

Risolvere i seguenti sistemi lineari:

$$1. \begin{cases} -x + y + 5z = 0 \\ x - 4z = 1 \\ x + y + z = 3 \end{cases} \quad 2. \begin{cases} 5x + y - 3z = 0 \\ 10x + 2y - 4z = 1 \\ 15x + 3y - 7z = 1 \end{cases} \quad 3. \begin{cases} 3x + y + z = 0 \\ x + 2z = 1 \\ 2x + 4z = -2 \end{cases} \quad 4. \begin{cases} 3x + y = 0 \\ x - 2z = 1 \\ -2x + 4z = -2 \end{cases}$$

$$5. \begin{cases} x + y = 0 \\ y - 4z = 1 \\ 2x - z = 3 \end{cases} \quad 6. \begin{cases} 5x + 7z = 0 \\ y - 4z = 1 \\ 5x + y + 3z = 1 \end{cases} \quad 7. \begin{cases} x - 3y + 2z = 0 \\ x - 4z = 3 \\ 2x - y = 3 \end{cases} \quad 8. \begin{cases} x + 5y - 3z = 0 \\ x + 5y - 4z = 1 \\ 2x + 10y - 7z = 1 \end{cases}$$

$$9. \begin{cases} 3x - y = 0 \\ 6x - 2y = 0 \\ x - 3y - 2z = 3 \end{cases} \quad 10. \begin{cases} y - 3z = 2 \\ x + 3z = 3 \\ x + y = 4 \end{cases} \quad 11. \begin{cases} x + y + z = 2 \\ x + 3z = 3 \\ 3x + 2y + 5z = 7 \end{cases} \quad 12. \begin{cases} x - y + 2z = 2 \\ 2x - 3z = 3 \\ -2y + 7z = 1 \end{cases}$$

$$13. \begin{cases} 3x - y = 0 \\ 9x - 3y + z = 0 \\ -6x + 2y - z = 0 \end{cases} \quad 14. \begin{cases} 2x + 3y + 5z = 0 \\ x - 2z = 3 \\ 2x - y + z = 1 \end{cases} \quad 15. \begin{cases} x + y - z = 2 \\ x + 2z = 3 \\ 2x + y + z = 1 \end{cases} \quad 16. \begin{cases} x + y + 3z = 0 \\ y + 2z = 1 \\ 2x - z = -2 \end{cases}$$

$$17. \begin{cases} x - y + 2z = 0 \\ x - y + z = 1 \\ 4x - 4y + 5z = 3 \end{cases} \quad 18. \begin{cases} -x + 2y + 2z = 1 \\ 3x - 6y + z = 1 \\ 2x - 4y + 3z = 2 \end{cases} \quad 19. \begin{cases} x + 2y + 2z = 0 \\ x + y - z = 3 \\ 3x + 4y = 6 \end{cases} \quad 20. \begin{cases} x - y - 2z = 0 \\ 4x - y - z = -3 \\ 6x - 3y - 5z = -3 \end{cases}$$

$$21. \begin{cases} 5x - z = 1 \\ x + y = 3 \\ 4x - y - z = 7 \end{cases} \quad 22. \begin{cases} x + z = 0 \\ y + 4z = 1 \\ 2x - y - z = 3 \end{cases} \quad 23. \begin{cases} -x + 3y + 2z = 1 \\ 2x - 6y + 2z = 0 \\ -3x + 9y = 1 \end{cases} \quad 24. \begin{cases} 5x + 3y - z = 1 \\ 10x + 6y + 2z = 4 \\ -5x - 3y - 3z = -3 \end{cases}$$

$$25. \begin{cases} 2x - y + 3z = 2 \\ x + 3z = 3 \\ x - y = 2 \end{cases} \quad 26. \begin{cases} -x + y + z = 1 \\ x + 3z = 3 \\ 2x + y + 6z = 6 \end{cases} \quad 27. \begin{cases} 3x + y + z = 0 \\ x - y + z = 0 \\ 5x - y + 3z = 0 \end{cases} \quad 28. \begin{cases} -x + y - 2z = 1 \\ x + y + 3z = 3 \\ x + y + 4z = 4 \end{cases}$$

$$29. \begin{cases} 2x - y - 2z = 1 \\ 4x - 2y + 2z = 1 \\ 2x - y - 8z = 2 \end{cases} \quad 30. \begin{cases} y - 3z = 2 \\ x + 3z = 3 \\ x + 2y = 4 \end{cases}$$

Risposte:

