

# Discrete Event Systems, Languages and Automata

From observability to privacy and security in discrete event systems

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- 2 Formal languages
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  - Operations on languages
- 3 Languages and automata
  - Operations on automata
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- 5 A glimpse of Supervisory Control Theory
- 6 Software tools

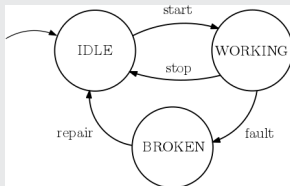
- Study of dynamic systems modelled as Discrete Event Systems (DES)
  - nonlinear. . .
  - . . .with discrete state space. . .
  - . . .whose dynamic is driven by the occurrence of *asynchronous* events over time
- *Uncertain* DES, where the main source of uncertainty is due to the occurrence of *unobservable events*
- This framework can be used to study fault-detection and secrecy problems when the system of interest can be modelled as a logical DES

## Formal languages

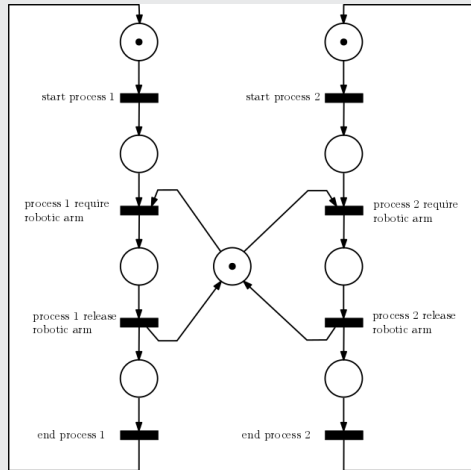
A logical DES can be seen as a formal language *generator*

- The events that drive the system dynamic can be regarded as *letters of an alphabet  $E$*
- The system trajectories become *words (strings, sequences)*
- The system itself can be regarded as a generator of words  $\rightarrow$  a *generator (recognizer) of a formal language*
- Different tools can be used to model DES at the logical level: queue systems, look-up-tables, automata, Petri nets
- Some of this tools can be also extended to study *timed* DES: timed automata and timed Petri nets, Markov chains,  $(\max, +)$  algebra,...

## Automata



## Petri nets



FLEXIBLE  
MANUFACTURING  
SYSTEMS (FMS)



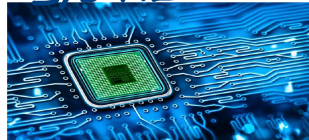
TRAFFIC  
SYSTEMS



COMMUNICATION  
PROTOCOLS

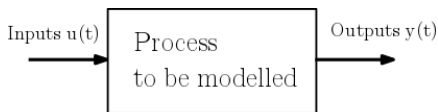


LARGE SCALE  
SYSTEMS

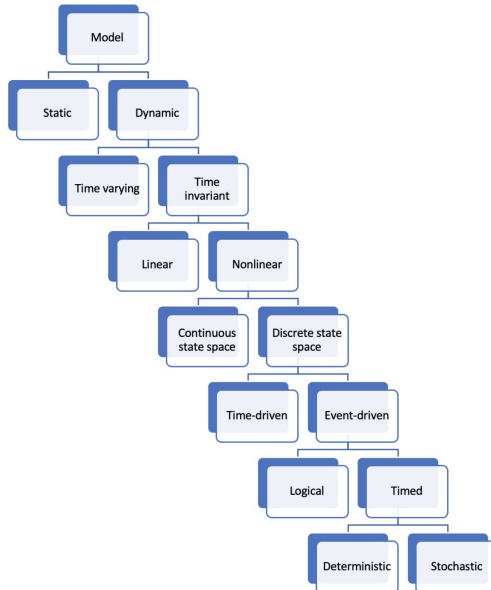


- There are analysis and synthesis tasks that cannot be practically performed when dealing with large scale/complex systems, if these are modelled using differential equations (ODEs)

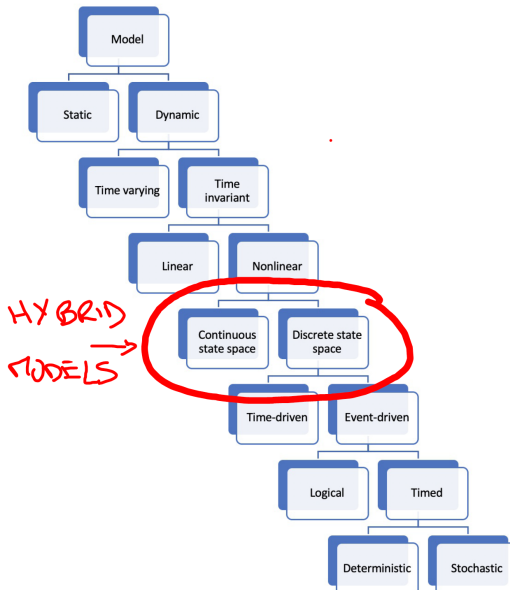
$$\dot{x}(t) = f(x(t), u(t), t),$$
$$y(t) = g(x(t), u(t), t).$$



- The DES framework permits to move to a higher level of abstraction, where (some) physical details can be neglected
- When this is not possible some hybrid approaches are possible (both for modelling and control)







