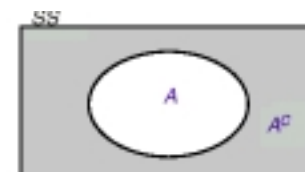


1.  $A \cup B = B \cup A$  Commutative Rule
2.  $(A \cup B) \cup C = A \cup (B \cup C)$  Associative Rule
3.  $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$  Distributive Rule
4.  $(A^c)^c = A$  Complement of a Complement Rule
5.  $(A \cap B)^c = A^c \cup B^c$  DeMorgan's Rule
6.  $A \cap A^c = \emptyset$  where  $\emptyset$  denotes the null set
7.  $A \cap S = A$



**FIGURE 2.10** Venn diagram depiction of the region corresponding to the complement of event  $A$ ,  $A^c$  whose area can be thought of as a representation of  $P(A^c)$ .

<b>Complement Probability Rule</b>
$P(A^c) = 1 - P(A)$

Verification

We can write  $SS$  as  $SS = A \cup A^c$  by the definition of the complement of an event. From the probability axiom 2,  $P(SS) = 1$  and so  $P(SS) = P(A \cup A^c) = 1$ . Finally, by definition  $A$  and  $A^c$  are mutually exclusive so by axiom 3 we can write  $P(A \cup A^c) = P(A) + P(A^c) = 1$ . Solving this for  $P(A^c)$

$$P(A^c) = 1 - P(A)$$

which is the desired result.