1. $\left\{ \left(2, \frac{3}{4}, \frac{1}{4} \right) \right\}$ 2. $\left\{ \left(x, \frac{3}{2} - 5x, \frac{1}{2} \right) : x \in \mathbf{R} \right\} = \left\{ \left(\frac{3}{10} - \frac{y}{5}, y, \frac{1}{2} \right) : y \in \mathbf{R} \right\}$ 3. \emptyset
4. $\left\{ \left(x, -3x, -\frac{1}{2} + \frac{x}{2} \right) : x \in \mathbf{R} \right\} = \left\{ \left(-\frac{y}{3}, y, -\frac{1}{2} - \frac{y}{6} \right) : y \in \mathbf{R} \right\} = \{(1 + 2z, -3 - 6z, z) : z \in \mathbf{R}\}$
5. $\left\{ \left(\frac{11}{9}, -\frac{11}{9}, -\frac{5}{9} \right) \right\}$
6. $\left\{ \left(x, 1 - \frac{20x}{7}, -\frac{5x}{7} \right) : x \in \mathbf{R} \right\} = \left\{ \left(\frac{7}{20} - \frac{7y}{20}, y, -\frac{1}{4} + \frac{y}{4} \right) : y \in \mathbf{R} \right\} = \left\{ \left(-\frac{7z}{5}, 1 + 4z, z \right) : z \in \mathbf{R} \right\}$
7. $\left\{ \left(\frac{5}{3}, \frac{1}{3}, -\frac{1}{3} \right) \right\}$ 8. $\left\{ \left(x, -\frac{3}{5} - \frac{x}{5}, -1 \right) : x \in \mathbf{R} \right\} = \{(-3 - 5y, y, -1) : y \in \mathbf{R}\}$
9. $\left\{ \left(x, 3x, -\frac{3}{2} - 4x \right) : x \in \mathbf{R} \right\} = \left\{ \left(\frac{y}{3}, y, -\frac{3}{2} - \frac{4y}{3} \right) : y \in \mathbf{R} \right\} = \left\{ \left(-\frac{3}{8} - \frac{z}{4}, -\frac{9}{8} - \frac{3z}{4}, z \right) : z \in \mathbf{R} \right\}$
10. \emptyset 11. $\left\{ \left(x, 1 - \frac{2x}{3}, 1 - \frac{x}{3} \right) : x \in \mathbf{R} \right\} = \left\{ \left(\frac{3}{2} - \frac{3y}{2}, y, \frac{1}{2} + \frac{y}{2} \right) : y \in \mathbf{R} \right\} = \{(3 - 3z, -1 + 2z, z) : z \in \mathbf{R}\}$
12. $\left\{ \left(x, -4 + \frac{7x}{3}, -1 + \frac{2x}{3} \right) : x \in \mathbf{R} \right\} = \left\{ \left(\frac{12}{7} + \frac{3y}{7}, y, \frac{1}{7} + \frac{2y}{7} \right) : y \in \mathbf{R} \right\} = \left\{ \left(\frac{3}{2} + \frac{3z}{2}, -\frac{1}{2} + \frac{7z}{2}, z \right) : z \in \mathbf{R} \right\}$
13. $\{(x, 3x, 0) : x \in \mathbf{R}\} = \left\{ \left(\frac{y}{3}, y, 0 \right) : y \in \mathbf{R} \right\}$ 14. $\left\{ \left(\frac{5}{4}, \frac{5}{8}, -\frac{7}{8} \right) \right\}$ 15. \emptyset 16. $\{(-1, 1, 0)\}$
17. $\{(x, -2 + x, -1) : x \in \mathbf{R}\} = \{2 + y, y, -1) : y \in \mathbf{R}\}$
18. $\left\{ \left(x, -\frac{1}{14} + \frac{x}{2}, \frac{4}{7} \right) : x \in \mathbf{R} \right\} = \left\{ \frac{1}{7} + 2y, y, \frac{4}{7} \right\} : y \in \mathbf{R}$
19. $\left\{ \left(x, \frac{3}{2} - \frac{3x}{4}, -\frac{3}{2} + \frac{x}{4} \right) : x \in \mathbf{R} \right\} = \left\{ \left(2 - \frac{4y}{3}, y, -1 - \frac{y}{3} \right) : y \in \mathbf{R} \right\} = \{(6 + 4z, -3 - 3z, z) : z \in \mathbf{R}\}$
20. $\{(x, 6 + 7x, -3 - 3x) : x \in \mathbf{R}\} = \left\{ \left(-\frac{6}{7} + \frac{y}{7}, y, -\frac{3}{7} - \frac{3y}{7} \right) : y \in \mathbf{R} \right\} = \left\{ \left(-1 - \frac{z}{3}, -1 - \frac{7z}{3}, z \right) : z \in \mathbf{R} \right\}$
21. \emptyset 22. $\{(-4, -15, 4)\}$ 23. $\left\{ \left(x, \frac{1}{9} + \frac{x}{3}, \frac{1}{3} \right) : x \in \mathbf{R} \right\} = \left\{ \left(-\frac{1}{3} + 3y, y, \frac{1}{3} \right) : y \in \mathbf{R} \right\}$
24. $\left\{ \left(x, \frac{1}{2} - \frac{5x}{3}, \frac{1}{2} \right) : x \in \mathbf{R} \right\} = \left\{ \left(\frac{3}{10} - \frac{3y}{5}, y, \frac{1}{2} \right) : y \in \mathbf{R} \right\}$ 25. \emptyset 26. $\{(0, 0, 1)\}$
27. $\{(x, -x, -2x) : x \in \mathbf{R}\} = \{(-y, y, 2y) : y \in \mathbf{R}\} = \left\{ \left(-\frac{z}{2}, \frac{z}{2}, z \right) : z \in \mathbf{R} \right\}$ 28. $\left\{ \left(-\frac{3}{2}, \frac{3}{2}, 1 \right) \right\}$
29. $\left\{ \left(x, -\frac{2}{3} + 2x, -\frac{1}{6} \right) : x \in \mathbf{R} \right\} = \left\{ \left(\frac{1}{3} + \frac{y}{2}, y, -\frac{1}{6} \right) : y \in \mathbf{R} \right\}$ 30. $\{(6, -1, -1)\}$