- Researchers in this field have different backgrounds: computer science, information theory, operations research, control & automation
- **Most of the concepts originated in the computer science community (some date back to Turing!)**
- These concepts have been brought in the control community in the 80's by Ramadge and Wonham (**Supervisory Control Theory, SCT**)
- Even earlier, in the mid 70's, Petri nets were used to derive the Grafset programming language, which is used in PLCs (nowadays known as SFC)
- The *jargon* adopted in this course is the one usually adopted by the *automation-oriented* researchers, as well as most of the reported results have been published on control and automation journals



W. M. Wonham, K. Cai, K. Rudie

Supervisory control of discrete-event systems: A brief history

*Annual Reviews in Control, 2018*

- 1 Discrete Event Systems (DES), Languages and Automata (**this lesson**)
- 2 Petri nets (PNs) and their twofold representation to model DES
- 3 MILP and ILP formulations: logical conditions, binary variables “do everything”, and variable connecting (**prof. Claudio Sterle**)
- 4 Adding uncertainty: unobservable events and observers for finite state automata and PNs
- 5 Augmenting the observers: diagnosability of prefix-closed languages, diagnosers and the fault detection for finite state automata (**prof. Francesco Basile**)
- 6 Diagnosability and fault detection in PNs - Part I: graph-based approaches (**prof. Francesco Basile**)
- 7 Diagnosability and fault detection in PNs - Part II: algebraic approaches for bounded systems
- 8 Security issues in DES: non-interference and opacity
- 9 Non-interference and opacity enforcement
- 10 Open issues

-  C. G. Cassandras and S. Lafortune,  
Introduction to Discrete Event Systems  
Springer, 2008
-  C. Seatzu, M. Silva, J. H. van Schuppen (eds.),  
Control of Discrete-Event Systems  
Springer, 2013
-  Some papers :)

- 1 Discrete Event Systems (DES), Languages and Automata**
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- Given a DES, the events that may occur can be seen as elements (*symbols*) of an **alphabet**  $E$  set

$$E = \{a, b, c, \dots\},$$

where the symbols  $a, b, c, \dots$  are used to denote events

- A **word** (**string**, **trace**)  $w$  is a sequence of event of **finite length**

Example:  $w = e^1 e^2 e^3 = aab$

- $|w|$  denotes the length of a word is denoted (some authors use  $\|w\|$ )
- $\varepsilon$  denotes the **empty word** or **silent event**, i.e.  $|\varepsilon| = 0$

- A language  $L$  defined over an alphabet  $E$  is a set of words defined on the symbols of  $E$
- **The cardinality of a language  $L$  can be either finite or infinite**
- Being  $E = \{a, b, c\}$ 
  - $L_1 = \{\varepsilon, a, abb\}$
  - $L_2 = \{\text{all words that starts with the event } a\}$
  - $L_3 = \{\varepsilon, b, b, bab\}$

- The key operation among words is the **concatenation**
- The concatenation of two words  $w_1$  and  $w_2$  is the new string  $w$  consisting of the events in  $w_1$  immediately followed by the events in  $w_2$ , and it is denoted  $w = w_1 w_2$
- In general, if  $u = w_1 w_2$  and  $v = w_2 w_1$  it does not necessarily follow that  $u = v \rightarrow$  **concatenation is not commutative**
- The empty word  $\varepsilon$  is the identity element of concatenation, i.e.  $w\varepsilon = \varepsilon w = w$
- Given a word  $w = tuv$  the following terminology is adopted
  - $t$  is called **prefix** of  $w$
  - $u$  is called **substring** of  $w$
  - $v$  is called **suffix** of  $w$



- The **Kleene closure** of an alphabet  $E$  is the set of all the finite-length words defined on the elements of  $E$  and is denoted with  $E^*$
- The empty word  $\varepsilon$  is always contained in  $E^*$
- Example:
  - $E = \{\alpha, \beta\}$
  - $E^* = \{\varepsilon, \alpha, \beta, \alpha\alpha, \alpha\beta, \beta\alpha, \beta\beta, \alpha\alpha\alpha, \dots\}$
- $E^*$  contains every possible language  $L$  defined on the symbols of  $E$

- Being sets, all the set operations are defined also on languages:
  - **union**  $L_1 \cup L_2$
  - **intersection**  $L_1 \cap L_2$
  - **difference**  $L_1 \setminus L_2$
  - **complement with respect to**  $E^* \setminus L$
- Language specific operations are
  - Concatenation (of languages)
  - Prefix-closure
  - Kleen-closure

Given two languages  $L_a, L_b \subseteq E^*$ , the concatenation  $L_a L_b$  is

$$L_a L_b := \{w \in E^* : w = w_a w_b \text{ with } w_a \in L_a, w_b \in L_b\}$$

- Let  $L \subseteq E^*$ , its prefix-closure is

$$\bar{L} := \{w \in E^* : \exists t \in E^* \text{ such that } wt \in L\}$$

- It is always  $L \subseteq \bar{L}$
- $L$  is said to be **prefix-closed** if  $L = \bar{L}$

