>\eta_{th} = \frac{\Delta R}{\sigma}</math></td> <td><math>\frac{L}{-} = \frac{(1 + 1)}{-}</math></td> <td>J ) V 9.e I</td> <td>uv<sub>19.e</sub></td> <td><math>(1 + a)v_0</math></td> <td><math>\frac{1}{2} = \frac{1}{2}</math></td> <td></td> <td><math>\frac{1}{20}</math> = 106</td> <td>= 33.8%</td> <td></td>	$\eta_{th} = \frac{\Delta R}{\sigma}$	$\frac{L}{-} = \frac{(1 + 1)}{-}$	J ) V 9.e I	uv <sub>19.e</sub>	$(1 + a)v_0$	$\frac{1}{2} = \frac{1}{2}$		$\frac{1}{20}$ = 106	= 33.8%	
t       2.39299       1.13493       0.33735       4.93422       t       0.00993       c       c       c         Section       0       2       3       4       5       9       13       19         Tt       288.0       288       746.8       1349.8       725.586       725.586       326.859       326.859         pt       101,300       101,300       2.18E+06       2.08E+06       145,448       142,539       154,989       153,439         Core       f       0.01726               Pt9/p9       M9       M9 Eff       Tt9/T9       P9       po/p9 <td><math>\mathcal{P}_{i}</math></td> <td></td> <td>1 + f</td> <td><math>2JQ_R</math></td> <td>(1</td> <td>۷۰۷ 1 تا در</td> <td><math>)1/1/\cdot 4</math></td> <td><math>2.8 \cdot 10^{6}</math></td> <td></td> <td></td>	$\mathcal{P}_{i}$		1 + f	$2JQ_R$	(1	۷۰۷ 1 تا در	$)1/1/\cdot 4$	$2.8 \cdot 10^{6}$		
t       2.39299       1.13493       0.33735       4.93422       t       0.00993       c       c       c         Section       0       2       3       4       5       9       13       19         Tt       288.0       288       746.8       1349.8       725.586       725.586       326.859       326.859         pt       101,300       101,300       2.18E+06       2.08E+06       145,448       142,539       154,989       153,439         Core       f       0.01726               Pt9/p9       M9       M9 Eff       Tt9/T9       P9       po/p9 <td><math>n_n = \frac{F_u V_u}{V_u}</math></td> <td><math>\frac{0}{1} = \frac{2V_0[(}{1)}</math></td> <td><math>(1 + f)V_{9.6}</math></td> <td><math>_{2} + \alpha V_{19.e}</math></td> <td><math>\frac{1}{2} - (1 + 0)</math></td> <td><math>\frac{v_0 v_0}{v_0} = 0</math></td> <td></td> <td></td> <td></td> <td></td>	$n_n = \frac{F_u V_u}{V_u}$	$\frac{0}{1} = \frac{2V_0[(}{1)}$	$(1 + f)V_{9.6}$	$_{2} + \alpha V_{19.e}$	$\frac{1}{2} - (1 + 0)$	$\frac{v_0 v_0}{v_0} = 0$				
t       2.39299       1.13493       0.33735       4.93422       t       0.00993       c       c       c         Section       0       2       3       4       5       9       13       19         Tt       288.0       288       746.8       1349.8       725.586       725.586       326.859       326.859         pt       101,300       101,300       2.18E+06       2.08E+06       145,448       142,539       154,989       153,439         Core       f       0.01726               Pt9/p9       M9       M9 Eff       Tt9/T9       P9       po/p9 <td><math>\Delta KI</math></td> <td>E (1</td> <td><math>(+ f)V_{9.e}^2</math></td> <td>+ αV<sup>2</sup><sub>19.e</sub> -</td> <td><math>-(1 + \alpha)</math></td> <td><math>V_0^2</math></td> <td></td> <td> </td> <td>  </td> <td></td>	$\Delta KI$	E (1	$(+ f)V_{9.e}^2$	+ αV <sup>2</sup> <sub>19.e</sub> -	$-(1 + \alpha)$	$V_0^2$				
t       2.39299       1.13493       0.33735       4.93422       t       0.00993       c       c       c         Section       0       2       3       4       5       9       13       19         Tt       288.0       288       746.8       1349.8       725.586       725.586       326.859       326.859         pt       101,300       101,300       2.18E+06       2.08E+06       145,448       142,539       154,989       153,439         Core       f       0.01726               Pt9/p9       M9       M9 Eff       Tt9/T9       P9       po/p9 <td>Section</td> <td>с</td> <td>f</td> <td>t</td> <td>λ</td> <td></td> <td>t</td> <td></td> <td></td> <td></td>	Section	с	f	t	λ		t			
Tt288.0288746.81349.8725.586725.586326.859326.859pt101,300101,3002.18E+062.08E+06145,448142,539154,989153,439Coref0.01726 </td <td>τ</td> <td>2.59299</td> <td>1.13493</td> <td>0.53755</td> <td>4.93422</td> <td><math>\pi</math></td> <td>0.06993</td> <td></td> <td></td> <td></td>	τ	2.59299	1.13493	0.53755	4.93422	$\pi$	0.06993			
pt101,300101,3002.18E+062.08E+06145,448142,539154,989153,439Coref0.01726Pt9/p9M9M9 EffTt9/T9P9po/p91.40710.727350.727351.092581013001T9a9V9V9/a0V9/a0 effF/ma0F/maira0Fc/Ft <td>Section</td> <td>0</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>9</td> <td>13</td> <td>19</td> <td></td>	Section	0	2	3	4	5	9	13	19	
Core         f         0.01726         Image: marked state	Tt	288.0	288	746.8	1349.8	725.586	725.586	326.859	326.859	
Pt9/p9         M9         M9 Eff         Tt9/T9         P9         po/p9         Image: Constraint of the text of tex of text of text of tex of text of text of tex of te	pt	101,300	101,300	2.18E+06	2.08E+06	145,448	142,539	154,989	153,439	
1.4071       0.72735       0.72735       1.09258       101300       1       Image: constraint of the state of the s	Core		f	0.01726						
T9       a9       V9       V9/a0       V9/a0 eff       F/ma0       F/maira0       Fc/Ft         664.102       495.666       360.524       1.06009       1.07838       0.17816       0.21127         Fan                 Pt19/p19       M19       M19 Eff       Tt19/T19       P19       po/p19             1.5147       0.79359       0.79359       1.12596       101300       1             T19       a19       V19       V19/a0       V19/a0 ef       F/ma0       F/maira0       FF/Ft         290.294       341.441       270.965       0.79675       0.79675       4.02595       0.66512       0.78873         Num       Section       t       th       p       0       TSFC*1e3       F/ma0       F/maira0	Pt9/p9	M9	M9 Eff	Tt9/T9	Р9	po/p9				
664.102       495.666       360.524       1.06009       1.07838       0.17816       0.21127         Fan       Image: Constraint of the state of t	1.4071	0.72735	0.72735	1.09258	101300	1				
Fan         Image: M19         M19 Eff         Tt19/T19         P19         po/p19         Image: M19         M19 Eff         Tt19/T19         P19         po/p19         Image: M10	Т9	a9	V9	V9/a0	V9/a0 eff	F/ma0	F/maira0		Fc/Ft	
Pt19/p19         M19         M19 Eff         Tt19/T19         P19         po/p19         Image: Mail of the state of the st	664.102	495.666	360.524	1.06009	1.06009	1.07838	0.17816		0.21127	
1.5147       0.79359       0.79359       1.12596       101300       1       Image: constraint of the state of the s	Fan									
T19       a19       V19       V19/a0       V19/a0 ef       F/ma0       F/maira0       FF/Ft         290.294       341.441       270.965       0.79675       0.79675       4.02595       0.66512       0.78873         Num       Section       t       th       p       0       TSFC*1e3       F/ma0       F/maira0	Pt19/p19	M19	M19 Eff	Tt19/T19	P19	po/p19				
290.294         341.441         270.965         0.79675         4.02595         0.66512         0.78873           Num         Section         t         th         p         0         TSFC*1e3         F/ma0         F/maira0	1.5147	0.79359	0.79359	1.12596	101300	1				
Num Section t th p 0 TSFC*1e3 F/ma0 F/maira0	T19	a19	V19	V19/a0	V19/a0 ef	F/ma0	F/maira0		FF/Ft	
	290.294	341.441	270.965	0.79675	0.79675	4.02595	0.66512		0.78873	
5.03E+05 η 0.9281 0.3407 0 0 0.0099 5.10433 0.84327	Num	Section	t	th	р	0	TSFC*1e3	F/ma0	F/maira0	
	5.03E+05	η	0.9281	0.3407	0	0	0.0099	5.10433	0.84327	

