# Discrete Event Systems and Supervisory Control

**Course introduction** 

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- Course name → Discrete event systems and supervisory control
- Part of Advanced control engineering
- Included in the Automation & control engineering curricula



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- If needed we can meet on Teams → Tue 14:30-16:30



### Study of dynamic systems modelled as Discrete Event Systems (DES)





- Study of dynamic systems modelled as Discrete Event Systems (DES)
  - nonlinear...
  - ....with discrete state space...
  - ...whose dynamic is driven by the occurrence of *asynchronous* events over time

## Modelling logical DES



#### Formal languages

A logical DES can be seen as a formal language generator

The events that drive the system dynamic can be regarded as letters of an alphabet E





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- $\blacksquare$  The system itself can be regarded as a generator of words  $\rightarrow$  a generator (recognizer) of a formal language



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- The system itself can be regarded as a generator of words  $\rightarrow$  a generator (recognizer) of a formal language
- Different tools can be used to model DES at the logical level: queue systems, look-up-tables, automata, Petri nets
- Some of this tools can be also extended to study *timed* DES: timed automata and timed Petri nets, Markov chains, (max,+) algebra,...

## Modelling logical DES





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## **Examples**







There are analysis and synthesis tasks that cannot be practically performed when dealing with large scale/complex systems, if these are modelled using differential equations (ODEs)

$$\dot{x}(t) = f(x(t), u(t), t),$$

$$y(t) = g(x(t), u(t), t).$$
Inputs u(t)
Process
to be modelled
Outputs y(t)



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- The DES framework permits to move to a higher level of abstraction, where (some) physical details can be neglected
- When this is not possible some hybrid approaches are possible (both for modelling and control)

### Bestiarium of dynamical systems





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## Bestiarium of dynamical systems





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## The DES research community



- Researchers in this field have different backgrounds: computer science, information theory, operations research, control & automation
- Most of the concepts originated in the computer science community (some date back to Turing!)
- These concepts have been brought in the control community in the 80's by Ramadge and Wonham (Supervisory Control Theory, SCT)
- Even earlier, in the mid 70's, Petri nets were used to derive the Grafcet programming language, which is used in PLCs (nowadays known as SFC)

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- Even earlier, in the mid 70's, Petri nets were used to derive the Grafcet programming language, which is used in PLCs (nowadays known as SFC)
- The jargon adopted in this course is the one usually adopted by the automation-oriented researchers, as well as most of the reported results have been published on control and automation journals

W. M. Wonham, K. Cai, K. Rudie

Supervisory control of discrete-event systems: A brief history Annual Reviews in Control, 2018



#### 1 Introduction (this lesson)

#### 2 Logic DES (deterministic & nondeterministic)

- Languages & automata
- Petri nets
- 3 Timed DES (just some hints)
- 4 Supervisory control
- 5 Privacy and security in DES

### **Textbooks**

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#### © 2008

### Introduction to Discrete Event Systems

Authors: Cassandras, Christos G., Lafortune, Stéphane

#### Lecture Notes in Control and Information Sciences

@ 2013



#### Control of Discrete-Event Systems

Automata and Petri Net Perspectives

Editors: Seatzu, Carla, Silva, Manuel, van Schuppen, Jan H. (Eds.)

### ...and some papers :)











....to be presented/discussed during....





- ....to be presented/discussed during....
- ...Oral exam





- ....to be presented/discussed during....
- ...Oral exam

#### A single mark will be given for Advanced control engineering





- ....to be presented/discussed during....
- ...Oral exam
- A single mark will be given for Advanced control engineering
  - Marks achieved in Discrete event systems and supervisory control and Control of complex systems and networks will be averaged

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