- Let  $L \subseteq E^*$ , its Kleene-closure is

$$L^* := \{\varepsilon\} \cup L \cup LL \cup LLL \cup \dots$$

- The Kleene-closure is idempotent, i.e.  $(L^*)^* = L^*$

- Closures comes first. . .
- . . .then concatenations. . .
- . . .finally set operators
- **unless there are brackets**

- Always remember that  $\varepsilon \neq \emptyset$
- If  $L = \emptyset \Rightarrow \bar{L} = \emptyset$
- If  $L \neq \emptyset \Rightarrow \varepsilon \in \bar{L}$
- $\emptyset^* = \{\varepsilon\}$
- $\{\varepsilon\}^* = \{\varepsilon\}$

- (Some) Languages with finite cardinality may be specified by enumerating their words
- (Some) Languages with infinite cardinality may be specified in terms of *word features*, example

$$L = \{all\ the\ words\ that\ start\ with\ \alpha\}$$

- **It would be better to have a formal tool to specify languages, in order to enable *quantitative* methods to solve analysis and synthesis problems**
- **Automata are one of these tools**

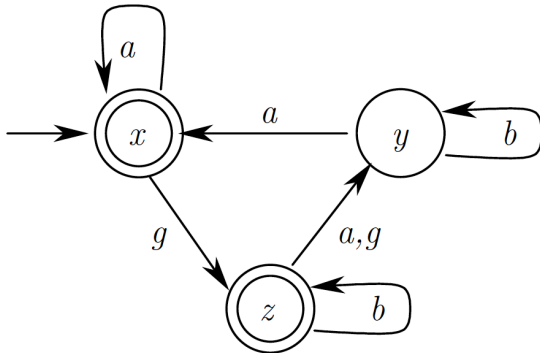


A (logic deterministic) automaton  $G$  is the 6-tuple

$$G = (X, E, f, \Gamma, x_0, X_m)$$

where

- $X$  is the *discrete* state space. If the cardinality of  $X$  is finite, then  $G$  is also referred to as *finite state machine (FSM)* or *finite state automaton*
- $E$  is the set of events associated with the transitions in  $G$
- $f(\cdot, \cdot) : X \times E \mapsto X$  is the *transition function*
- $\Gamma(\cdot) : X \mapsto 2^E$  is the active event function.  $\Gamma(\cdot)$  is implicitly defined by  $f(\cdot, \cdot)$
- $x_0$  is the initial state
- $X_m \subseteq X$  is the the set of *marked* or *final* states (used in the SCT context to deal with non-blocking requirements)



It is common to recursively extend the transition function  $f(\cdot, \cdot)$  from the  $X \times E$  domain to the  $X \times E^*$  one as follows

- $f(x, \varepsilon) := x$  for all  $x \in X$
- $f(x, we) := f(f(x, w), e)$  with  $w \in E^*$  and  $e \in E$

Let  $G = (X, E, f, \Gamma, x_0, X_m)$

## Language generated by $G - \mathcal{L}(G)$

$$\mathcal{L}(G) := \{w \in E^* : f(x_0, w) \text{ is defined}\}$$

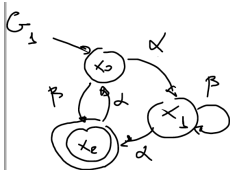
## Language marked by $G - \mathcal{L}_m(G)$

$$\mathcal{L}_m(G) := \{w \in \mathcal{L}(G) : f(x_0, w) \in X_m\}$$

By definition

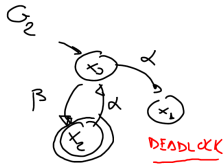
- $\mathcal{L}(G)$  is always prefix-closed, i.e.  $\overline{\mathcal{L}(G)} = \mathcal{L}(G)$
- $\mathcal{L}_m(G) \subseteq \overline{\mathcal{L}_m(G)} \subseteq \mathcal{L}(G)$
- If  $\overline{\mathcal{L}_m(G)} \subset \mathcal{L}(G)$ , then there are *deadlock* and/or *livelock* in  $G$
- If  $\overline{\mathcal{L}_m(G)} = \mathcal{L}(G)$ , then  $G$  is said to be *non-blocking*

# Examples of blocking automata



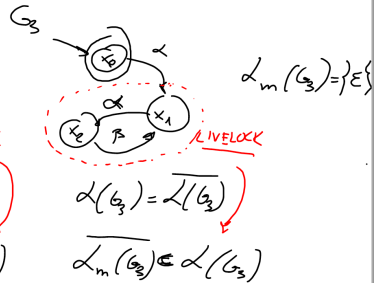
$$\mathcal{L}(G_1) = \overline{\mathcal{L}(G_1)}$$