## J79D by Tom M0=0.85

JT9d By	Tom							13	19
	2	3	4	5	9	13	19		<u>5</u>
	diff	comp	CC	Tur	No	Fan	No FAn	[d†c∏	
с <sub>р</sub>	1004			1057				$\sqrt{3}$	4
γ	1.4			1.35					
$\pi$	1	21.5	0.955		0.98	1.53	0.99		
η, e <sub>c,t</sub>		0.92	0.95	0.9		0.96			
Tt				1349.8					
M0	0.85				QR	42800	kJ/kgK		
то	288	К	p0	101,300	Ра	$\eta_m$	0.98		
alpha	5.053								

 $k = \frac{\gamma - 1}{\gamma} = \frac{0.4}{1.4} = 0.2867 \quad k_5 = \frac{\gamma_5 - 1}{\gamma_5} = \frac{0.35}{1.35} = 0.2593$   $R = kc_p = 0.2867 \cdot 1004 = 286.9J/kgK \quad R_5 = 0.2593 \cdot 1057 = 274.0J/kgK$   $a_0 = \sqrt{\gamma RT_0} = 1.4 \cdot 286.9 \cdot 288 = 340.1m/s$   $V_0 = M_0 \cdot a_0 = 0.85 \cdot 340.1 = 289.1m/s$ 

#### Presa d'aria

 $\begin{aligned} \tau_r &= \psi_0 = 1 + \frac{\gamma - 1}{2} M_0^2 = 1 + 0.2 \cdot 0.85^2 = 1.145 \\ T_{t0} &= T_{t2} = T_0 \tau_r = 288 \cdot 1.145 = 329.6K \quad p_{t0} = \tau_r^{\frac{1}{k}} p_0 = 1.145 \frac{1}{0.2867} 1.013 \cdot 10^5 = 162.5 kPa \\ p_{t2} &= p_{t0} \pi_d = 162.5 \cdot 1 = 162.5 kPa \end{aligned}$ 

#### Compressore

 $\begin{aligned} \tau_c &= \pi_c^{\frac{k}{e_c}} = 21.5^{\frac{0.2867}{0.92}} = 2.593 \\ p_{t3} &= p_{t2}\pi_c = 162.5 \cdot 21.5 \cdot 10^3 = 3493 kPa \qquad T_{t3} = T_{t2}\tau_c = 329.6 \cdot 2.593 = 854.7K \end{aligned}$ 

#### Camera di combustione

 $p_{t4} = p_{t3}\pi_b = 3.493 \cdot 0.955 \cdot 10^3 = 3336kPa \qquad \tau_\lambda = \frac{c_{p5}T_{t4}}{c_pT_0} = \frac{1057 \cdot 1350}{288 \cdot 1004} = 4.934$  $f = \frac{\tau_\lambda - \tau_c\tau_r}{Q_R\eta_b/(c_pT_0) - \tau_\lambda} = \frac{4.934 - 2.593 \cdot 1.145}{42.8 \cdot 10^6 \cdot 0.95/(288 \cdot 1004) - 4.934} = 0.01449$ 

Fan

$$\tau_f = \pi_f^{\frac{k}{e_f}} = 1.53^{\frac{0.2867}{0.96}} = 1.135$$
  
$$p_{t13} = p_{t2}\pi_f = 162.5 \cdot 1.53 \cdot 10^3 = 248.6kPa \quad T_{t13} = T_{t2}\tau_f = 329.6 \cdot 1.135 = 374.1K$$

# Turbina

$$\begin{aligned} \tau_t &= 1 - \frac{\tau_r \left[ (\tau_c - 1) + \alpha \left( \tau_f - 1 \right) \right]}{\eta_m (1 + f) \tau_\lambda} = 1 - \frac{1.145 [1.593 + 5.053 \cdot 0.135]}{0.98 \cdot 1.014 \cdot 4.934} = 0.4693 \\ \pi_t &= \tau_t^{\frac{1}{k_5 e_t}} = 0.4693 \overline{0.2593 \cdot 0.900} = 0.03907 \\ p_{t5} &= p_{t4} \pi_t = 333.6 \cdot 0.03907 \cdot 10^3 = 130.3 kPa \\ T_{t5} &= T_{t4} \tau_t = 1350 \cdot 0.4693 = 633.4 K \end{aligned}$$

# Ugello

$$p_{t9} = p_{t5}\pi_n = 130.3 \cdot 0.98 \cdot 10^3 = 127.7kPa$$

$$\frac{p_{t9}}{p_9} = \frac{127.7}{101.3} = 1.261 \qquad \psi_9 = \left(\frac{p_{t9}}{p_9}\right)^{k_5} = 1.261^{0.2593} = 1.062$$

$$M_9 = \sqrt{\frac{2}{\gamma_5 - 1}}[\psi_9 - 1] = \sqrt{\frac{2}{.35}}[1.062 - 1] = 0.5950$$

$$M_9 < 1 \rightarrow p_9 = p_0 \text{ (OK)}$$

$$T_9 = T_{t9}/\psi_9 = T_{t5}/\psi_9 = 633.4/1.062 = 596.5K$$

$$a_9 = \sqrt{\gamma_5 R_5 T_9} = \sqrt{1.35 \cdot 274.0 \cdot 596.5} = 469.8m/s$$

$$V_9 = M_9 \cdot a_9 = 0.5950 \cdot 469.8 = 279.5m/s \qquad \frac{V_9}{a_0} = \frac{279.5}{340.1} = 0.8219 \qquad < M_0 \quad (??)$$

# Ugello Fan

$$p_{t19} = \pi_{nf} p_{t13} = 0.99 \cdot 249.0 = 247 \cdot kPa \qquad T_{t19} = T_{t13} = 374 \cdot K$$

$$\frac{p_{t19}}{p_{19}} = \frac{p_{t19}}{p_0} \frac{p_0}{p_{19}} = \frac{247}{101.3} 1 = 2.44 \qquad \psi_{19} = \frac{T_{t19}}{T_{19}} = \left(\frac{p_{t19}}{p_{19}}\right)^k = (1.515)^{0.286} = 1.291$$

$$M_{19} = \sqrt{\frac{2}{\gamma - 1}(\psi_{19} - 1)} = \sqrt{\frac{2}{0.4}(1.291 - 1)} = 1.205$$