$$\underline{\mathcal{L}_m(G_1)} = \mathcal{L}(G_1)$$



$$\mathcal{L}(G_2) = \overline{\mathcal{L}(G_2)}$$

$$\underline{\mathcal{L}_m(G_2)} \in \mathcal{L}(G_2)$$



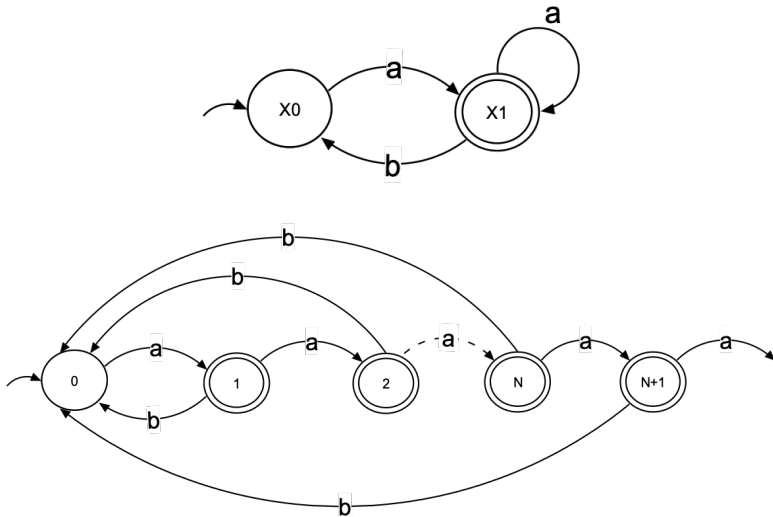
$$\mathcal{L}(G_3) = \overline{\mathcal{L}(G_3)}$$

$$\underline{\mathcal{L}_m(G_3)} \in \mathcal{L}(G_3)$$

Automata  $G_1$  and  $G_2$  are said to be equivalent if

- $\mathcal{L}(G_1) = \mathcal{L}(G_2)$
- $\mathcal{L}_m(G_1) = \mathcal{L}_m(G_2)$

# Equivalence of automata - Example



Removes all the states that are unreachable from  $x_0$  (and the related transitions) Given  $G = (X, E, f, x_0, X_m)$  the **accessible part of  $G$**   $Ac(G)$  is

$$Ac(G) := (X_{ac}, E, f_{ac}, x_0, X_{ac,m})$$

where

- $X_{ac} = \{x \in X \mid \exists w \in E^* \text{ s.t. } f(x_0, w) = x\}$
- $X_{ac,m} = X_m \cap X_{ac}$
- $f_{ac} = f|_{X_{ac} \times E \rightarrow X_{ac}}$
- The accessible part does not affect nor  $\mathcal{L}(G)$  neither  $\mathcal{L}_m(G)$
- If  $G = Ac(G)$ , then  $G$  is said to be *accessible*



Removes all the states that do not lead to a marked state (and the related transitions) Given  $G = (X, E, f, x_0, X_m)$  the **coaccessible part of  $G$**   $CoAc(G)$  is

$$CoAc(G) := (X_{coac}, E, f_{coac}, x_{0_{coac}}, X_m)$$

where

- $X_{coac} = \{x \in X \mid \exists w \in E^* \text{ s.t. } f(x, w) \in X_m\}$
- $x_{0_{coac}} = x_0$  if  $x_0 \in X_{coac}$ , otherwise  $x_0$  is left undefined
- $f_{coac} = f|_{X_{coac} \times E \rightarrow X_{coac}}$
- By definition  $CoAc(G)$  is always non-blocking, i.e. the generated language is modified in such a way that
  - $\mathcal{L}(CoAc(G)) = \overline{\mathcal{L}_m(CoAc(G))} = \overline{\mathcal{L}_m(G)}$
- If  $G = CoAc(G)$ , then  $G$  is said to be *coaccessible*

- $Trim(G) := CoAc(Ac(G)) = Ac(CoAc(G))$
- If  $G = Trim(G)$ , then  $G$  is said to be *trimmed*
- A trimmed automaton is both accessible and coaccessible

- Let  $G$  be a trimmed automaton with
  - $\mathcal{L}_m(G) = L$
  - $\mathcal{L}(G) = \bar{L}$
- The **complement automaton**  $G^{comp}$  is such that

$$\mathcal{L}(G^{comp}) = E^* \setminus L$$

- 1 Complete the transition function  $f(\cdot, \cdot)$  as follows

$$f_{tot}(x, e) := \begin{cases} f(x, e) & \text{if } e \in \Gamma(x) \\ x_d & \text{otherwise} \end{cases}$$

with  $x_d \notin X_m$  and  $f_{tot}(x_d, e) = x_d \forall e \in E$

- 2 Let

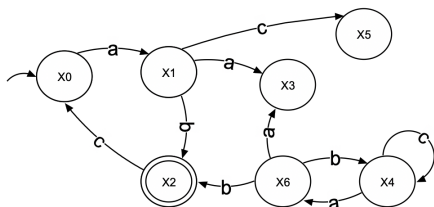
$$G^{comp} = (X \cup \{x_d\}, E, f_{tot}, x_0, X_m^{new})$$

with  $X_m^{new} = (X \cup \{x_d\}) \setminus X_m$

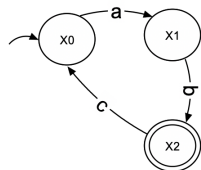
Clearly it is

- $\mathcal{L}(G^{comp}) = E^*$
- $\mathcal{L}_m(G^{comp}) = E^* \setminus \mathcal{L}_m(G)$