Se l'ugello non è convergente divergente allora  $\frac{p_0}{p_{19}} \neq 1$ . . Si impone  $M_{19} = 1$ 

$$\begin{aligned} \frac{T_{t19}}{T_{19}} &= \psi_{19} = 1 + \frac{\gamma - 1}{2} M_{19}^2 = 1 + \frac{0.4}{2} 1 = 1.200 \quad T_{19} = \frac{T_{19}}{T_{t19}} T_{t19} = \frac{374}{1.200} = 312 \cdot K \\ \frac{p_{t19}}{p_{19}} &= \left(\frac{T_{t19}}{T_{19}}\right)^{\frac{1}{k}} = 1.200^{\frac{1}{0.286}} = 1.892 \\ p_{19} &= \frac{p_{19}}{p_{t19}} p_{t19} = \frac{247}{1.892} = 130.5 \cdot kPa \quad \frac{p_0}{p_{19}} = \frac{101.3}{130.5} = 0.776 \\ a_{19} &= \sqrt{\gamma R T_{19}} = \sqrt{1.40 \cdot 287 \cdot 312} = 354 \cdot \frac{m}{s} \quad V_{19} = M_{19}a_{19} = 1 \cdot 354 = 354 \cdot \frac{m}{s} \\ V_{19.e} &= V_{19} \left(1 + \frac{1 - \frac{p_0}{p_{19}}}{\gamma M_{19}^2}\right) = 354 \left(1 + \frac{1 - 0.776}{1.4 \cdot 1^2}\right) = 411 \cdot \frac{m}{s} \quad \frac{V_{19.e}}{a_0} = \frac{411}{340} = 1.209 \end{aligned}$$

# Spinta

$\frac{F_u}{\dot{m}_{air}a_0} = \frac{F_{u.core}}{\dot{m}_{air}a_0} + \frac{F_{u.Fan}}{\dot{m}_{air}a_0} = \frac{(1+f)}{1+\alpha} \frac{V_{9.e}}{a_0} + \frac{\alpha}{1+\alpha} \frac{V_{19.e}}{a_0} - M_0$
$\frac{F_{u.core}}{\dot{m}_{air}a_0} = \frac{(1+f)}{1+\alpha} \frac{V_{9.e}}{a_0} - \frac{M_0}{1+\alpha} = \frac{1.014}{6.05} 0.822 - \frac{0.85}{6.05} = -0.00273$
$\frac{F_{u.Fan}}{\dot{m}_{air}a_0} = \frac{\alpha}{1+\alpha} \frac{V_{19.e}}{a_0} - \frac{\alpha M_0}{1+\alpha} = \frac{5.05}{6.05} 1.209 - \frac{5.05}{6.05} 0.85 = 0.299$
$\frac{F_u}{\dot{m}_{air}a_0} = \frac{F_{u.core}}{\dot{m}_{air}a_0} + \frac{F_{u.Fan}}{\dot{m}_{air}a_0} =00273 + 0.299 = 0.297$
$\frac{F_{u.core}}{F_u} = \frac{00273}{0.297} = -0.92\% \qquad \qquad \frac{F_{u.Fan}}{F_u} = \frac{0.299}{0.297} = 100.7\%$
$\frac{F_u}{\dot{m}_0} = D = (1+f)V_{9.e} + \alpha V_{19.e} - (1+\alpha)V_0 = 1.014 \cdot 280 + 5.05 \cdot 411 - 6.05 \cdot 289 = 611 \cdot \frac{s}{m}$
$TSFC = \frac{\dot{m}_f}{F_u} = \frac{f}{F_u/\dot{m}_0} = \frac{f}{(1+f)V_{9.e} + \alpha V_{19.e} - (1+\alpha)V_0} = \frac{0.01449}{611} = 2.37 \cdot 10^{-5} \cdot \frac{kg}{sN}$
$N = (1+f)V_{9.e}^2 + \alpha V_{19.e}^2 - (1+\alpha)V_0^2 = 1.014 \cdot 280^2 + 5.05 \cdot 411^2 - 6.05 \cdot 289^2 = 4.27 \cdot 10^5$
$\eta_{th} = \frac{\Delta K \dot{E}}{\mathcal{P}_t} = \frac{(1+f)V_{9,e}^2 + \alpha V_{19,e}^2 - (1+\alpha)V_0^2}{2fQ_R} = \frac{4.27 \cdot 10^5}{2 \cdot 0.01449 \cdot 42.8 \cdot 10^6} = 34.5\%$
$\eta_p = \frac{F_u V_0}{\Delta K \dot{E}} = \frac{2V_0 [(1+f)V_{9.e} + \alpha V_{19.e} - (1+\alpha)V_0]}{(1+f)V_{9.e}^2 + \alpha V_{19.e}^2 - (1+\alpha)V_0^2} = \frac{2 \cdot 289 \cdot 611}{4.27 \cdot 10^5} = 83\%$
$\eta_0 = \eta_p \eta_{th} = .345 \cdot .83 = 28.6\%$

k	0.28571			0.25926					
R	286.857			274.037					
a0	340.1	m/s	V0	289.1	m/s				
$\tau_r = T_{t0} = 0$	1.1445								
Section	С	f	t	λ		t			
τ	2.59299	1.13493	0.46929	4.93422	π	0.03907			
Section	0	2	3	4	5	9	13	19	
Tt	329.6	329.616	854.7	1349.8	633.443	633.443	374.09	374.0899	
pt	162,467	162,467	3.49E+06	3.34E+06	130,342	127,735	248,574	246,089	
Core		f	0.01449						
Pt9/p9	M9	M9 Eff	Tt9/T9	Р9	po/p9				
1.26096	0.59502	0.59502	1.06196	101300	1				
Т9	a9	V9	V9/a0	V9/a0 eff	F/ma0	F/maira0		Fc/Ft	
596.486	469.755	279.513	0.82188	0.82188	-0.01621	-0.00268		-0.00913	
Fan									
Pt19/p19	M19	M19 Eff	Tt19/T19	P19	po/p19				
2.4293	1.20137	1	1.2	130004	0.77921				
T19	a19	V19	V19/a0	V19/a0 ef	F/ma0	F/maira0		FF/Ft	
311.742	353.83	353.83	1.0404	1.20448	1.7912	0.29592		1.00913	
Num	Section	t	th	р	0	TSFC*1e3	F/ma0	F/maira0	
4.21E+05	η	0.93345	0.3396	0.82835	0.28131	0.0240	1.775	0.293243	

# Farokhi Example 4.16

	2	3	4	5	13	15	6	7	9
	diff	comp	СС	Tur	Fan		Mixer		No
с <sub>р</sub>	1004			1152				1241	
γ	1.4			1.33				1.3	
$\pi$	0.9	13	0.95		1.9	0.99	0.9709	0.92	0.95
η, e <sub>c,t</sub>		0.9	0.98	0.8	0.9			0.98	
Tt			1600					2000	
M0	2.0000				QR	42000	kJ/kgK		
т0	223.0	К	p0	10000.0	Ра	$\eta_m$	0.95	p9/p0	3.8
k	0.2857			0.2481				0.2308	
R	286.9			285.8	kJ/kgK			286.4	kJ/kgK
a0	299.3	m/s	V0	598.5	m/s	$\tau_r = (\psi)$	1.8		

$$k = \frac{\gamma - 1}{\gamma} = \frac{1.4 - 1}{1.4} = 0.2857 \qquad k_t = \frac{\gamma_t - 1}{\gamma_t} = \frac{1.33 - 1}{1.33} = 0.2481$$

$$k_9 = \frac{\gamma_9 - 1}{\gamma_9} = \frac{1.3 - 1}{1.3} = 0.2308 \qquad R = kc_p = 1004 \cdot 0.2857 = 287 \cdot \frac{J}{kg \cdot K}$$

$$R_t = k_t c_{pt} = 1057 \cdot 0.2593 \frac{J}{kg \cdot K} = 286 \cdot \frac{J}{kg \cdot K}$$

$$R_9 = k_9 c_{p9} = 286 \cdot \frac{J}{kg \cdot K} \qquad p_0 = 10 \cdot kPa$$

### **Effetto Ram**

$$a_{0} = \sqrt{\gamma R T_{0}} = \sqrt{1.4 \cdot 287 \cdot 223} = 299 \cdot \frac{m}{s}$$

$$V_{0} = M_{0}a_{0} = 2.0 \cdot 299 = 598 \frac{m}{s} \qquad \tau_{r} = \psi_{0} = 1 + \frac{\gamma - 1}{2}M_{0}^{2} = 1.8$$

$$T_{t0} = T_{0}\tau_{r} = 223 \cdot 1.8 = 401 \cdot K$$

$$p_{t0} = p_{0}\tau_{r}^{\frac{1}{k}} = 10 \cdot 1.8^{\frac{1}{0.2857}} = 78.2 \cdot kPa$$

### Diffusore

 $p_{t2} = p_{t0}\pi_d = 78.2 \cdot 0.9 = 70.4 \cdot kPa$ 

# Compressore

 $\begin{aligned} \tau_c &= \pi_c^{\frac{k}{e_c}} = 13^{\frac{0.2857}{0.90}} = 2.26 \qquad p_{t3} = p_{t2}\pi_c = 70.4 \cdot 13 = 915 \cdot kPa \\ T_{t3} &= T_{t2}\tau_c = 401 \cdot 2.26 = 906 \cdot K \end{aligned}$ 

### **Camera di Combustione**

$$\tau_{\lambda} = \frac{c_{pt}T_{t4}}{c_p T_0} = \frac{1152 \cdot 1600}{1004 \cdot 223} = 8.23$$

$$f = \frac{\tau_{\lambda} - \tau_{c}\tau_{r}}{Q_{R}\eta_{b}/(c_{p}T_{0}) - \tau_{\lambda}} = \frac{8.23 - 2.26 \cdot 1.8}{\frac{42.0 \cdot 10^{6} \cdot 0.98}{1004 \cdot 223} - 8.23} = 0.0237$$
$$\tau_{b} = \frac{\tau_{\lambda}}{\tau_{c}\tau_{r}} = \frac{8.23}{2.26 \cdot 1.8} = 2.03$$
$$p_{t4} = p_{t3}\pi_{b} = 915 \cdot 0.95 = 870 \cdot kPa$$

### Fan

 $\begin{aligned} \tau_f &= \pi_f^{\frac{k}{e_f}} = 1.90^{\frac{0.2857}{0.90}} = 1.226 \qquad p_{t13} = p_{t2}\pi_f = 70.4 \cdot 1.90 = 134 \cdot kPa \\ T_{t13} &= T_{t2}\tau_f = 401 \cdot 1.226 = 492 \cdot K \end{aligned}$ 