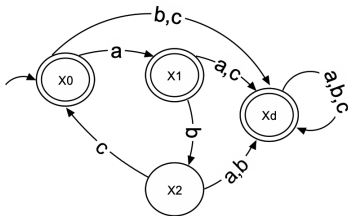
# Example of complement automaton



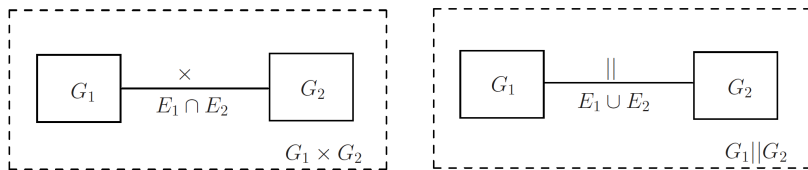
Automaton G



Trimmed automaton



Complement automaton



**Figure:** Cross product  $G_1 \times G_2$  and parallel composition (or concurrent product)  $G_1 \parallel G_2$

Given  $G_1$  and  $G_2$  the **product**  $G_1 \times G_2$  automaton is

$$G_1 \times G_2 := Ac(X_1 \times X_2, E_1 \cap E_2, f, \Gamma_{1 \times 2}, (x_{0_1}, x_{0_2}), X_{m_1} \times X_{m_2})$$

with

$$f((x_1, x_2), e) := \begin{cases} (f_1(x_1, e), f_2(x_2, e)) & \text{if } e \in \Gamma_1(x_1) \cap \Gamma_2(x_2) \\ \text{undefined} & \text{otherwise} \end{cases}$$

$$\text{and } \Gamma_{1 \times 2}(x_1, x_2) = \Gamma_1(x_1) \cap \Gamma_2(x_2)$$

**NOTE:** an event occurs in  $G_1 \times G_2$  if and only if it occurs in both automata  $G_1$  and  $G_2$ . It follows that

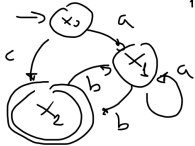
- $\mathcal{L}(G_1 \times G_2) = \mathcal{L}(G_1) \cap \mathcal{L}(G_2)$
- $\mathcal{L}_m(G_1 \times G_2) = \mathcal{L}_m(G_1) \cap \mathcal{L}_m(G_2)$

# Example of cross product



$$E_1 = \{a, b, c\}$$

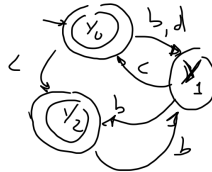
$G_1$



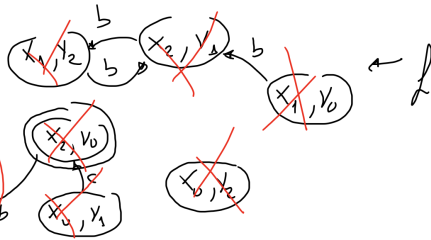
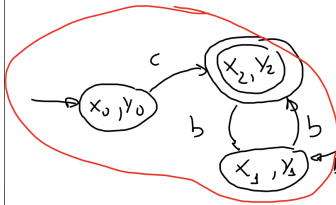
$G_2$

$$E_2 = \{b, c, d\}$$

$$E_1 \cap E_2 = \{b, c\}$$



$$G_1 \times G_2$$





Given  $G_1$  and  $G_2$  the **parallel composition**  $G_1 \parallel G_2$  automaton is

$$G_1 \parallel G_2 := Ac (X_1 \times X_2, E_1 \cup E_2, f, \Gamma_{1 \parallel 2}, (x_{0_1}, x_{0_2}), X_{m_1} \times X_{m_2})$$

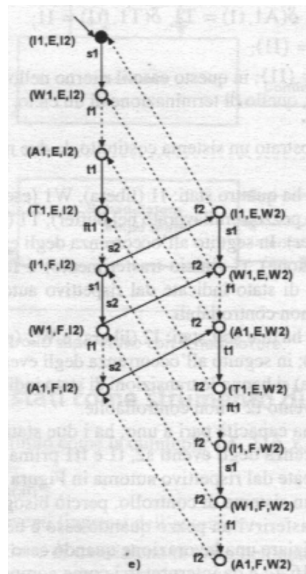
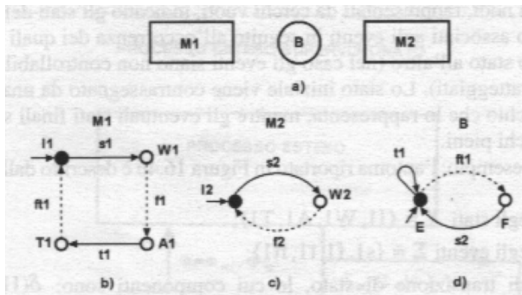
with

$$f((x_1, x_2), e) := \begin{cases} (f_1(x_1, e), f_2(x_2, e)) & \text{if } e \in \Gamma_1(x_1) \cap \Gamma_2(x_2) \\ (f_1(x_1, e), x_2) & \text{if } e \in \Gamma_1(x_1) \setminus E_2 \\ (x_1, f_2(x_2, e), x_2) & \text{if } e \in \Gamma_2(x_2) \setminus E_1 \\ \text{undefined} & \text{otherwise} \end{cases}$$

and

$$\Gamma_{1 \parallel 2}(x_1, x_2) = [\Gamma_1(x_1) \cap \Gamma_2(x_2)] \cup [\Gamma_1(x_1) \setminus E_2] \cup [\Gamma_2(x_2) \setminus E_1]$$