## Turbina

$$\pi_t = \frac{\pi_{fd}\pi_f}{\pi_b\pi_c} = \frac{0.99 \cdot 1.90}{0.95 \cdot 13} = 0.1523 \qquad \tau_t = \pi_t^{k_t e_t} = 0.1523^{0.2481 \cdot 0.8} = 0.688$$
$$p_{t5} = p_{t4}\pi_t = 870 \cdot 0.1523 = 132 \cdot kPa \qquad T_{t5} = T_{t4}\tau_t = 1600 \cdot 0.688 = 1101 \cdot K$$

### Mixer

$$\alpha = \frac{\eta_m (1+f)(1-\tau_t)\tau_\lambda - \tau_r(\tau_c - 1)}{\tau_r(\tau_f - 1)} = \frac{0.95 \cdot 1.024(1 - 0.688)8.23 - 1.8(2.26 - 1)}{1.8(1.226 - 1)} = 0.571$$
  
$$\tau_M = \frac{\frac{\alpha \tau_f \tau_r}{\tau_t \tau_\lambda} + (1+f)}{1+\alpha + f} = \frac{0.571 \frac{1.226 \cdot 1.8}{0.688 \cdot 8.23} + 1.024}{1.024 + 0.571} = 0.782$$
  
$$p_{t6} = p_{t5}\pi_M = 132 \cdot 0.9709 = 128.6 \cdot kPa \qquad T_{t6} \sim T_{t5}\tau_M = 1101 \cdot 0.782 = 861 \cdot K$$

### **Post Bruciatore**

$$\tau_{\lambda AB} \frac{c_{p9}T_{t7}}{c_p T_0} = \frac{1241 \cdot 2000}{1004 \cdot 223} = 11.09$$

$$f_{AB} = \left(1 + \frac{f}{1+\alpha}\right) \frac{\tau_{\lambda AB} - \tau_M \tau_t \tau_\lambda}{\frac{Q_{R,AB} \eta_{AB}}{c_p T_0} - \tau_{\lambda,AB}} = \left(1 + \frac{0.0237}{1.571}\right) \frac{11.09 - 0.782 \cdot 0.688 \cdot 8.23}{\frac{42 \cdot 10^6 0.98}{1004 \cdot 223} - 11.09} = 0.0391$$

Section	с	f	t	λ	М	$\lambda_{AB}$			
τ	2.258	1.2260	0.6883	8.233	0.78147	11.0857			
Section	0	2	3	4	5	6	7	9	13
Tt	401.4	401.4	906.2	1600	1101.27	860.61	2000	2000	492.12
pt	78,244	70,420	915,461	869,688	132,460	128,606	118,317	112,401	133,798
$\pi_t$	0.15231	f	0.02374	α	0.5707	f <sub>AB</sub>	0.03912	f <sub>tot</sub>	0.05424
Pt9/p9	M9	M9 Eff	Tt9/T9	Р9	po/p9				
2.958	1.377	1.377	1.28437	38000	0.26316		13	156	
Т9	a9	V9	V9/a0	V9/a0 eff	F/ma0	F/maira0			
1557.19	761.407	1048.36	3.50318	4.551	4.39376	2.79736	d fic	btt	
Num	Section	t	th	р	0	TSFC*e3		3 4 5	<b>√</b> 9
1.6E+06	η	0.83551	0.3505	0.6275	0.21996	0.06479		64.787	

# Farokhi Example 4.386

	2	3	4	4.5	5	9		$10^{2}$	4.55 3 4	
	diff	comp	СС	Tur	Tur	No	Prop	dc	τ.Υ.Υ.	n
ср	1004			1152	J/kgs					
g	1.4			1.33				$\eta_m$ H	0.99	
р	0.99	35	0.96					$\eta_m$ L	0.99	
h, ec,t		0.92	0.99	0.8	0.859	0.95	0.85	$\eta_{gb}$	0.995	
Tt				1650						
M0	0.82				QR	42000	kJ/kgK			
т0	258	К	p0	30,000	Ра					
alpha	0.75	m0	50	kg/s						

$$k = \frac{\gamma - 1}{\gamma} = \frac{0.4}{1.4} = 0.2867 \quad k_5 = \frac{\gamma_5 - 1}{\gamma_5} = \frac{0.33}{1.33} = 0.2481$$
$$R = kc_p = 0.2867 \cdot 1004 = 286.9J/kgK \quad R_5 = 0.2481 \cdot 1152 = 285.8J/kgK$$
$$a_0 = \sqrt{\gamma RT_0} = 1.4 \cdot 286.9 \cdot 258 = 321.9m/s$$
$$V_0 = M_0 \cdot a_0 = 0.82 \cdot 321.9 = 263.9m/s$$

#### Effetto Ram

$$\tau_r = \psi_0 = 1 + \frac{\gamma - 1}{2} M_0^2 = 1 + 0.2 \cdot 0.81 = 1.134$$
$$T_{t0} = T_0 \tau_r = 288 \cdot 1.134 = 292.7K \qquad p_{t0} = \tau_r^{\frac{1}{k}} p_0 = 1.135^{\frac{1}{0.2867}} 30.00 \cdot 10^3 = 46.66 kPa$$

### Diffusore

 $p_{t2} = p_{t0}\pi_d = 46.66 \cdot 0.99 \cdot 10^3 = 46.19 kPa \qquad T_{t0} = T_{t2}$ 

### Compressore

$$\begin{split} \tau_c &= \pi_c^{\frac{k}{e_c}} = 35^{\frac{0.2867}{0.92}} = 3.017 \\ p_{t3} &= p_{t2}\pi_c = 46.19 \cdot 35 \cdot 10^3 = 1617 kPa \\ \end{split} \qquad T_{t3} &= T_{t2}\tau_c = 292.7 \cdot 3.017 = 883.0K \end{split}$$

### Camera di combustione

 $p_{t4} = p_{t3}\pi_b = 1.617 \cdot 0.99 \cdot 10^3 = 1552kPa \quad \tau_\lambda = \frac{c_{p5}T_{t4}}{c_pT_0} = \frac{1152 \cdot 1650}{258 \cdot 1004} = 7.338$  $f = \frac{\tau_\lambda - \tau_c\tau_r}{Q_R\eta_b/(c_pT_0) - \tau_\lambda} = \frac{7.338 - 3.017 \cdot 1.134}{42.0 \cdot 10^6 \cdot 0.99/(258 \cdot 1004) - 7.338} = 0.02556$ 

## **Turbina HP**

$$\tau_{tH} = 1 - \frac{\tau_r(\tau_c - 1)}{\eta_{mH}(1 + f)\tau_\lambda} = 1 - \frac{1.134(2.017)}{0.99 \cdot 1.026 \cdot 7.338} = 0.6929$$

 $\pi_{tH} = \tau_{tH}^{\frac{1}{k_5 e_{tH}}} = 0.6929^{\frac{1}{0.2481 \cdot 0.800}} = 0.1575$  $p_{t45} = p_{t4}\pi_{tH} = 155.2 \cdot 0.1575 \cdot 10^3 = 244.5 kPa \qquad T_{t45} = T_{t4}\tau_{tH} = 1650 \cdot 0.6929 = 1143K$ 

## **Turbina LP**

Supponendo funzionamento corretto nell'ugello:  $\frac{p_9}{p_0}=1$ 

$$\tau_{tL} = 1 - \eta_{tL} \alpha_p \left[ 1 - \left(\frac{p_0}{p_{t45}}\right)^{k_5} \right] = 1 - \eta_{tL} 0.75 \left[ 1 - \left(\frac{30}{244.5}\right)^{0.2481} \right]$$
  
$$\tau_{tL} = 1 - \eta_{tL} 0.75 [1 - 0.5942] = 1 - \eta_{tL} 0.3044$$
  
Supponendo  $\eta_{tL} = 1 \rightarrow \tau_{tL} = 0.6956$   $\eta_{tL} = \frac{1 - \tau_{tL}}{1 - \tau_{tL}^{\frac{1}{e_{tL}}}} = \frac{1 - 0.6956}{1 - 0.6956 \frac{1}{0.859}} = 0.8833$ 

Iterando si ha in sequenza:  $\tau_{tL}=0.7312,~\eta_{tL}=0.88010,~\tau_{tL}=0.7321,~\eta_{tL}=0.8800,~\tau_{tL}=0.7322$ 

$$\pi_{tL} = \tau_{tL}^{\frac{1}{k_5 e_{tL}}} = 0.7322^{\frac{1}{0.2481 \cdot 0.859}} = 0.2316$$

$$p_{t5} = p_{t45}\pi_{tL} = 244.5 \cdot 0.2316 \cdot 10^3 = 56.63kPa \qquad T_{t5} = T_{t45}\tau_{tL} = 1143 \cdot 0.7322 = 837.1K$$

## Ugello

$$\begin{split} \eta_n &= \frac{\left(\frac{p_{t5}}{p_9}\right)^{k_5} - \pi_n^{-k_5}}{\left(\frac{p_{t5}}{p_9}\right)^{k_5} - 1} \to \pi_n = \left\{ \left(\frac{p_{t5}}{p_9}\right)^{k_9} - \eta_n \left[ \left(\frac{p_{t5}}{p_9}\right)^{k_9} - 1 \right] \right\}^{-\frac{1}{k_5}} \\ \left(\frac{p_{t5}}{p_9}\right)^{k_5} &= \left(\frac{p_{t5}}{p_0}\right)^{k_5} = \left(\frac{56.63}{30}\right)^{0.2481} = 1.171 \\ \pi_n &= \{1.171 - 0.95[1.171 - 1]\}^{-\frac{1}{0.2481}} = 0.9663 \\ p_{t9} &= p_{t5}\pi_n = 56.63 \cdot 0.9663 \cdot 10^3 = 54.72kPa \qquad \frac{p_{t9}}{p_9} = \frac{54.72}{30} = 1.824 \\ \psi_9 &= \left(\frac{p_{t9}}{p_9}\right)^{k_5} = 1.824^{0.2481} = 1.161 \qquad M_9 = \sqrt{\frac{2}{\gamma_5 - 1}} [\psi_9 - 1] = \sqrt{\frac{2}{.33}} [1.161 - 1] = 0.9873 \\ M_9 &< 1 \to p_9 = p_0 \text{ (OK)} \\ T_9 &= T_{t9}/\psi_9 = T_{t5}/\psi_9 = 837.1/1.161 = 721.1K \\ a_9 &= \sqrt{\gamma_5 R_5 T_9} = 1.33 \cdot 285.8 \cdot 721.1 = 523.6m/s \\ V_9 &= M_9 \cdot a_9 = 0.9873 \cdot 523.6 = 516.9m/s \qquad \frac{V_9}{a_0} = \frac{516.9}{321.9} = 1.606 > M_0 \quad (OK) \end{split}$$