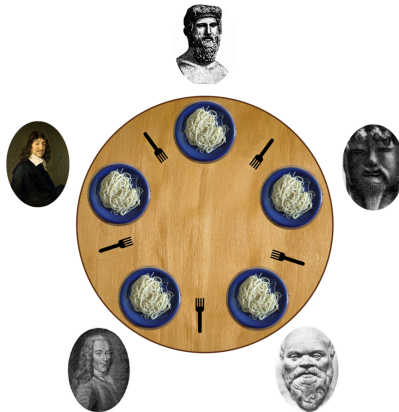
# Example - Simple FMS



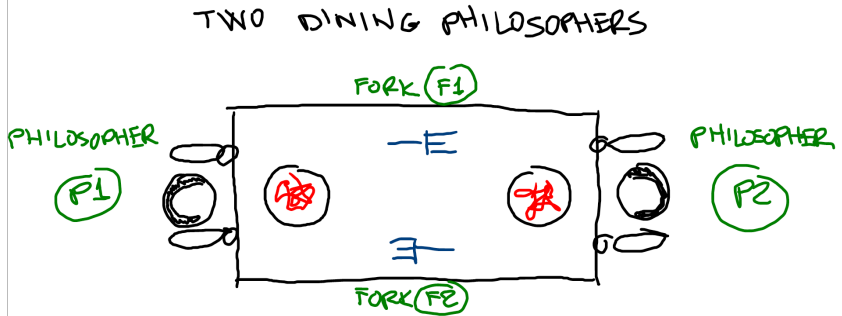
# Dijkstra's dining philosophers problem and the curse of dimensionality



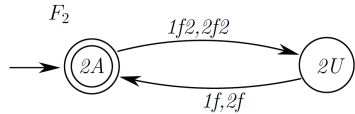
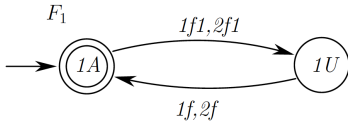
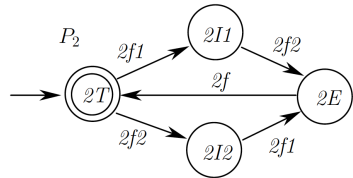
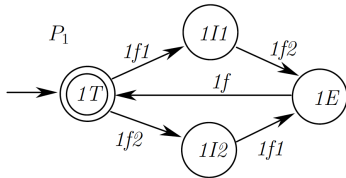
## Dijkstra's dining philosophers problem (1965) Deadlock due to shared resources (the forks)



# Two dining philopoppers

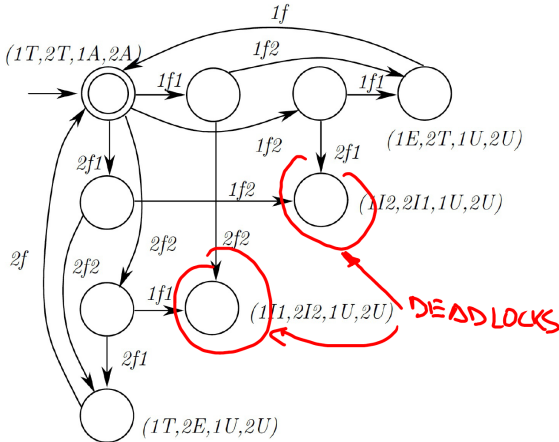


# Modelling philosophers and forks



# The overall system $F1 \parallel F2 \parallel P1 \parallel P2$

$F1 \parallel F2 \parallel P1 \parallel P2 \rightarrow 9$  STATES



- 2 philosophers 2 forks → overall model with 9 states
- 3 philosophers 3 forks → overall model with 504 states
- 4 philosophers 4 forks → overall model with 4.080 states
- 5 philosophers 5 forks → overall model with 32.736 states
- 6 philosophers 6 forks → overall model with 262.080 states → **about 1 minute** to compute the parallel composition on this laptop
- 7 philosophers 7 forks → overall model with 2.097.024 states → **more than 1 hour** to compute the parallel composition on this laptop
- 8 philosophers 8 forks → **GOD KNOWS :)**

- Given the two sets of events  $E_1$  and  $E_2$ , we need to introduce the **projection functions**  $P_i(\cdot)$  and their inverse in order to derive a compact expression for both the generated and marked languages of  $G_1 \parallel G_2$

$$P_i : (E_1 \cup E_2)^* \mapsto E_i^*$$

$$\left\{ \begin{array}{ll} P_i(\varepsilon) := \varepsilon & \\ P_i(e) := e & \text{if } e \in E_i \\ P_i(e) := \varepsilon & \text{if } e \notin E_i \\ P_i(we) := P_i(w)P_i(e) & w \in (E_1 \cup E_2)^* , e \in (E_1 \cup E_2) \end{array} \right.$$