## Propeller

$$\frac{\mathcal{P}_{s}}{\dot{m}_{0}} = (1+f)\eta_{gb}\eta_{m_{tL}}(1-\tau_{tL})c_{p5}T_{t45} = \frac{\mathcal{P}_{s}}{\dot{m}_{0}} = 1.026 \cdot 0.995 \cdot 0.99 \cdot (1-0.7322) \cdot 1152 \cdot 1143 = 356.4 \frac{kJ}{kg}$$

# Spinta

$$\begin{aligned} \frac{F_{u.c}}{\dot{m}_0 a_0} &= (1+f) \frac{V_{9.e}}{a_0} - M_0 = 1.026 \cdot 1.606 - 0.82 = 0.8270 \\ \frac{F_{u.p}}{\dot{m}_0 a_0} &= \frac{\eta_{prop} \mathcal{P}_s}{\dot{m}_0 V_0 a_0} = \frac{0.85 \cdot 356.4}{263.9 \cdot 321.9} 10^3 = 3.565 \\ \frac{F_u}{\dot{m}_0 a_0} &= \left(\frac{F_{u.c}}{\dot{m}_0 a_0} + \frac{F_{u.0}}{\dot{m}_0 a_0}\right) = 0.8279 + 3.565 = 4.392 \\ TSFC &= \frac{f}{F_u/\dot{m}_0} = \frac{0.02556 \cdot 10^3}{4.392 \cdot 321.9} = 0.01808 \frac{g}{s} \frac{1}{N} \\ \eta_{th} &= \frac{a_0^2 [(1+f)V_{9.e}^2/a_0^2 - M_0^2] + 2\mathcal{P}_s/\dot{m}_0}{2fQ_R} = \\ \eta_{th} &= \frac{321.9^2 [1.026 \cdot 0.8279^2 - 0.82^2] + 2 \cdot 356.4}{2 \cdot 0.02556 \cdot 42.0 \cdot 10^6} = \frac{9.171 \cdot 10^5}{2.147 \cdot 10^6} = 0.4271 \\ \eta_p &= \frac{2 \frac{F_u}{\dot{m}_0 a_0} a_0 V_0}{a_0^2 [(1+f)V_{9.e}^2/a_0^2 - M_0^2] + 2\mathcal{P}_s/\dot{m}_0} = \frac{2 \cdot 4.392 \cdot 263.9 \cdot 321.9}{9.171 \cdot 10^5} = 0.8138 \end{aligned}$$

 $\eta_0 = \eta_{th} \eta_p = 0.4271 \cdot 0.8138 = 0.3476$ 

L	0.20571			0.24012				T I	I
k	0.28571			0.24812	1.1.11.1.1				
R	286.857			285.835					
a0	321.9	m/s	V0	263.9	m/s				
$\tau_r = T_{t0} = 0$	1.13448								
Section	с	tH	tL	λ		tH	tL		
τ	3.01665	0.69292	0.73216	7.33809	π	0.15754	0.23161		
Section	0	2	3	4	4.5	5	9		
Tt	292.7	292.696	883.0	1650	1143.32	837.102	837.102		
pt	46,656	46,190	1.62E+06	1.55E+06	244,499	56,629	54,722		
Core		f	0.02556						
Pt9/p9	M9	M9 Eff	Tt9/T9	Р9	po/p9				
1.82407	0.98729	0.98729	1.16083	30000	1				
Т9	a9	V9	V9/a0	V9/a0 eff	F/ma0	Fc/Ft			
721.122	523.585	516.931	1.60593	1.60593	0.82698	0.18828			
Prop									
PS/mo					F/ma0	FP/Ft			
356,378	J/kg				3.56535	0.81172			
Num	Section	t	th	р	0	TSFC*1e3	F/ma0		
9.17E+05	η	0.83491	0.42712	0.8138	0.34759	0.01808	4.39233		
Calcolo ite	vrativo reno	dimento TL	nartendo	la eTi					
		$\tau$	$\eta_{\tau L}$	τ	$\eta_{TL}$	τ	n	τ	
	$\eta_{TL}$	-	-		-		112	•	
0.1227	1	0.69564							
	0.88	0.73216	0.88	0.73216	0.88	0.73216	0.88	0.73216	
Calcolo $\pi_n$ partendo da $\eta_n$									
Tt5/T0	1.17074	$\pi_n$	0.96632						