- The projection function will be used also when uncertainty in terms of presence of unobservable events will be considered



- The **inverse projection**  $P_i^{-1}(\cdot)$  is defined as

$$P_i^{-1} : E_i^* \mapsto 2^{(E_1 \cup E_2)^*}$$

$$P_i^{-1}(t) := \{w \in (E_1 \cup E_2)^* : P_i(w) = t\}$$

- While the projection of a word is a (possibly empty) word, **the inverse projection of a word is a language**

- Given a language  $L$  defined over  $E_1 \cup E_2$ , the extensions of the projection functions to  $L$  are

$$P_i(L) := \{t \in E_i^* : \exists w \in L, P_i(w) = t\}$$

- Given a language  $L_i \subseteq E_i^*$  defined over  $E_i (i = 1, 2)$ , the extension of the inverse projection to  $L_i$  is

$$P_i^{-1}(L_i) := \{w \in (E_1 \cup E_2)^* : \exists t \in L_i, P_i(w) = t\}$$

- Note that

$$P_i(P_i^{-1}(L)) = L$$

and that

$$L \subseteq P_i^{-1}(P_i(L))$$

Let  $E_1 = \{a, b\}$  and  $E_2 = \{b, c\}$  and

$$L = \{c, ccb, abc, cacb, cabcbba\}$$

Then

- $P_1(L) = \{\varepsilon, b, ab, abbba\}$
- $P_2(L) = \{c, ccb, bc, cbcbbc\}$
- $P_1^{-1}(\{\varepsilon\}) = \{c\}^*$
- $P_1^{-1}(\{ab\}) = \{c\}^* \{a\} \{c\}^* \{b\} \{c\}^*$
- $P_1^{-1}(P_1(\{abc\})) = P_1^{-1}(\{ab\})$

Language generated by  $G_1 \parallel G_2$

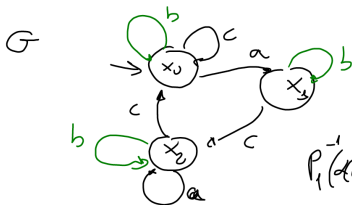
$$\mathcal{L}(G_1 \parallel G_2) = P_1^{-1}(\mathcal{L}(G_1)) \cap P_2^{-1}(\mathcal{L}(G_2))$$

Language marked by  $G_1 \parallel G_2$

$$\mathcal{L}_m(G_1 \parallel G_2) = P_1^{-1}(\mathcal{L}_m(G_1)) \cap P_2^{-1}(\mathcal{L}_m(G_2))$$

$$E_1 = \{a, c\} \subseteq E = \{a, b, c\}$$

$$L \subseteq P_i^{-1}(L)$$



$$\mathcal{L}(G) \subseteq E_1^*$$

$$P_1^{-1}(\mathcal{L}(G)) = \{t \in E^* \mid P_1(t) = s \text{ with } s \in \mathcal{L}(G)\}$$

## Regular expressions over an alphabet $E$ – $RE(E)$

Given the alphabet  $E$ , the **regular expressions** defined over  $E$  are defined as follows

- 1  $\emptyset$  and  $e$ , for all  $e \in E$  are regular expressions
- 2 if  $a, b \in RE(E)$  then the following are regular expressions
  - $a \cup b$  (union)
  - $ab$  and  $ba$  (concatenation)
  - $a^*$  and  $b^*$  (Kleene closure)
- 3 There are no other regular expressions than the ones defined by rules 1 and 2

## Regular languages – $Reg(E)$

In words, the class of **regular languages** defined over  $E$  –  $Reg(E)$  – is the class of languages that can be *built* by using regular expressions

Let us denote with  $Rec(E)$  the class of recognizable languages, i.e. the languages that can be marked by finite state automata.

## Kleene Theorem (1936)

$$Rec(E) = Reg(E)$$



S. Haar, T. Masopust

Languages, decidability, and complexity  
in *Control of Discrete-Event Systems*  
Springer, 2013



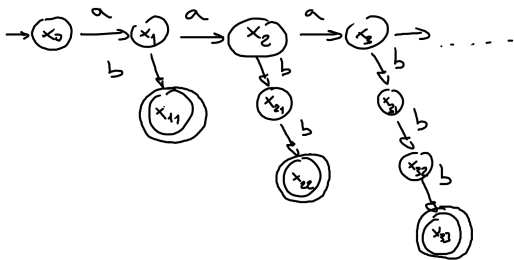
# Are all the languages regular?

Clearly, the answer is **NO!**

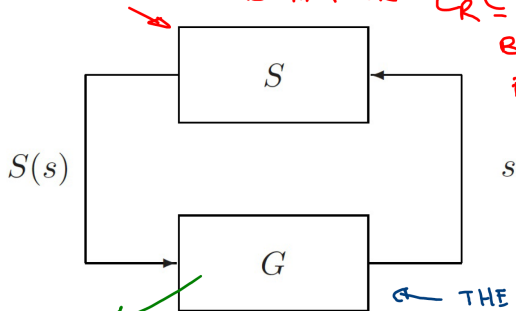
$$L = \{w \in E^* \text{ s.t. } w = a^n b^n, n > 0\} \quad E = \{a, b\}$$

$$a^n = \underbrace{aa \dots a}_n$$

THIS IS NOT  
A REGULAR LANGUAGE



THE SUPERVISOR  $\rightarrow$  TRIES TO FORCE A REQUIRED BEHAVIOUR  $L_R = \mathcal{L}(G)$  BY DISABLING EVENTS



$\mathcal{L}(G)$   
IS THE OPEN-LOOP BEHAVIOUR

THE PLANT MODEL  
(CAN BE OBTAINED BY COMPOSITION OF SUBSYSTEMS)

A nice tutorial lecture can be found here

<https://www.control.utoronto.ca/~wonham/Research.html>


## Proposed (1982): Supervisory Control Theory (Peter Ramadge & WMW)

- **Automaton** representation
  - **internal** state descriptions for concrete modeling and computation
- **Language** representation
  - **external** i/o descriptions for implementation-independent concept formulation
- Simple **control** 'technology'

## Community Response

Anonymous Referees (1983-87)

- **[Leading control journal]**  
"Automata have no place in control engineering."  
**Reject!**
- **[Leading computer journal]**  
"Finite automata and regular languages are nothing new at best and trivial at worst."  
**Reject!**
- **SIAM J. Control & Optimization**  
"So this is optimal control? Well..."  
**Accept**

- Many tools – Most of them developed by academic groups
  - TCT (Wonham's group @ University of Toronto)
    - <https://www.control.utoronto.ca/~wonham/Research.html>
  - **UMDES-DESUMA** (Lafortune's group @ University of Michigan)
    - <https://wiki.eecs.umich.edu/desuma/index.php/DESUMA>
  - Supremica (Chalmers University)
    - <https://supremica.org/>
  - ...
- Some tools includes automatic code generation for industrial devices (IEC-61131 compliant)
- For those who are interested a nice (and not too old) overview can be found here
  -  **L. Preischadt Pinheiro et al.**  
Nadzoru: A Software Tool for Supervisory Control of Discrete Event Systems  
*5th IFAC Int. Workshop on Dependable Control of Discrete Systems, 2015*

UMDES allows to specify automata as .fsm text files

## Example

4 ← *number of states*

I 1 1 (*state name, marked state flag, number of output transitions*)

s W c o (*output event, new state, controllability flag, observability flag*)

W 0 1

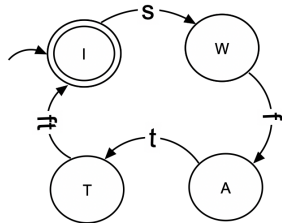
f A u c o

A 0 1

t T c o

T 0 1

ft I u c o



- `acc` → accessible part  $Ac(G)$
- `co_acc` → coaccessible part  $CoAc(G)$
- `trim` → trim automaton  $Trim(G)$
- `comp_fsm` → complement automaton  $G^{comp}$
- `product` → cross product  $G_1 \times G_2$
- `par_comp` → parallel composition  $G_1 \parallel G_2$

For those of you who like GUI, there is DESUMA (or Supremica or ...)

The screenshot shows the DESUMA software interface. The main window displays a state transition diagram with states s0 through s15. State s0 is the initial state, indicated by a blue circle. Transitions are labeled trans1, trans2, trans3, and trans4. State s12 has a self-loop labeled trans3. The right-hand panel shows the 'Automata' and 'Properties' tabs. The 'Properties' tab displays the following information:

**Automata Properties:**

- Name: New1
- Editable: true
- States: 15
- Transitions: 4

**STATES Table:**


State Name	Marked	Initial
s0	<input type="checkbox"/>	<input checked="" type="checkbox"/>
s1	<input type="checkbox"/>	<input type="checkbox"/>
s10	<input checked="" type="checkbox"/>	<input type="checkbox"/>
s11	<input type="checkbox"/>	<input type="checkbox"/>
s12	<input checked="" type="checkbox"/>	<input type="checkbox"/>
s13	<input type="checkbox"/>	<input type="checkbox"/>
s14	<input type="checkbox"/>	<input type="checkbox"/>
s2	<input type="checkbox"/>	<input type="checkbox"/>
s3	<input type="checkbox"/>	<input type="checkbox"/>
s4	<input checked="" type="checkbox"/>	<input type="checkbox"/>
s5	<input type="checkbox"/>	<input type="checkbox"/>
s6	<input type="checkbox"/>	<input type="checkbox"/>
s7	<input checked="" type="checkbox"/>	<input type="checkbox"/>
s8	<input type="checkbox"/>	<input type="checkbox"/>
s9	<input checked="" type="checkbox"/>	<input type="checkbox"/>

**EVENTS Table:**

Name	Observed	Control
trans1	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
trans2	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
trans3	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
trans4	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>

**COMMAND:** [s0 s5 trans4  
Transition trans4 added.

Chapter 2 (up to section 2.3.2) in

-  **C. G. Cassandras and S. Lafortune**  
Introduction to Discrete Event Systems  
Springer, 2008



# Discrete Event Systems, Languages and Automata

From observability to privacy and security in discrete event systems

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